

Circles

1. Introduction to Circle

A circle is the locus of a point which lies in the plane in such a manner that its distance from a fixed point in the plane is constant. The fixed point is called the centre and the constant distance is called the radius of the circle.

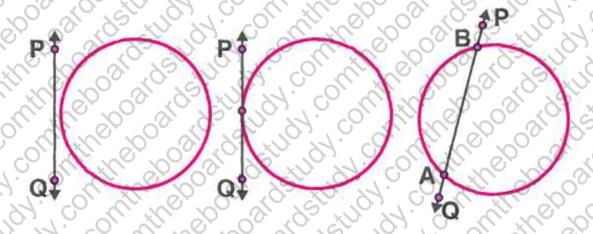
Circle and line in a plane

For a circle and a line on a plane, there can be three possibilities.

they can be non-intersecting

they can have a single common point; in this case, the line touches the circle.

they can have two common points: in this case, the line cuts the circle.



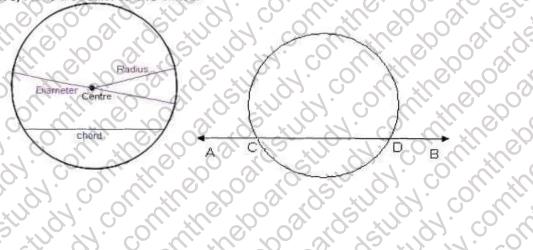
(i) Non intersecting (ii) Touching (iii) Intersecting

2. Parts of the circle

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- A line segment that joins any two points lying on a circle is called the chord of the circle.
- A chord passing through the centre of the circle is called **diameter** of the circle.
- A line segment joining the centre and a point on the circle is called radius of the circle.
- A line which intersects a circle at two distinct points is called a secant of the circle.

In the figure, AB is a secant to the circle.



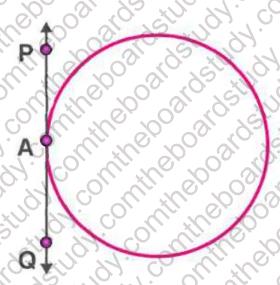
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3. Tangent to the circle

A tangent to the circle is a line that intersects the circle (touches the circle) at only one point. The word 'tangent' comes from the Latin word 'tangere', which means to touch The common point of the circle and the tangent is called point of contact.



In the figure, AB is a tangent to the circle and P is the point of contact.

- The tangent to a circle is a special case of the secant, when the two end points of its corresponding chord coincide.

 The tangent at any point of a circle is perpendicular to contact. This point of contact is a special case of the secant, when the two end points of its corresponding chord coincide.



A line drawn through the end of a radius (point on circumference) and perpendicular to it is a tangent to the circle.

5. Number of tangents on a circle

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- There is no tangent possible to a circle from the point (or passing through a point) lying inside the circle.
- "I'M" COMITTE DO BILDE There are exactly two tangents possible to a circle through a point outside the circle

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" Countille poake ichidy.cominex At any point on the circle, there can be one and only one tangent possible

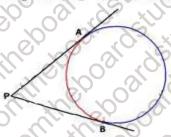
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6. Length of the tangent

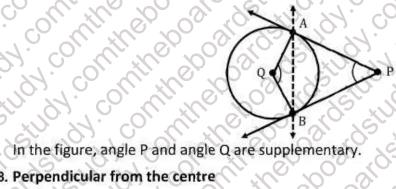
The length of the segment of the tangent from the external point P and the point of contact with the circle is called the length of the tangent.

- The lengths of tangents drawn from an external point to the circle are equal.
- The figure shows two equal tangents (PA = PB) from an external point P.



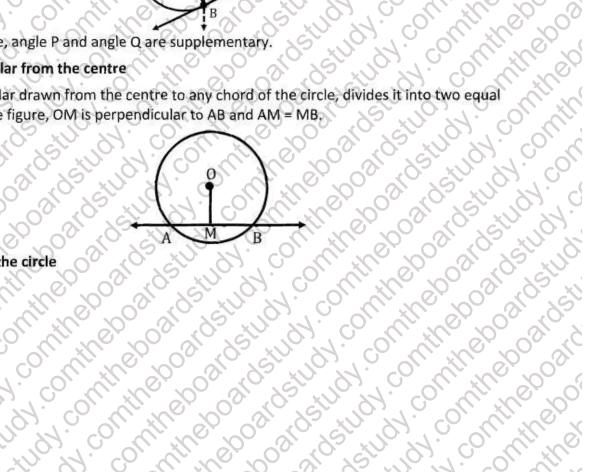
7. Angle between two tangents from an external point

- The centre of a circle lies on the bisector of the angle between the two tangents drawn from an external point.
- Angle between two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line segment joining the points of contact at the centre.



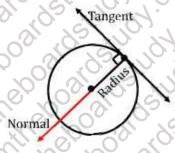
8. Perpendicular from the centre

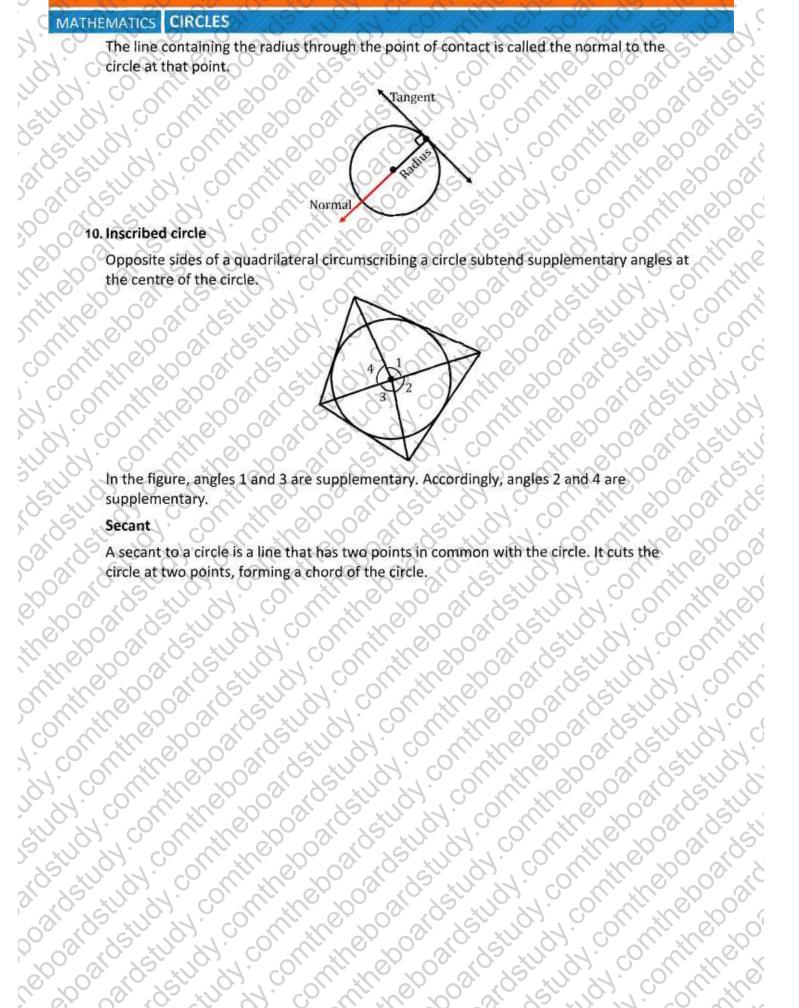
Perpendicular drawn from the centre to any chord of the circle, divides it into two equal parts. In the figure, OM is perpendicular to AB and AM = MB.



- Ardellidy confineboard Actual Contine board

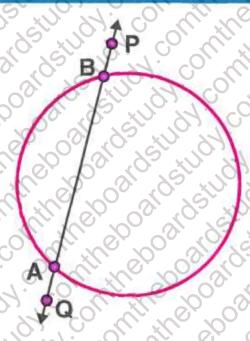
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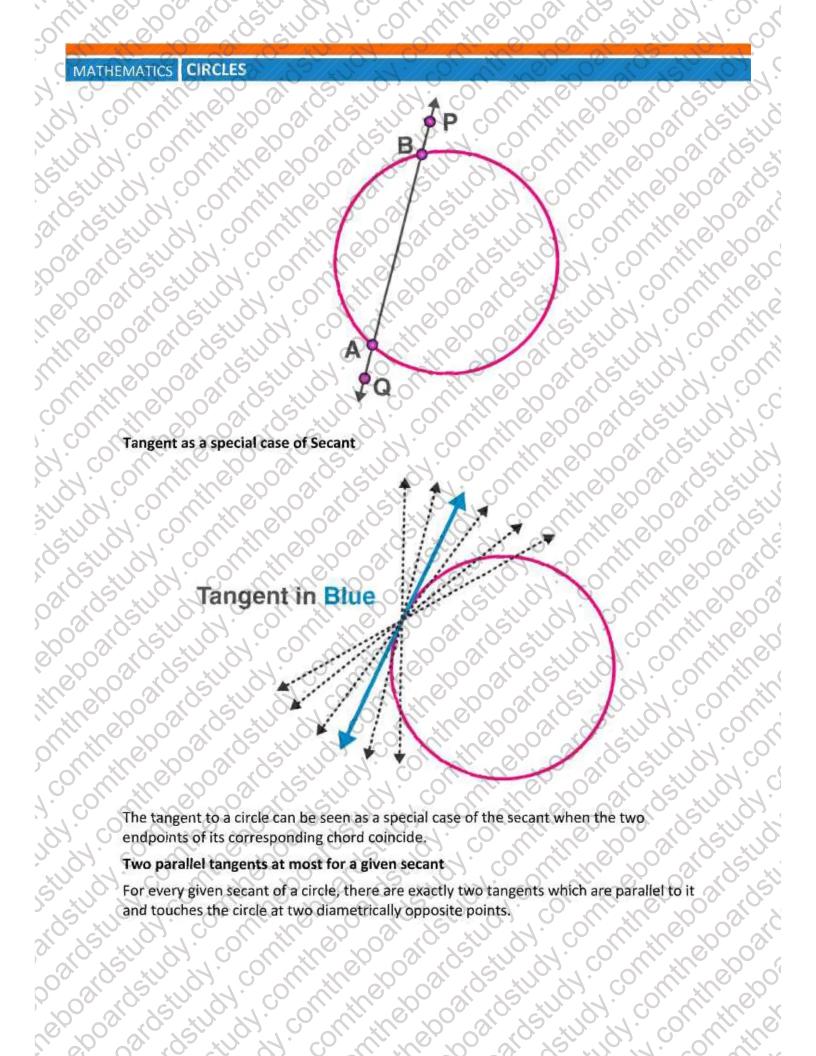




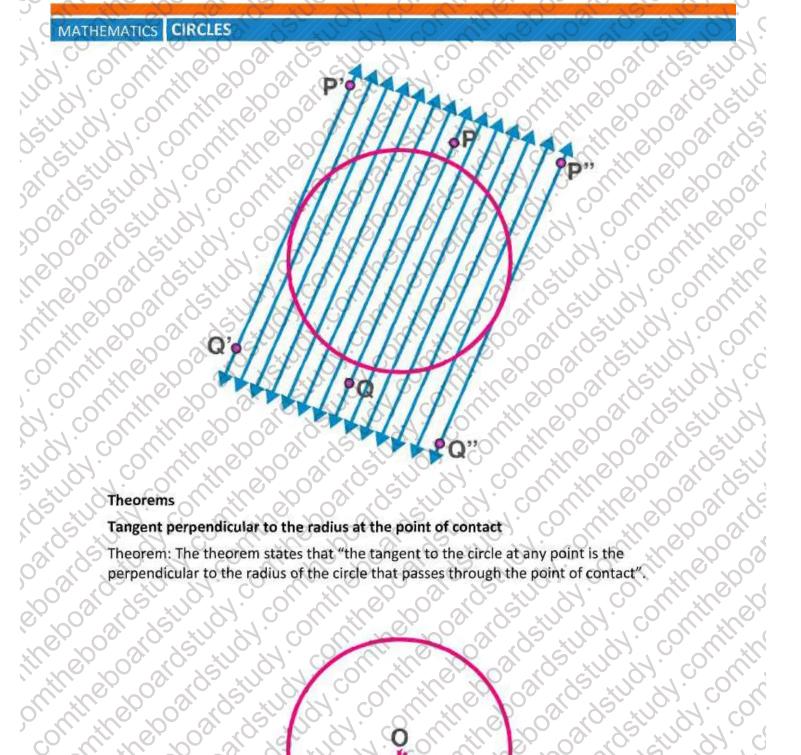
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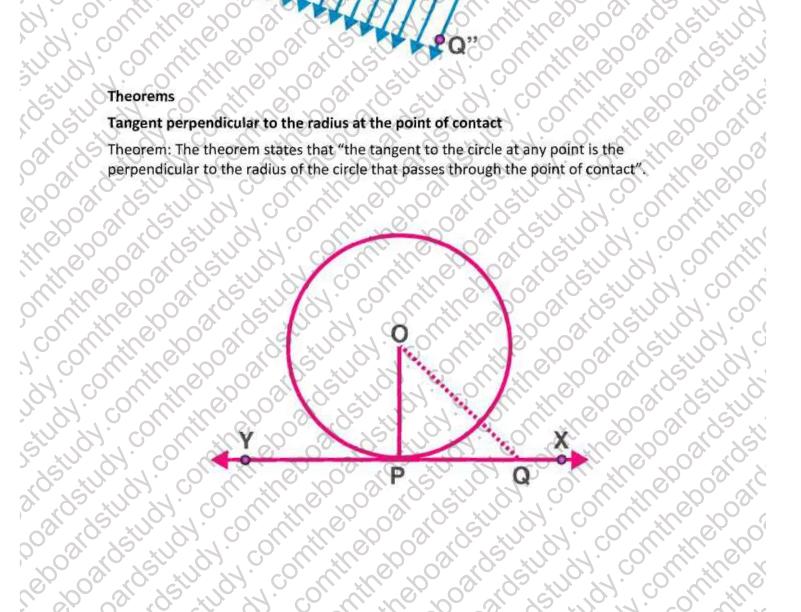
A secant to a circle is a line that has two points in circle at two points, forming a chord of the circle. Oardstudy comine boards tudy comine boards to the continue of Doardstudy. Contine to British of the boards to be a superior of the boards to be a superior





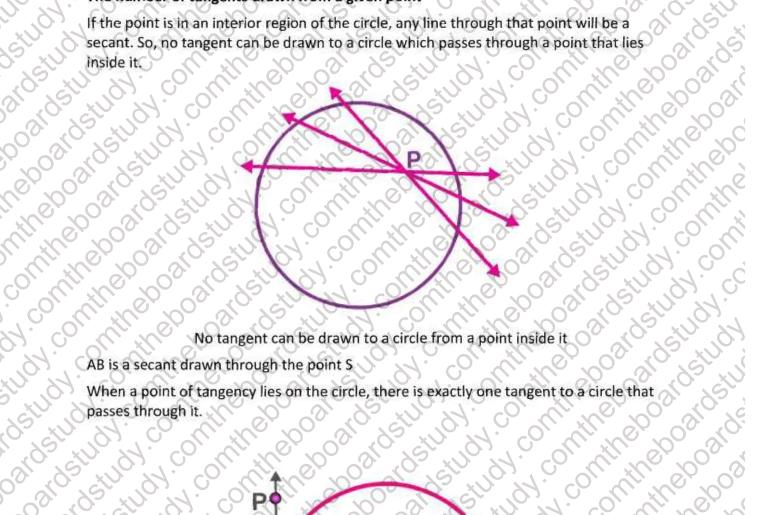
or every given secant of a circle, there are exactly two tanges and touches the circle at two diametrically opposite points. ardstudy.cor 3hOStdStUdy!





Here, O is the centre and OPLXY.

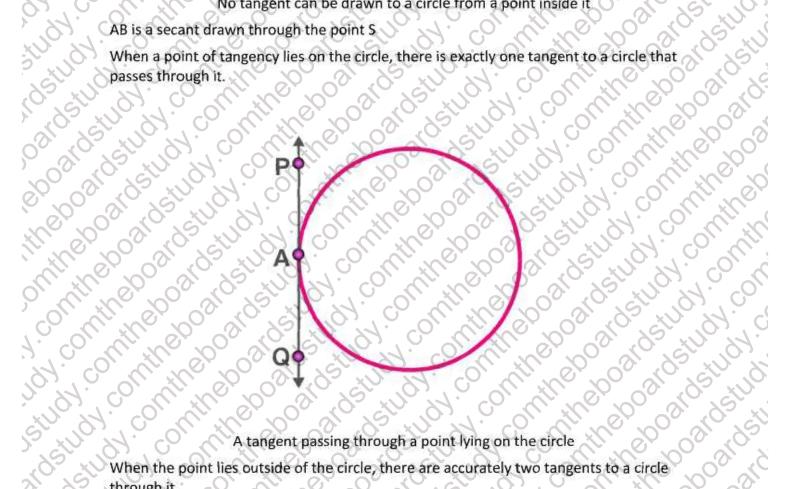
secont is in an interior region of the circle, any line through that point will be a secant. So, no tangent can be drawn to a circle which passes through a point that lies inside it.



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AB is a secant drawn through the point S

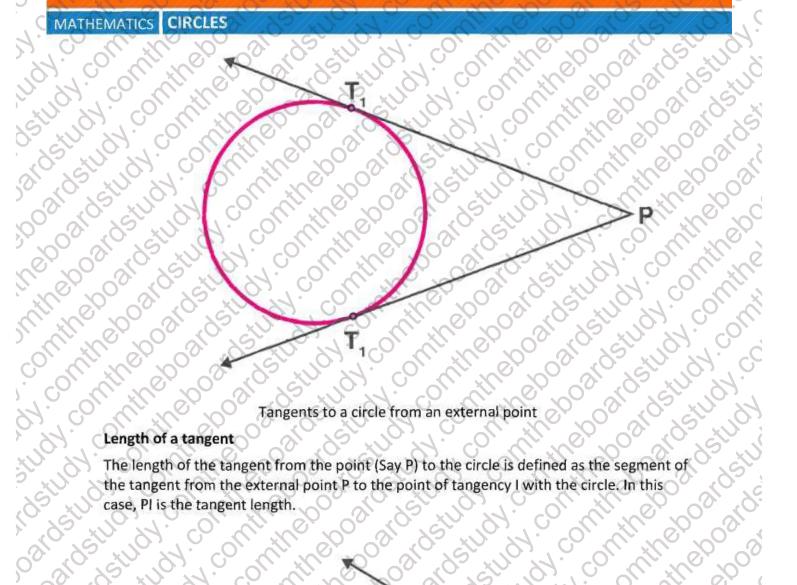
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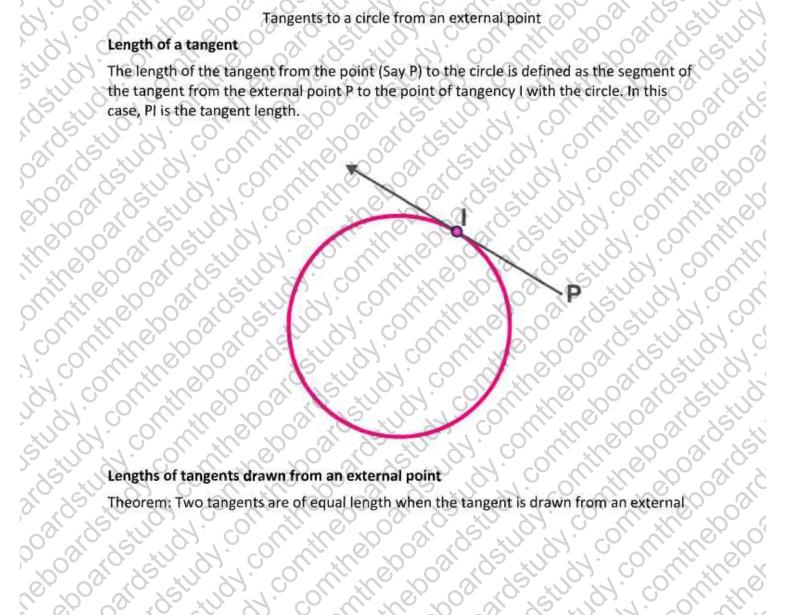
A tangent passing through a point lying on the circle

When the point lies outside of the circle, there are accurately two tangents to a circle through it i, Au contine boards to When the through it cultusposi Jetildy comi and study.co mardstudy HINA CORNIY wikepoard, nahoardsti An COURTURAL "Yelly A'CC -Ardstud



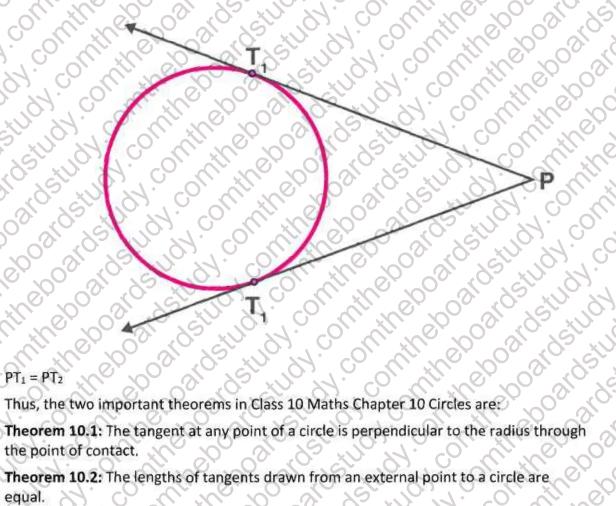
Length of a tangent

The length of the tangent from the point (Say P) to the circle is defined as the segment of the tangent from the external point P to the point of tangency I with the circle In this case, PI is the tangent length. the tangent from the external point P to the point of tangency I with the circle. In this



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point to a circle.



 $PT_1 = PT_2$

Interesting facts about Circles and its properties are listed below:

In two concentric circles, the chord of the larger circle, which touches the smaller circle, is bisected at the point of contact.

The tangents drawn at the ends of a diameter of a circle are parallel.

The perpendicular at the point of contact to the tangent to a circle passes through the centre.

The angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line segment joining the points of contact at the centre.

The parallelogram circumscribing a circle is a rhombus.

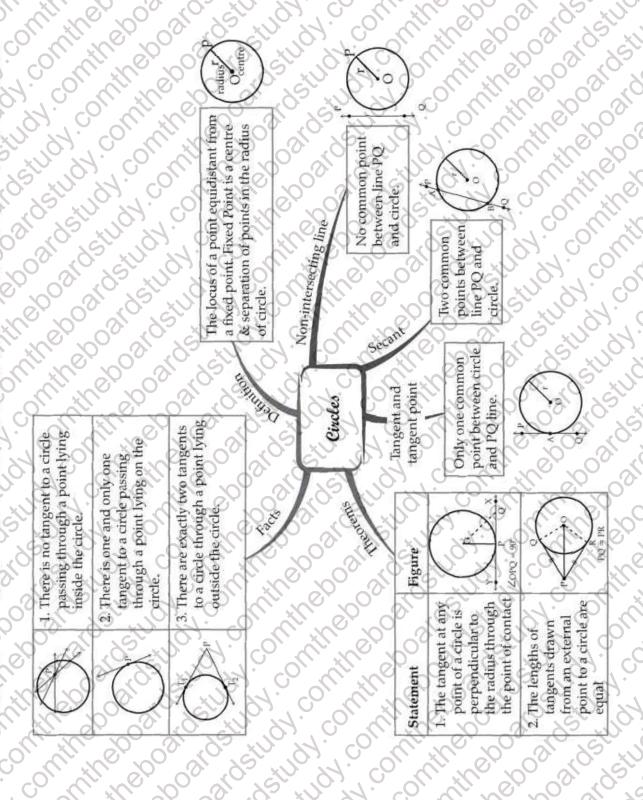
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Letildy. Contheboards! The opposite sides of a quadrilateral circumscribing a circle subtend supplementary I.A. COMINEDO ards angles at the centre of the circle. mardstudy.com and study comits contheboards'

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Multiple	Choice questions
1. Two circ circles. The	le touch each other externally at C and AB is a common tangent to the en, ∠ACB =
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(b) 45°	"A could the post of standy to out the
(c) 30°	71,94. Co. Williams to Sign Per 179 A. Cou Vill
(d) 90°	eingy, columning book of the inghistory
2. If TP and ∠PTQ is eq	TQ are two tangents to a circle with centre O so that $\angle POQ = 110^{\circ}$, then, ual to
(a) 60°	20 31 49 2111 194. 100 Will the book of 925 410 9
(b) 70°	3000 storesin 1927 cold till sopposition
(c) 80°	16 600 0 41 92 5111 94 CO WILLINGS 100 310 921
(d) 90°	Willing to signify to out the spool of
3. Tangent	s from an external point to a circle are
(a) equal	courtille book 1925 Fin 197. Courtille 60
(b) not equ	ay countilles possions in 1971 countilles
(c) parallel	1927 Co Chi 192 60 Co 193 197 19. Co 1911 14
(d) perpen	
4. Two partis 25 n cm ²	allel lines touch the circle at points A and B respectively. If area of the circle, then AB is equal to rough point of contact and passing through centre of circle is known as
(a) 5 cm	00, 310, 32, 179, 16, 04, 11, 16, 00, 00, 19, 21, 19, 94,
(b) 8 cm	900 SIC 925 470 94. COLULTINO 900 SIC 1251,116
(c) 10 cm	ineposition of the solution of significant
(d) 25 cm	in the soo die 9 ste 11927 could in the post of
5. A line th	rough point of contact and passing through centre of circle is known as
5. A line th (a) tangent (b) chord	rough point of contact and passing through centre of circle is known as

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- CIRCLES (c) normal 6. A tangent PQ at a point P of a circle of radius 5 cm meets a line through the centre O at a point Q onlikeboard neboardstud iheboardst (a) V119 cm (b) 13 cm (c) 12 cm (d) 8.5 cm 7. From a point P which is at a distance of 13 cm from the centre O of a circle of radius 5 cm, the pair of tangents PQ and PR to the circle are drawn. Then the area of the 8. At point A on a diameter AB of a circle of radius 10 cm, tangent XAY is drawn to the circle. The length of the chord CD parallel to XY at a distance 16 cm from A is

 (a) 8 cm

 (b) 10 cm quadrilateral PQOR is (d) 18 cm

 9. The tangents drawn at the extremities of the diameter of a circle are
 (a) perpendicular
 b) parallel
 none of these
 A circle is in-10. A circle is inscribed in a ΔABC having AB = 10cm, BC = 12cm and CA = 8cm and touching these sides at D, E, F respectively. The lengths of AD, BE and CF will be A child contine boards fully
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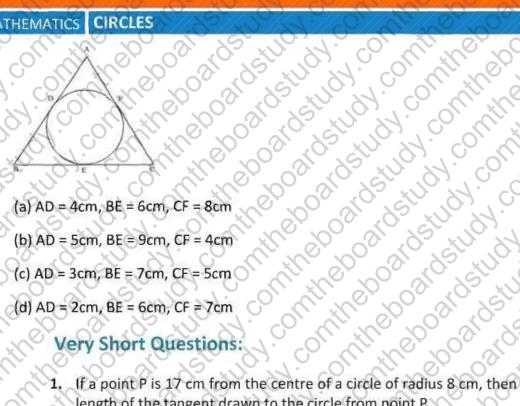
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(d) AD = 2cm, BE = 6cm, CF = 7cm

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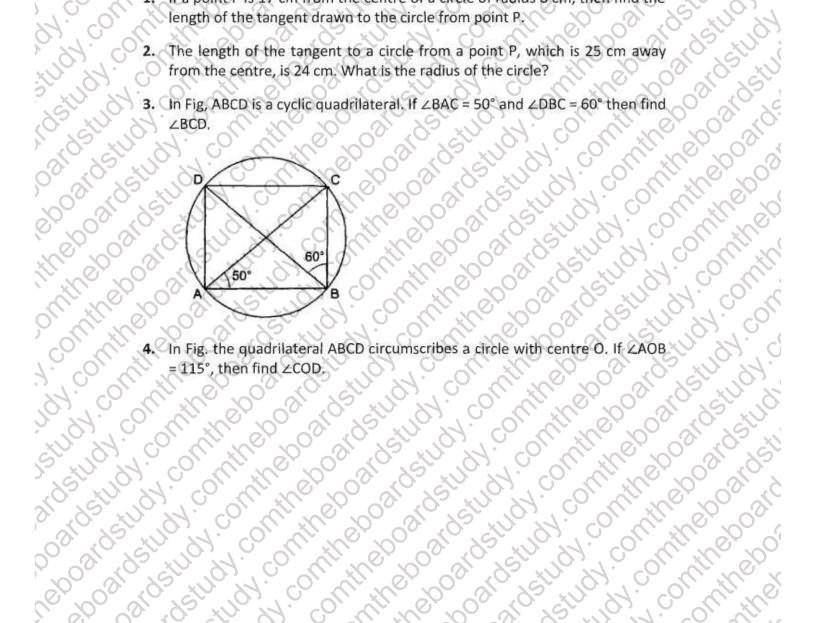
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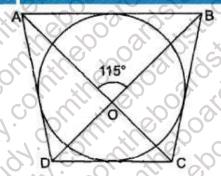
 If a point P is 17 cm from the centre of a circle of radius 8 cm, then find the length of the tangent drawn to the circle from point P.

 The length of the tangent to a circle from a point P, which is 2th rom the centre, is 24 cm. What is the radius of the circle?

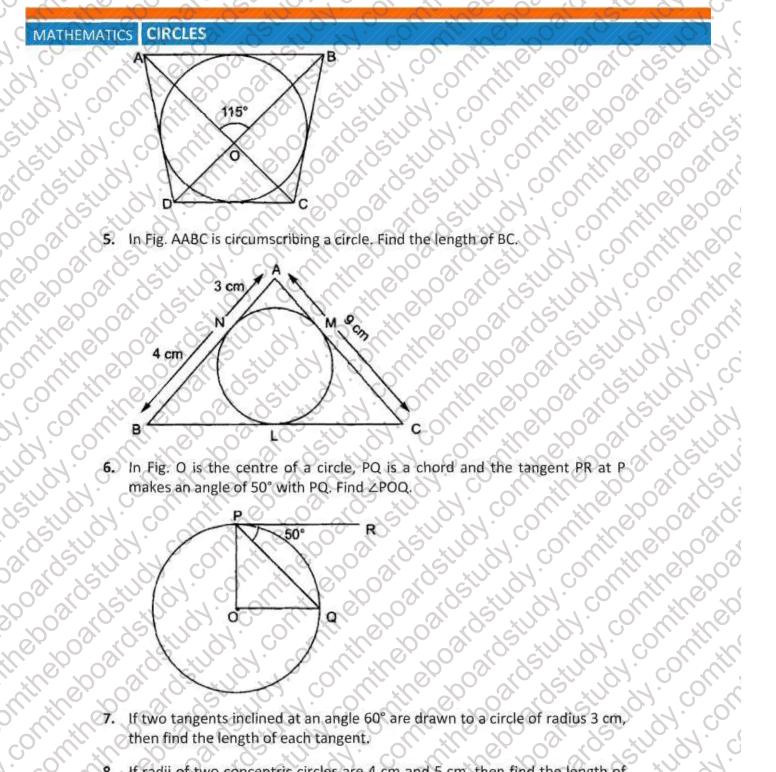
 Fig. ABCD is a cyclic quadrilateral. If ∠BAC ICD. cm from the centre of a circle of radius 8 cm, then find the largen of the tangent drawn to the circle from point P.
 2. The length of the tangent to a circle from a point P, which is 25 cm away from the centre, is 24 cm. What is the radius of the circle?
 3. In Fig. ABCD is a cyclic quadrilateral. If ∠BAC = 50° and ∠BCD.



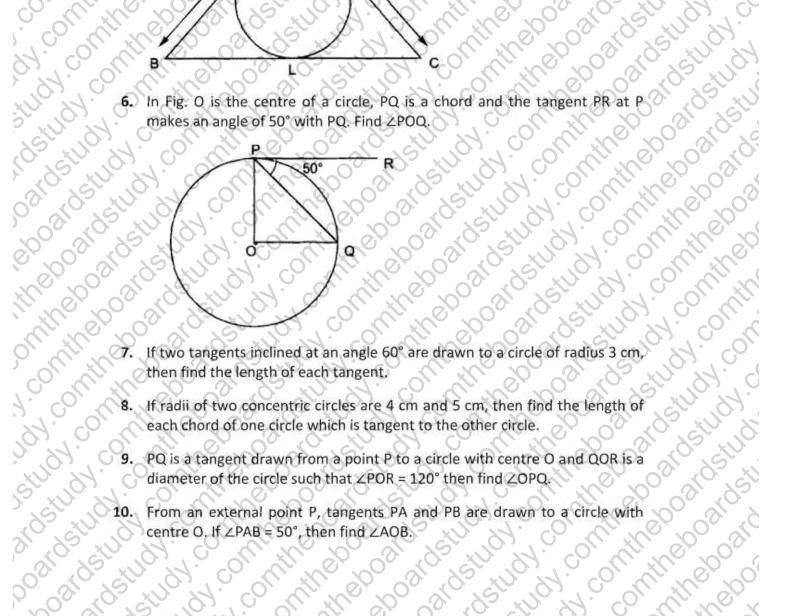
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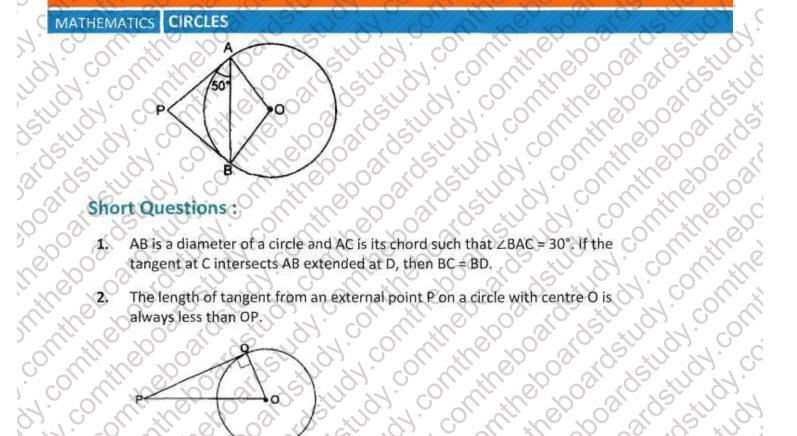
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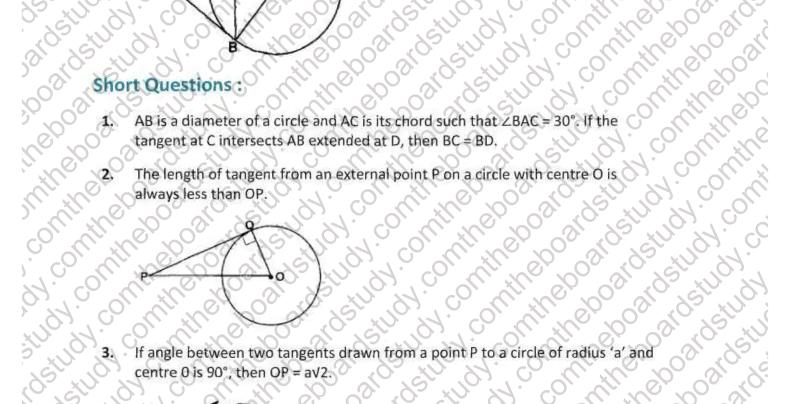
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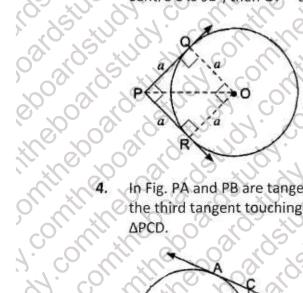
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- AB is a diameter of a circle and AC is its chord such that tangent at C intersects AB extended at D, then BC = BD.

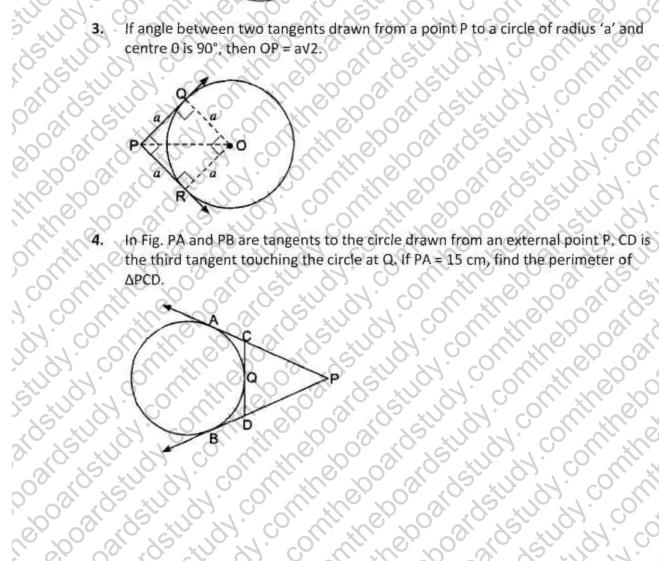
 2. The length of tangent from an external point P always less than OP.



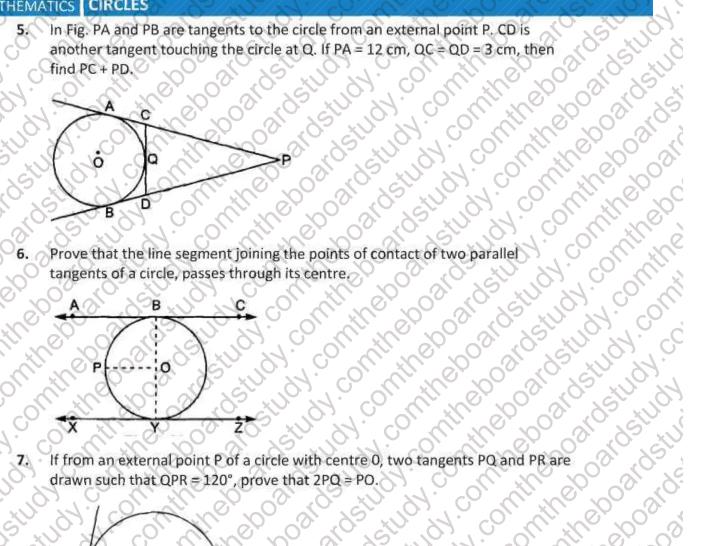


If angle between two tangents drawn from a point P to a circle of radius 'a' and centre 0 is 90°, then OP = av2.

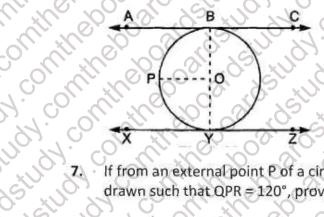
PA and PB are tangents to the circle drawn for dangent touching the circle at Q, if for dangent to Q, if IED GIVE THE COUNTY OF THE POST OF THE POS

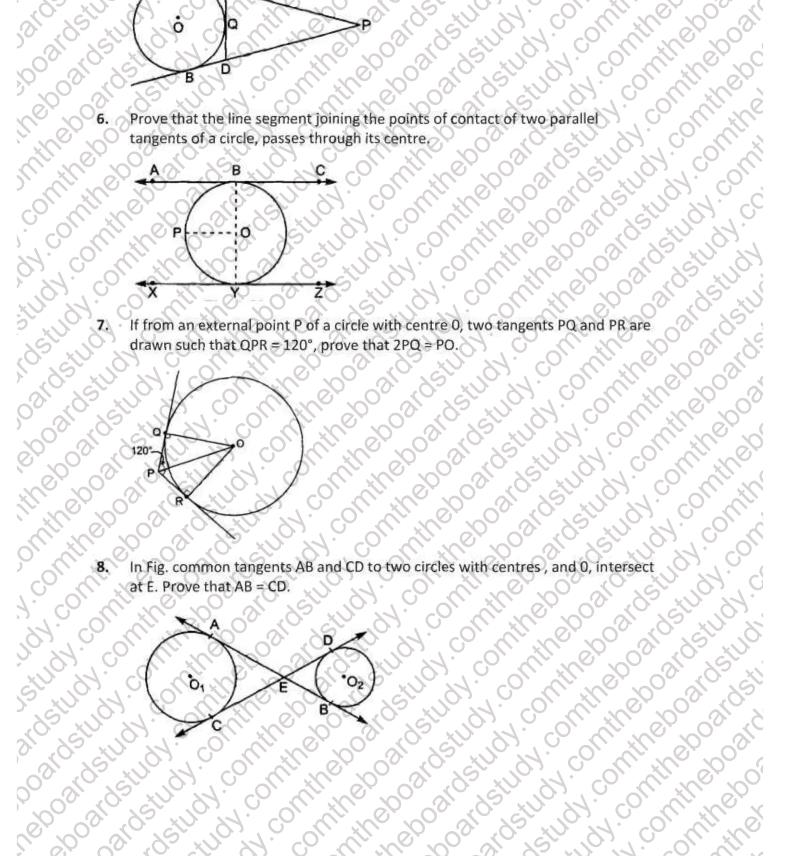


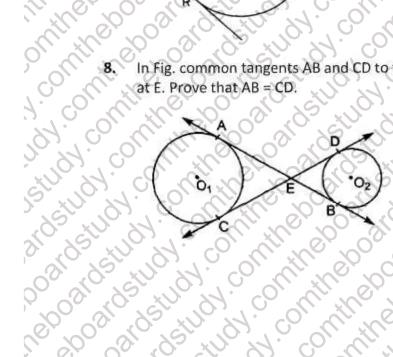
detudy.comineboarden W. Study comittee boards tud In Fig. PA and PB are tangents to the circle from an external point P. CD is



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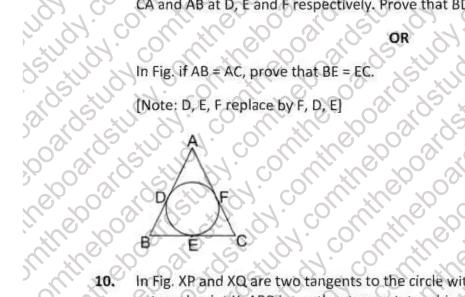


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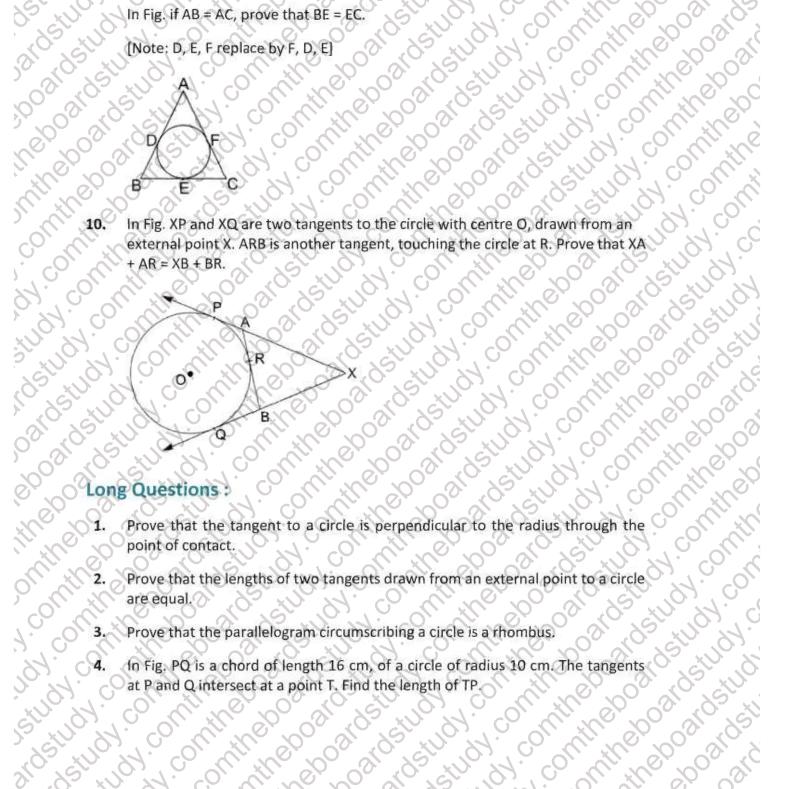
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In Fig. if AB = AC, prove that BE = EC.

[Note: D, E, F replace by F, D onthe boards that contine boards the incircle of an isosceles triangle ABC, in which AB = AC, touches the sides BC, COMILIEDO SI DE LINDA COMILA idy comine postdetudy co CA and AB at D, E and F respectively. Prove that BD = DC.



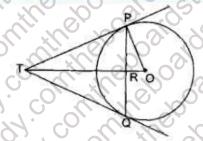
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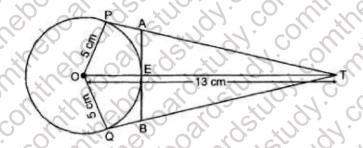
ong Questions:

- Prove that the parallelogram circumscribing a circle is a rhombus.
- ough the several point to a circle over that the parallelogram circumscribing a circle is a rhombus.

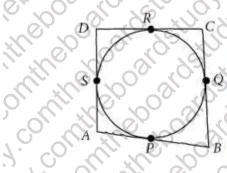
 In Fig. PQ is a chord of length 16 cm, of a circle of radius 10 cm. The tangents at P and Q intersect at a point T. Find the length of TP. on and a findly continuous defindry. ents, comine book hahnardstudy comine mine hoardstudy com annardstudy.comthe And comineboards uepoarde tudy com "Hethidy contineboard in contheboardstuc - And Study contine of contheboards tudy

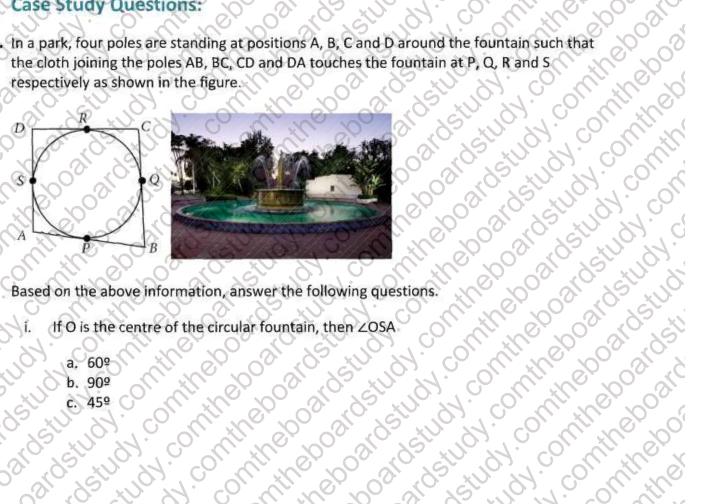


- JAY COMINEDO 35tudy contine 2ardstudy.comit If PQ is a tangent drawn from an external point P to a circle with centre O and QOR is a diameter where length of QOR is 8 cm such that ∠POR = 120°, then find OP and PQ.
- Y. contine postdetudy comits In Fig. O is the centre of a circle of radius 5 cm. T is a point such that OT = 13 cm and OT intersects circle at E. If AB is a tangent to the circle at E, find the ing A countilise post of stridi length of AB, where TP and TQ are two tangents to the circle.



1. In a park, four poles are standing at positions A, B, C and D around the fountain such that the cloth joining the poles AB, BC, CD and DA touches the fountain at P, Q, R and S respectively as shown in the figure.





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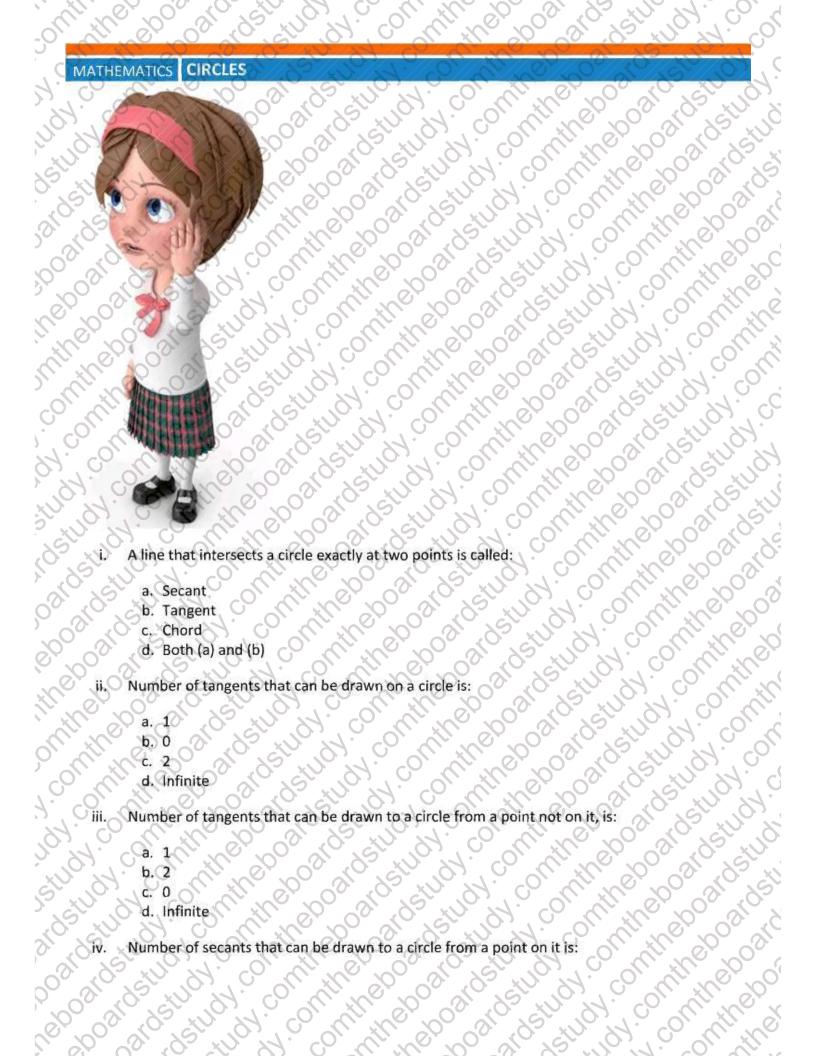
- ii. Which of the following is correct?

 a. AS = AP
 b. P = BQ
 c. CO
- AS = AI b. P = BQ c. CQ = CR d. All of th
- d. All of these

 If DR = 7cm and AD= 11cm, then AP =

 a. 4cm
 b. 18cm
 c. 7cm
 d. 11cm

) is the centre of the Milheboard contineboats iv. If O is *
- 2. Smita always finds it confusing with the concepts of tangent and secant of a circle. But this time she has determined herself to get concepts easier. So, she started listing down the differences between tangent and secant of a circle, along with at points in question form are listed. IED GIUSUUM, CORTHODORIUS LIUN, A SOUTH THE POOR TO SHIP OF THE PROPERTY OF TH J. Heiligh. Coulting to Still A. Columbia. The Columbia of the LUNY CORTINED ORIGINAL CORTINE Julius of Study of the boards to the continuous of the continuous our deflidy. On the loan deflidy. On h Showing the house of the house ooalds judy continue oo alds july Weboat grind hours in the boat of the hours IIII Shook de tildy continuo and e tildy continuo a



- a. Infinite

- oardstudy.comineboard one point is called: A line that touches a circle at only
 - a. Secant
 - b. Chord
 - c. Tangent
 - Diameter

Assertion Reason Questions

- 32 de tudy contine poarde i Directions: In the following questions, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:
- a. Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A)
- b. Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).

Assertion (A): In a circle of radius 6 cm, the angle of a sector is 60°. Then the area of the sector is 132/7 cm².

Reason (R): Area of the circle with radius

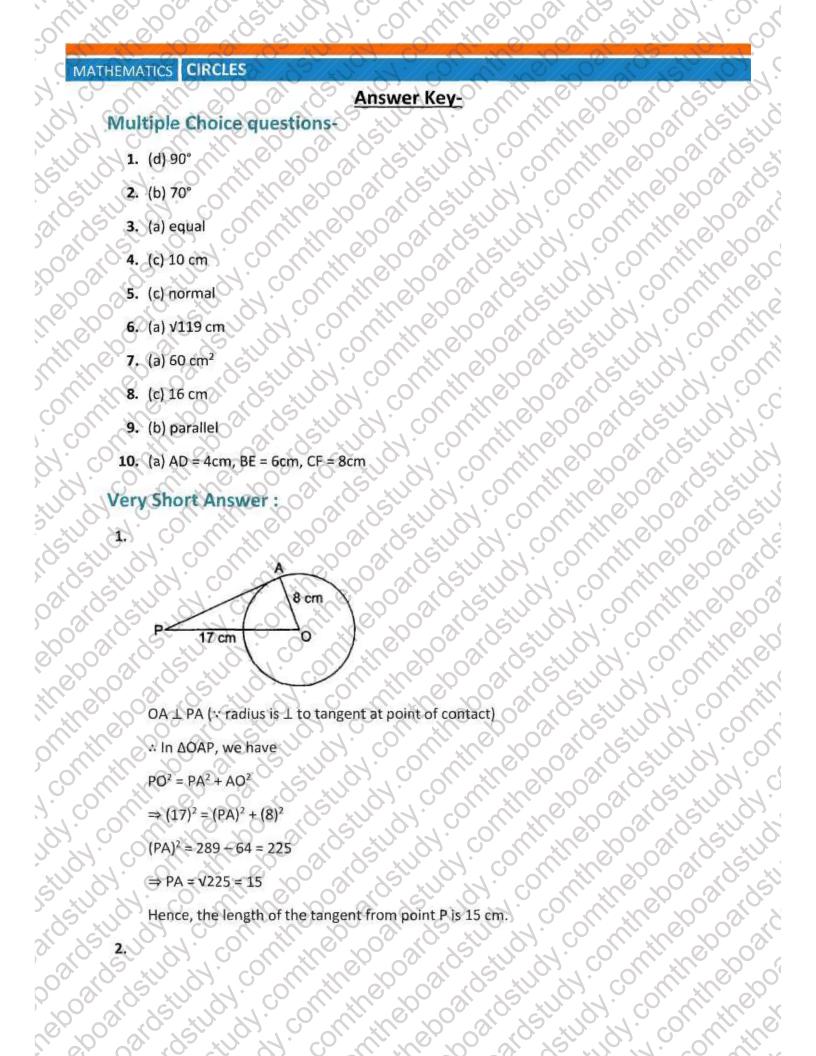
- 2. Directions: In the following questions, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:
- a. Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A)

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- b. Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A). in the board study
- Assertion (A) is true but reason (R) is false.
- d. Assertion (A) is false but reason (R) is true

Assertion (A): If the circumference of a circle is 176 cm, then its radius is 28 cm " Cultipeposic ard study comi mardstudy.cc

mineboards cultueposi Reason (R): Circumference $2\pi \times radius$

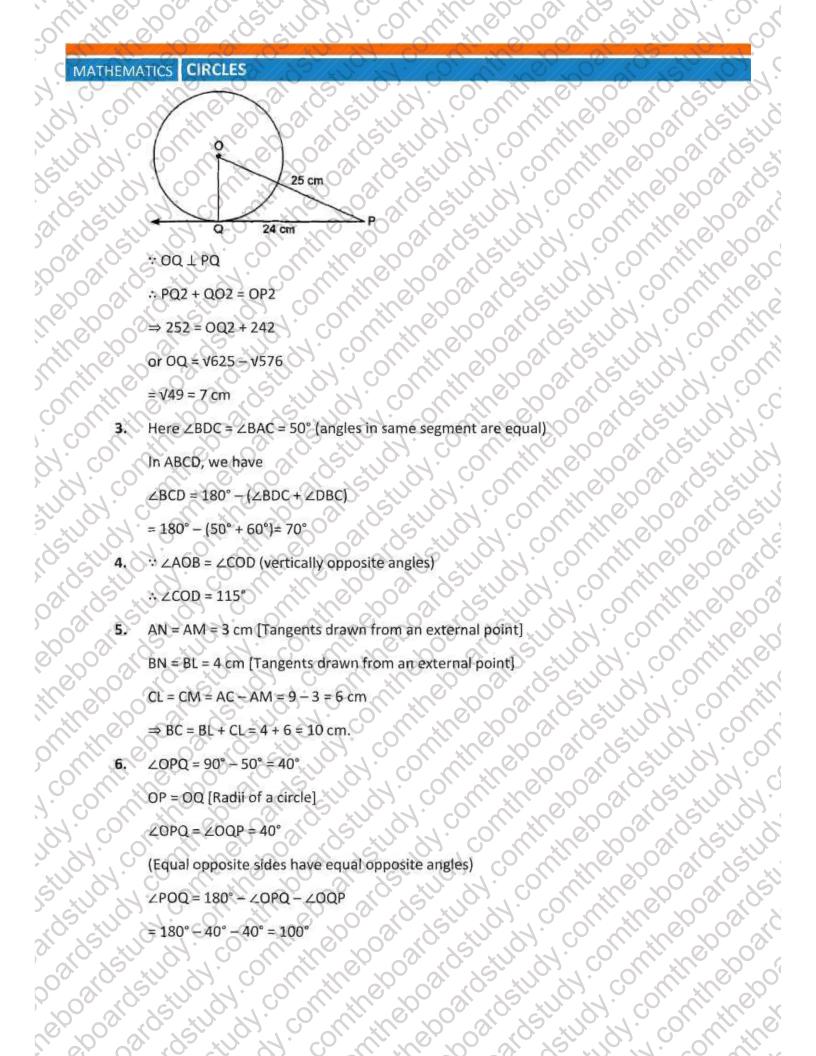


$$PO^2 = PA^2 + AO^2$$

$$\Rightarrow$$
 (17)² = (PA)² + (8)³

$$(PA)^2 = 289 - 64 = 225$$

$$\Rightarrow$$
 PA = $\sqrt{225}$ = 15



$$\Rightarrow$$
 252 = OQ2 + 242

or
$$OQ = \sqrt{625 - \sqrt{576}}$$

$$= \sqrt{49} = 7 \text{ cm}$$

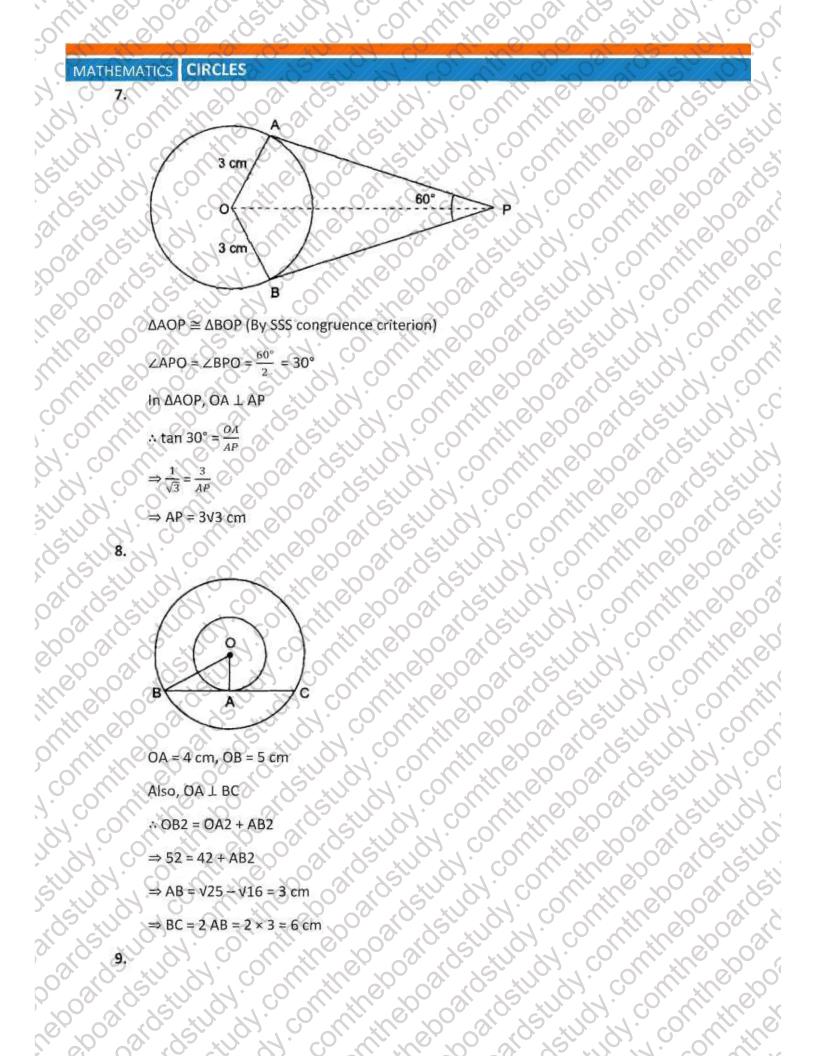
$$\angle BCD = 180^{\circ} - (\angle BDC + \angle DBC)$$

$$= 180^{\circ} - (50^{\circ} + 60^{\circ}) = 70^{\circ}$$

... external point]
... om an external point]
... + 6 = 10 cm... + 6 = 10 cm... $-50^{\circ} = 40^{\circ}$ = 00 [Radii of a circle]... $20\text{PQ} = 20\text{QP} = 40^{\circ}$ (Equal opposite sides have equal opposite angles) $2\text{PQQ} = 180^{\circ} - 20\text{PQ} - 20\text{QP}$ $= 180^{\circ} - 40^{\circ} - 40^{\circ} = 100^{\circ}$

$$CL = CM = AC - AM = 9 - 3 = 6 cm$$

$$\Rightarrow$$
 BC = BL + CL = 4 + 6 = 10 cm.



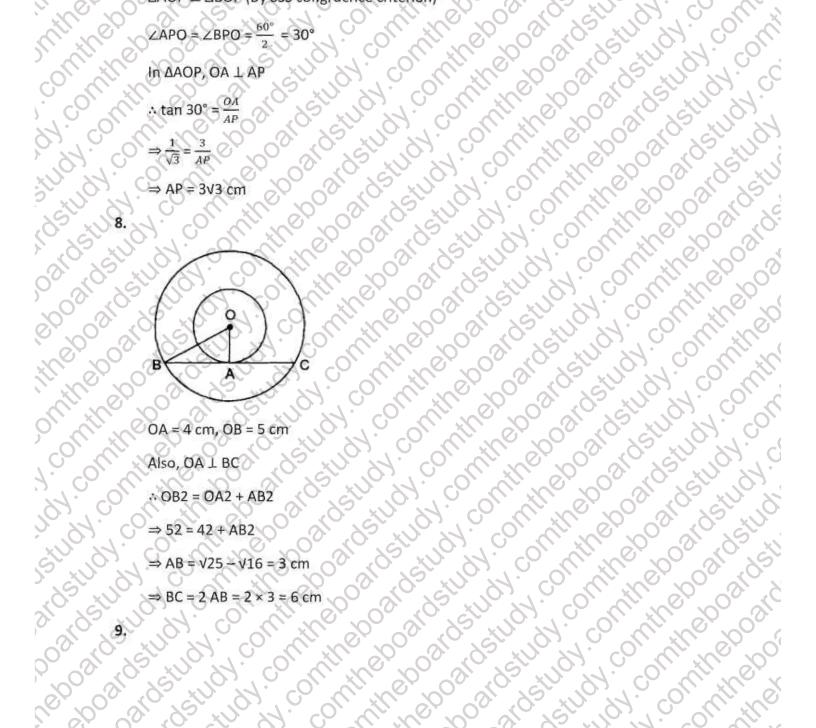
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$$\angle APO = \angle BPO = \frac{60^{\circ}}{2} = 30^{\circ}$$

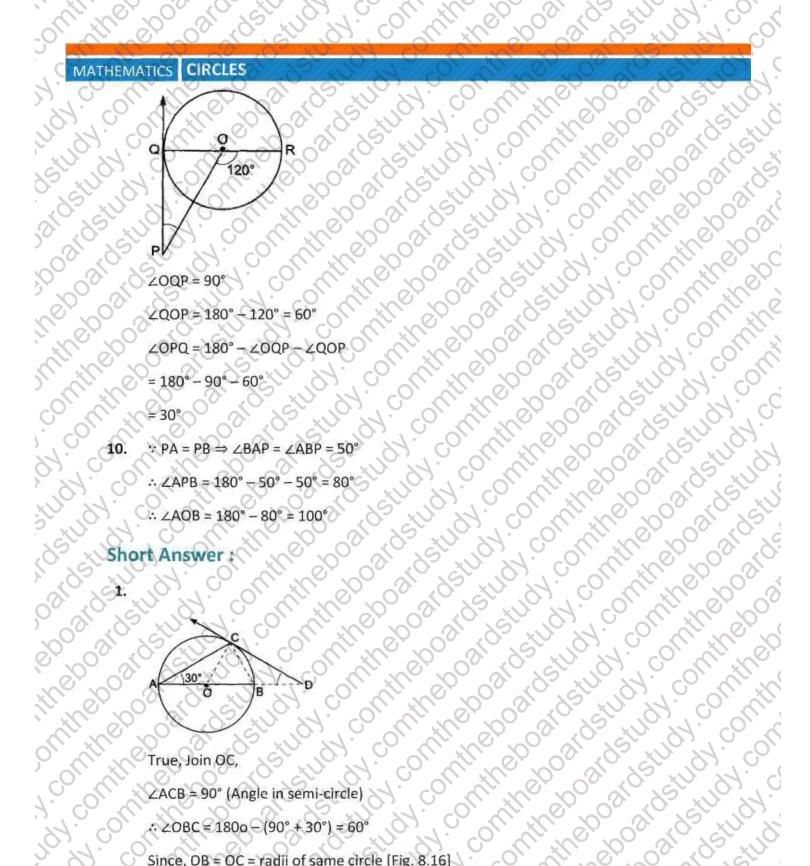
$$\therefore$$
 tan 30° = $\frac{OA}{AP}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{3}{AP}$$

$$\Rightarrow$$
 AP = 3v3 cm

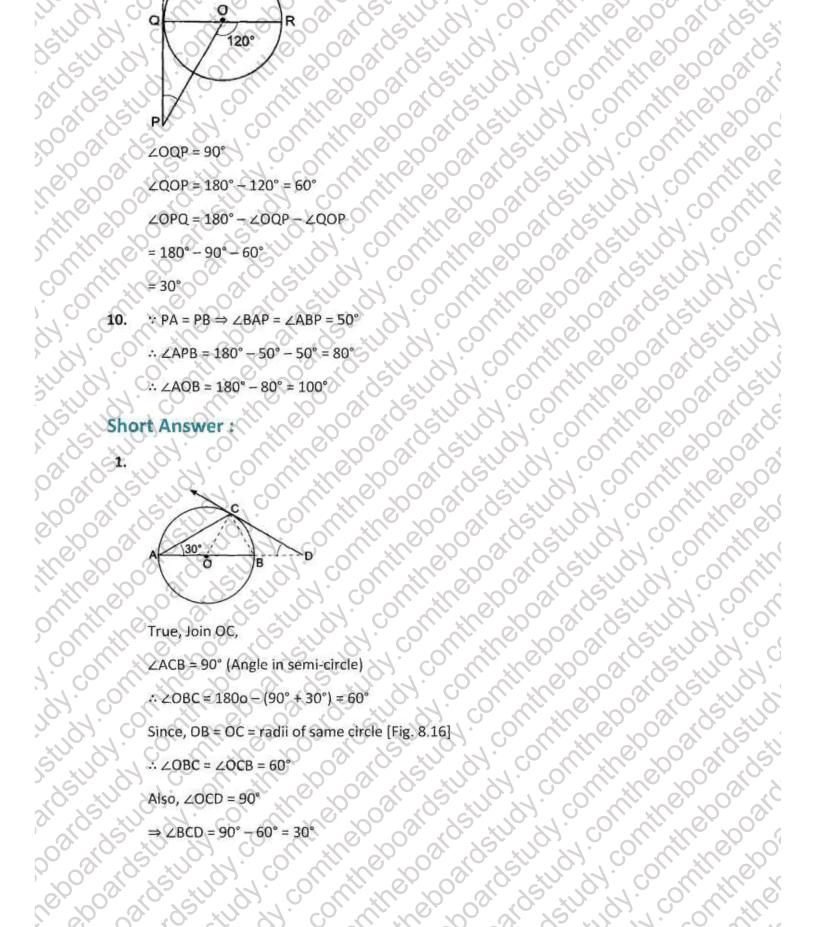


$$\Rightarrow$$
 BC = 2 AB = 2 × 3 = 6 cm



$$\angle OPQ = 180^{\circ} - \angle OQP - \angle QOP$$

10.
$$PA = PB \Rightarrow \angle BAP = \angle ABP = 50^\circ$$



$$\Rightarrow$$
 \angle BCD = 90° -60 ° = 30°

 $DC = 30^{\circ}$ DC = BDTrue, let PQ be the tangent from the external point P.

Then ΔPQQ is always a right angled triangle with Ω is always less than QP.

"rue, let PQ and PR be the tangent from the external point P. ∠BCD = ... BC = BD z pe the ta

then ΔPQO is always a
is always less than OP.

3. True, let PQ and Since

Since
$$ZP = 90^\circ$$
, so $\angle QOR = 90^\circ$

Also,
$$OR = OQ = a$$

$$\Rightarrow$$
 $OP = \sqrt{a^2 + a^2} = \sqrt{2a^2} = a\sqrt{2}$

$$\therefore PA = PB = 15 \text{ cm}$$

Now, Perimeter of
$$\triangle PCD = PC + CD + DP = PC + CQ + QD + DP$$

∴ the hypotenuse. So, PQ

∴ a square

∴ PA and PB are tangent from same external point

∴ PA ∈ PB = 15 cm

→ W, Perimeter of ΔPCD = PC + CD + DP = PC

C + CA + DB + DP

+ PB = 15 + 15 = 30 cr

PC + CA = Pr $\sqrt{a^2 + a^2} \approx \sqrt{2a^2} = a\sqrt{2}$ A and PB are tangent from same external point $\therefore PA = PB = 15 \text{ cm}$ Now, Perimeter of $\Delta PCD = PC + CD + DP = PC + CQ + QD + DP$ = PC + CA + DB + DP = PA + PB = 15 + 15 = 30 cm5. PA = PC + CA = PC + CQ (v CA = CQ (tangents drawn An from external point are equal)] $\Rightarrow 12 \neq PC + 3 = PC = 9 \text{ cm}$ $\therefore PA = PB - PA - AC = PB - BD$ $\Rightarrow PC = PD$ $\therefore PD = 9 \text{ cm}$ (Hence, PC + PD = 18 cm)
6. Let the tangents to a circle with centre O be ABC and XYZ.
Construction? Join GB and OY.

$$\Rightarrow$$
 12 = PC + 3 = PC = 9 cm

,eboards

Draw OPLIAC

Since AB||PO

 $\angle ABO = 90^\circ$ (A tangent to a circle is perpendicular to the radius through the point of contact) $10^\circ + \angle POB = 180^\circ = \angle POB = 90^\circ$ $10^\circ + \angle POY = 90^\circ$ Study.comineboardstud Hence, BOY is a straight line passing through the centre of the circle. Given, $\angle QPR = 120^\circ$ (adius is perpendicular to the tangent at the point $QPR = 90^\circ$)

$$\angle POB + \angle POY = 90^{\circ} + 90^{\circ} = 180^{\circ}$$

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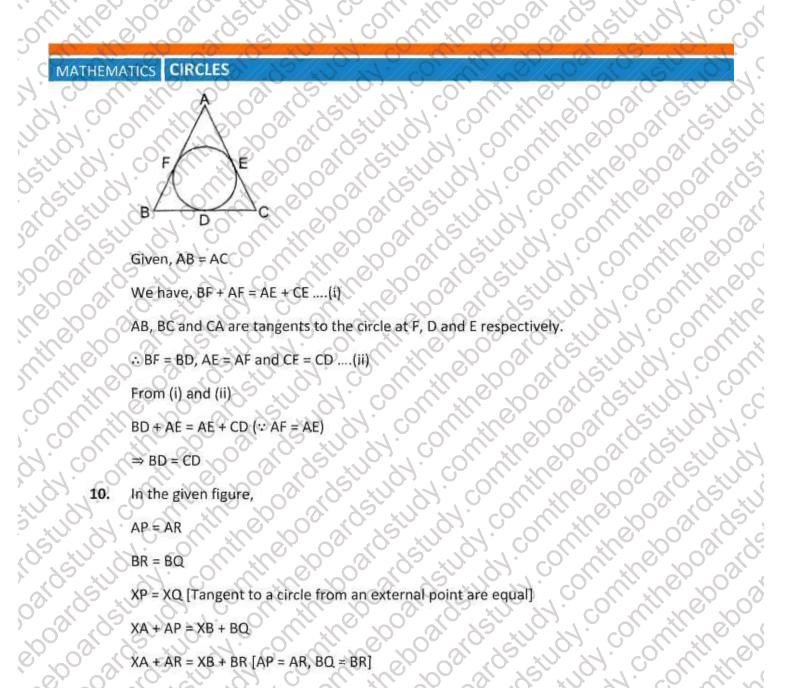
Milheboal ontheboa COWITYSK

eboardstudy contine to a circle from an external point are equally inclined to the the centre to that point) $\frac{PQ}{PO} \implies \frac{1}{2} = \frac{PQ}{PO}$... of a circle from an external point are equally in ... ing the centre to that point) PQ = PQ PQ = PQ 2PQ = PQ 2PQ = PQ8. AE = CE and BE = ED [Tangents drawn from an external point are equal]

On addition, we get AE + BE = CE + ED $2QPO = 60^{\circ}$ $\Rightarrow AB = CD$ 9. Y. contine boards tudy contine boards tudy contine boards tudy.

In
$$\triangle QPO$$
, $\cos 60^\circ = \frac{PQ}{PO} \Rightarrow \frac{1}{2} = \frac{PQ}{PO}$

Onthe Doards tudy contine boards tudy contine



ac + ČE(i)

and CA are tangents to the circl

BF = BD, AE = AF and CF = CD(ii)

From (i) and (ii)

BD + AE = AE + CF

→ AE =
⇒ BD = CD

BR = BQ

Long Answer:

...respectively.

...respectiv

an external point are equal]

Answer:

Given: A circle C(O,r) and a tangent AB at a point P.

To Prove: OP \perp AB.

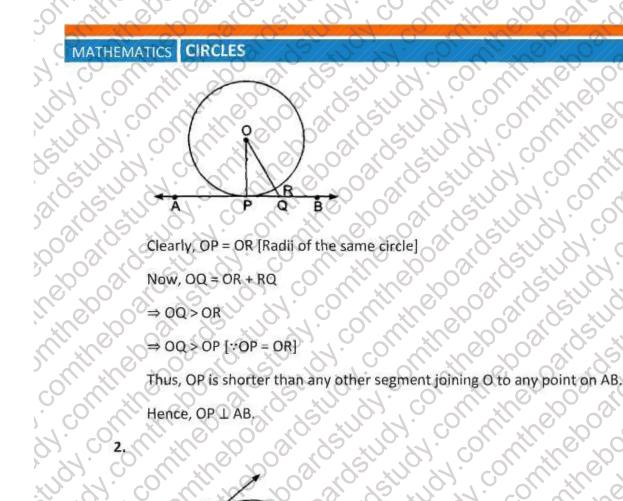
Construction: Take any point I, other than ruppose OQ meets the circle at R.

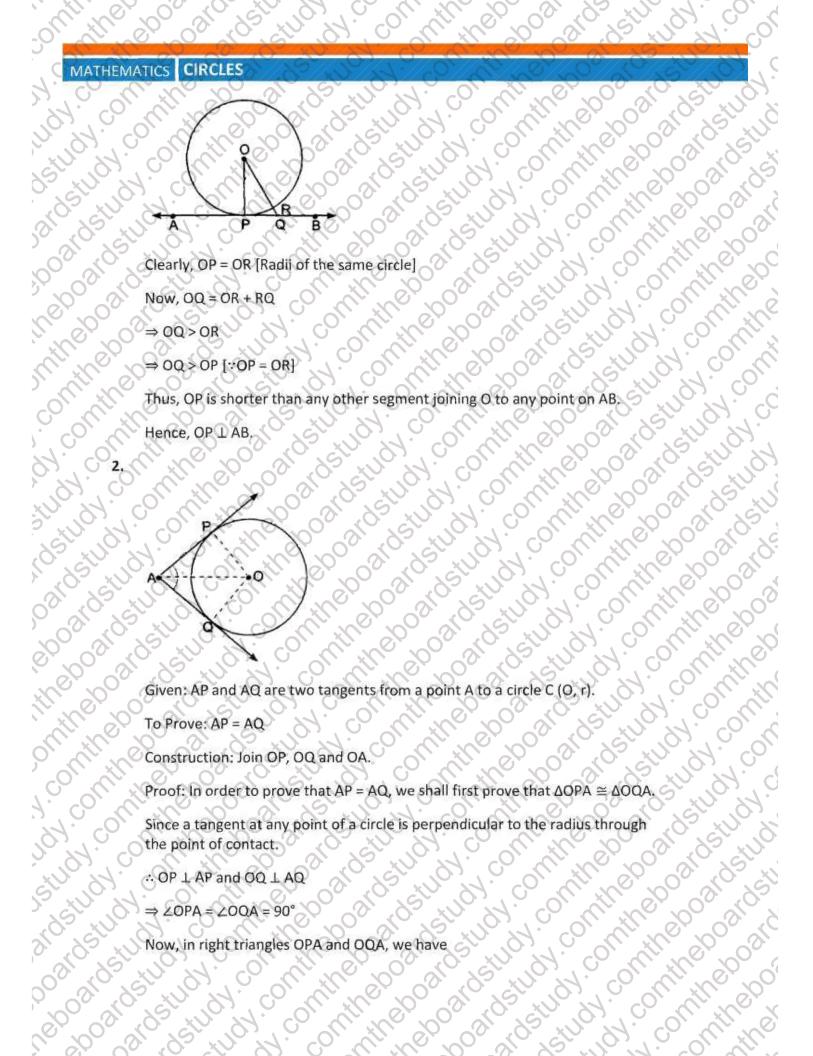
20f: We know that arrushortest one for rove the force of the circle at R. To Prove: OP ⊥ AB.

Construction: Take any point I, other than P, on the tangent AB. Join OQ.

Suppose OQ meets the circle at R.

Proof: We know that among all line segments joining the point Prove that OP is shorter than any other segments. Activity Contine boards tild , detildy comine And Conthebo contine boards mardstudy.cot ardefudy.comily in coulthepositi 3hnardstudy.cc mine boardstur -Ardstudy.com rahnardstudy Reposition



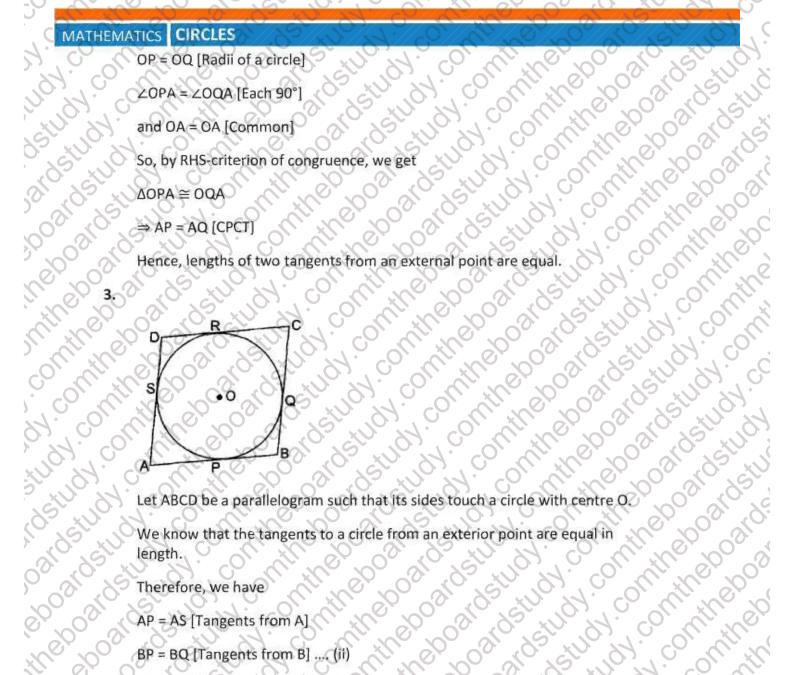


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MATHEMATICS

∠OPA = ∠OQA [Each 90°]

 $ΔOPA \cong OQA$ ⇒ AP = A



that? are & Contine Doard

Offilialing of the state of the (iii)

..... (iii)

..... (iii)

..... (iii)

..... (iv)

Adding (i), (ii), (iii) and (iv), we have (AP + BP) + (CR + DR) = (AS + DS) + (BQ + CQ) AB + CD = AD + BC B + AB = BC + BC [:: ABCD is a paraller] $B = 2BC \Rightarrow AB = BC$ I, AB = BC = CD

$$(AP + BP) + (CR + DR) = (AS + DS) + (BQ + CQ)$$

Hence, ABCD is a rhombus.

4.

To find:
$$TP$$
 $PR = RQ = \frac{16}{2} = 8 \text{ cm}$ [Per lin $\triangle OPR$

$$OR = \sqrt{OP^2 - PR^2}$$

$$= \sqrt{10^2 - 8^2} = \sqrt{100 - 64}$$

$$= \sqrt{36} = 6 \text{ cm}$$

In
$$\triangle OPR$$

$$OR = \sqrt{0P^2 - 8}$$

$$= \sqrt{36} = 8$$

Let $\angle POR$ be θ
In $\triangle POR$, $\tan \theta = \frac{PR}{RO} = \frac{8}{6}$

In
$$\triangle POR$$
, $\tan \theta = \frac{TR}{RO} = \frac{3}{6}$
 $\tan \theta = \frac{4}{3}$

We know, $OP \perp TP$ (Point of contact of a tang In $\triangle OTP$, $\tan \theta = \frac{OP}{TP} \implies \frac{4}{3} = \frac{10}{TP}$
 $TP = \frac{10 \times 3}{4} = \frac{15}{2} = 7.5 \text{ cm.}$

5. Let O be the centre and QOR = 8 cm is diamed that $\angle POR = 120^{\circ}$

Now, $OQ = OR = \frac{8}{2} = 4 \text{ cm}$
 $\angle POQ = 180 - 120^{\circ} = 60^{\circ}$ (Also $OQ \perp PQ$)

Now, in right $\triangle POQ$.

that
$$\angle POR = 120^{\circ}$$

Now,
$$OQ = OR = \frac{8}{2} = 4 \text{ cm}$$

$$\angle POQ = 180 - 120^{\circ} = 60^{\circ} \text{ (Linear pair)}$$
Also
$$OQ \perp PQ$$
Now, in right $\triangle POQ$.
$$\cos 60^{\circ} = \frac{OQ}{PO}$$

$$\Rightarrow \qquad \frac{1}{2} = \frac{OQ}{PO} \Rightarrow \frac{1}{2} = \frac{4}{PO}$$

$$\Rightarrow \qquad PQ = 8 \text{ cm}.$$
Again, $\tan 60^{\circ} = \frac{PQ}{OQ} \Rightarrow \sqrt{3} = \frac{PQ}{4} \Rightarrow PQ = 4\sqrt{3} \text{ cm}$

$$\cos 60^\circ = \frac{OQ}{PO}$$

$$\frac{1}{2} = \frac{OQ}{PO} \implies \frac{1}{2} = \frac{4}{PO}$$

$$PO = 8 \text{ cm}$$

Also
$$OQ \perp P$$

Now, in right ΔPOQ .

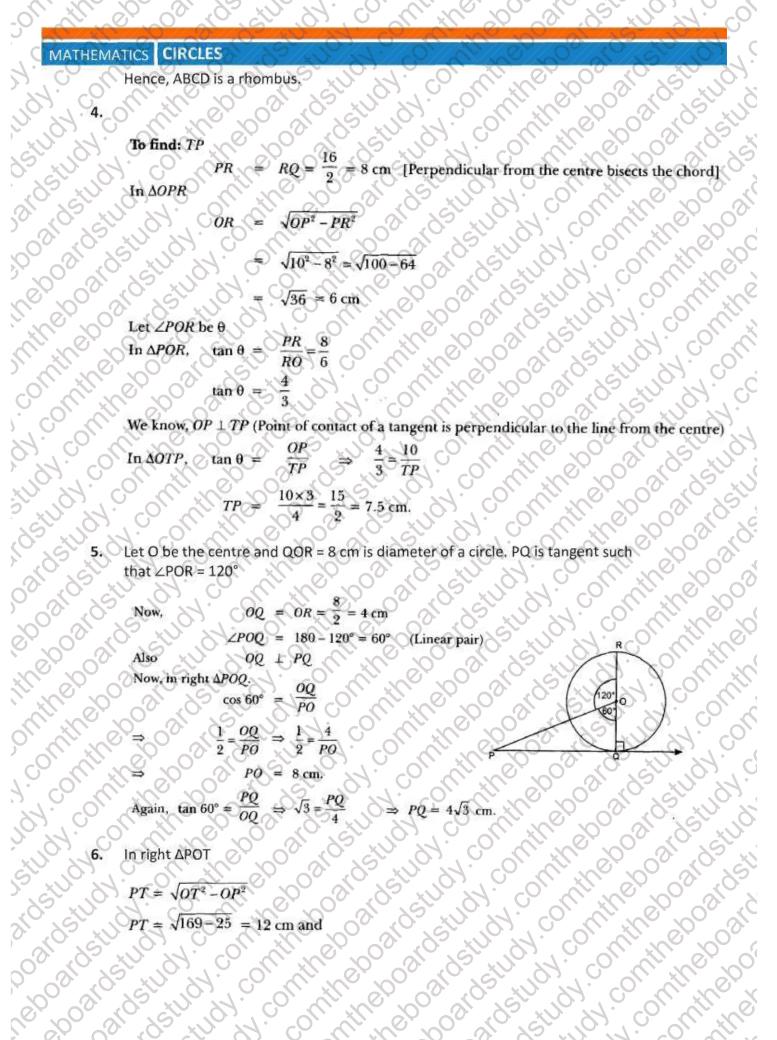
$$\cos 60^{\circ} = \sqrt{\frac{1}{2}} = \frac{OQ}{PO} \Rightarrow \sqrt{\frac{1}{2}} = \sqrt{\frac{1}} = \sqrt{\frac{1}{2}} = \sqrt{\frac{1}{2}} =$$

$$\frac{1}{2} \Rightarrow \frac{4}{2} \Rightarrow \frac{4}{PQ}$$

$$\Rightarrow \sqrt{3} = \frac{PQ}{4} \Rightarrow PQ = 4\sqrt{3} \text{ cm.}$$
12 cm and

$$PT = \sqrt{OT^2 - OP^2}$$

$$PT = \sqrt{169 - 25} = 12 \text{ cm and}$$



$$TE = 8 cm$$

Let
$$PA = AE = x$$

... external point to a circle are equal) $\begin{array}{c}
-TE^2 + EA^2 \\
\Rightarrow (12 - x)^2 = 64 + x^2 \\
\Rightarrow 144 + x^2 - 24x = 64 + x^2 \\
\Rightarrow x = \frac{80}{24} \\
\Rightarrow x = 3.3 \text{ cm} \\
\text{Thus, AB} = 6.6 \text{ cm}$ Case Study Answer:

1. Answer:

1. (b) 909

Solution: Answer:

(a) 99%

Solution: onthe boards tudy continue boa Acontral and state the property of the poor of the property of Jeth Contrato and state and some sta Setudy control of the load statuty control of the load sta

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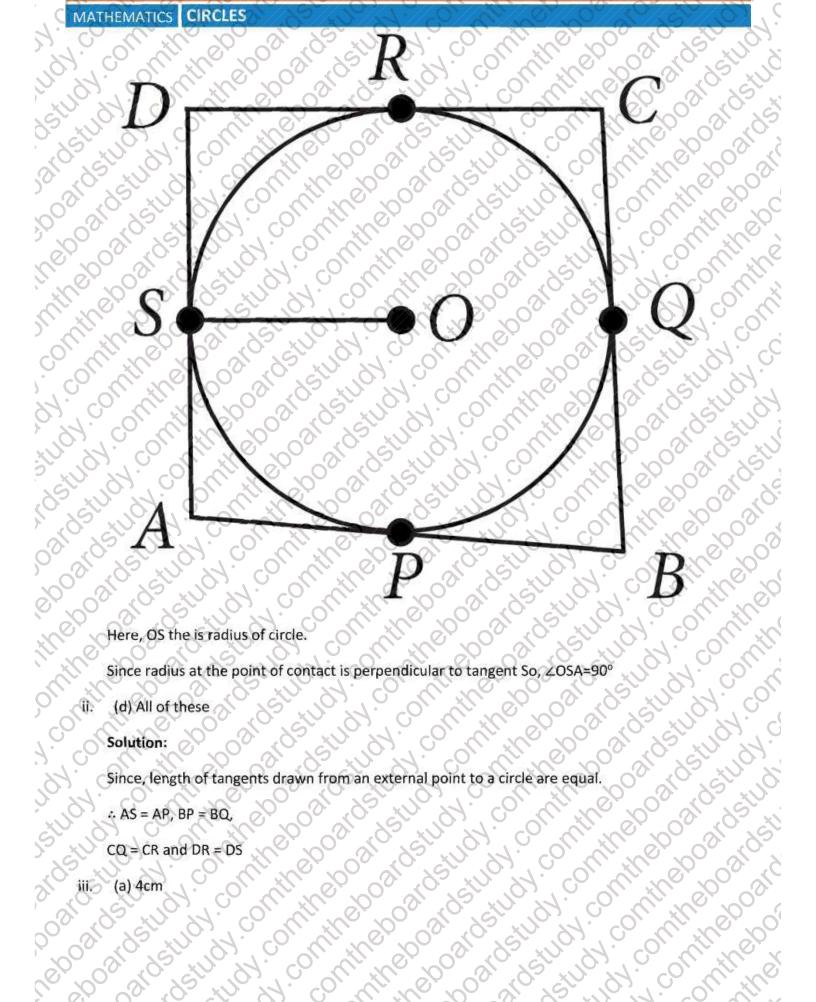
$$TA^2 = TE^2 + EA^2$$

$$\Rightarrow (12 - x)^2 = 64 + x^2$$

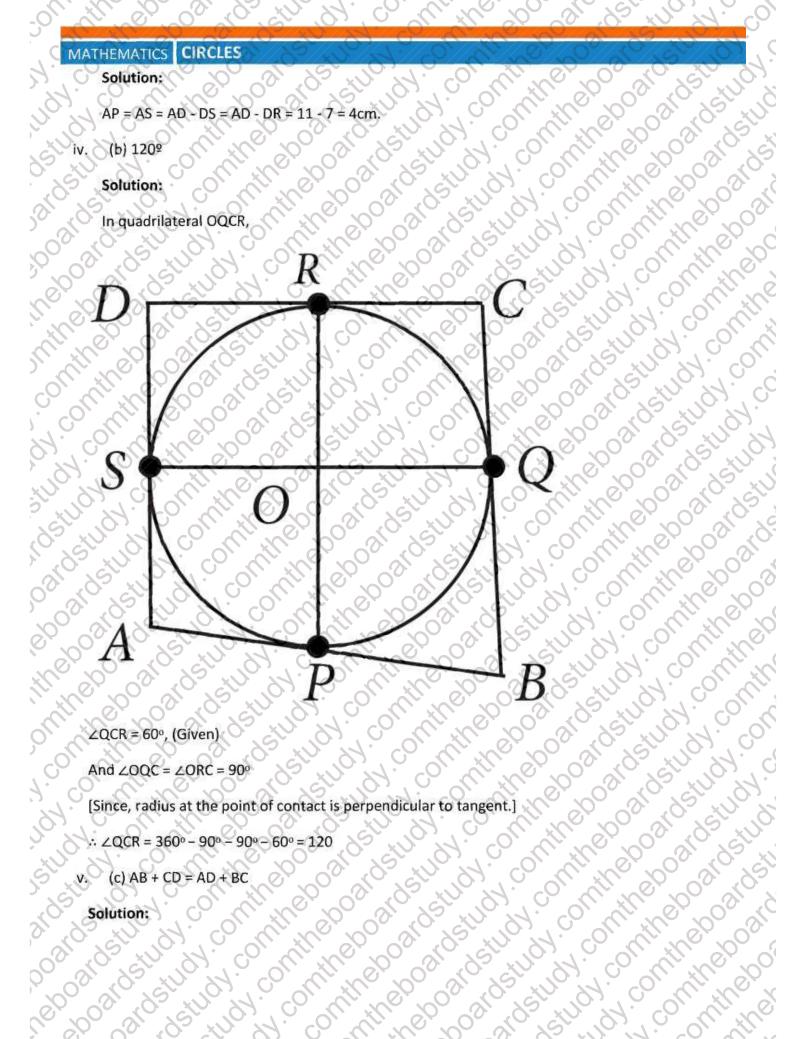
$$\Rightarrow$$
 144 + x^2 - 24x = 64 + x^3

$$\Rightarrow \chi = \frac{80}{24}$$

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$$AP = AS = AD - DS = AD - DR = 11 - 7 = 4cm$$



Ven,

And
$$\angle OQC = \angle ORC = 90^{\circ}$$

$$AS + DS + BQ + CQ = AP + DR + BP + CR$$

$$\Rightarrow$$
 AD + BC = AB + CD