

12th Physics

Chapter:- 1st

Electric charge and Field

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Electric charge:- It is intrinsic property of any material which shows that material is electrify or not.

→ Q/q

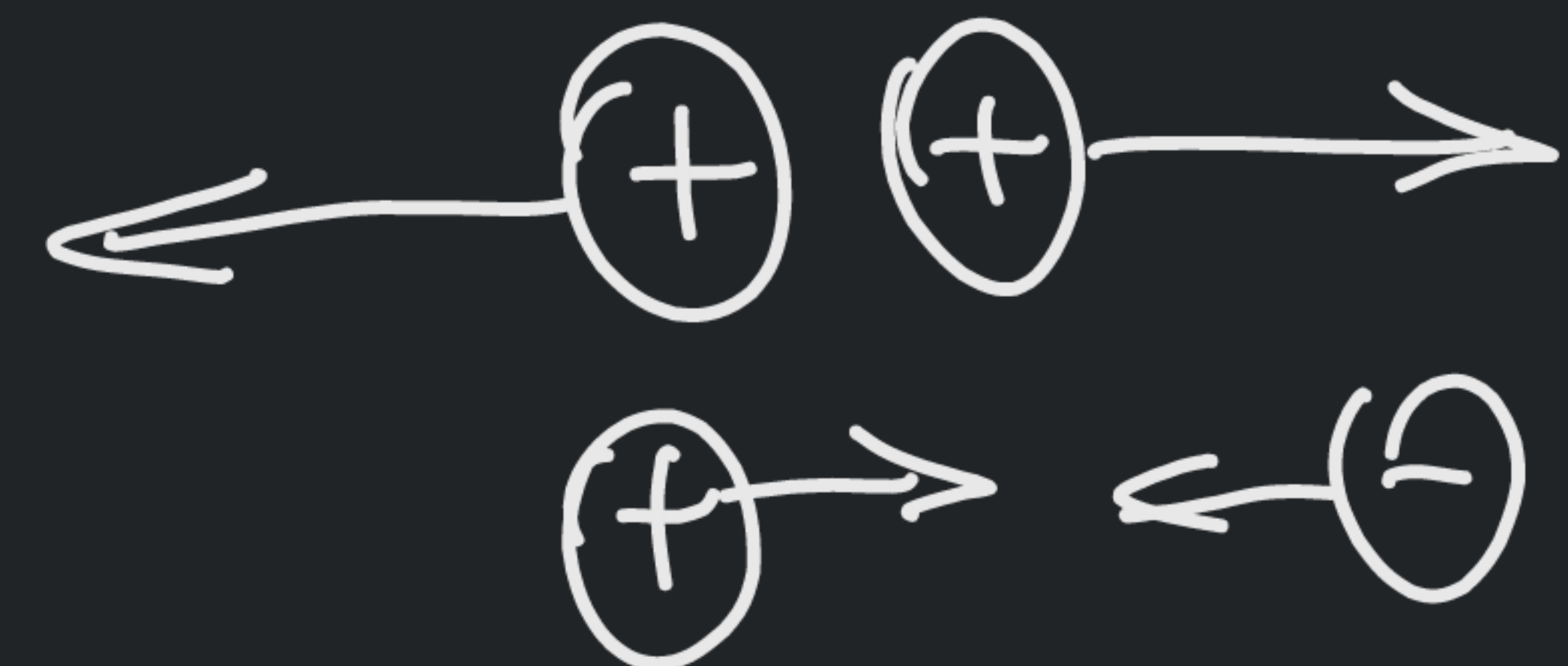
→ Unit:- Coulomb

→ Dimensional formula:- [AT]

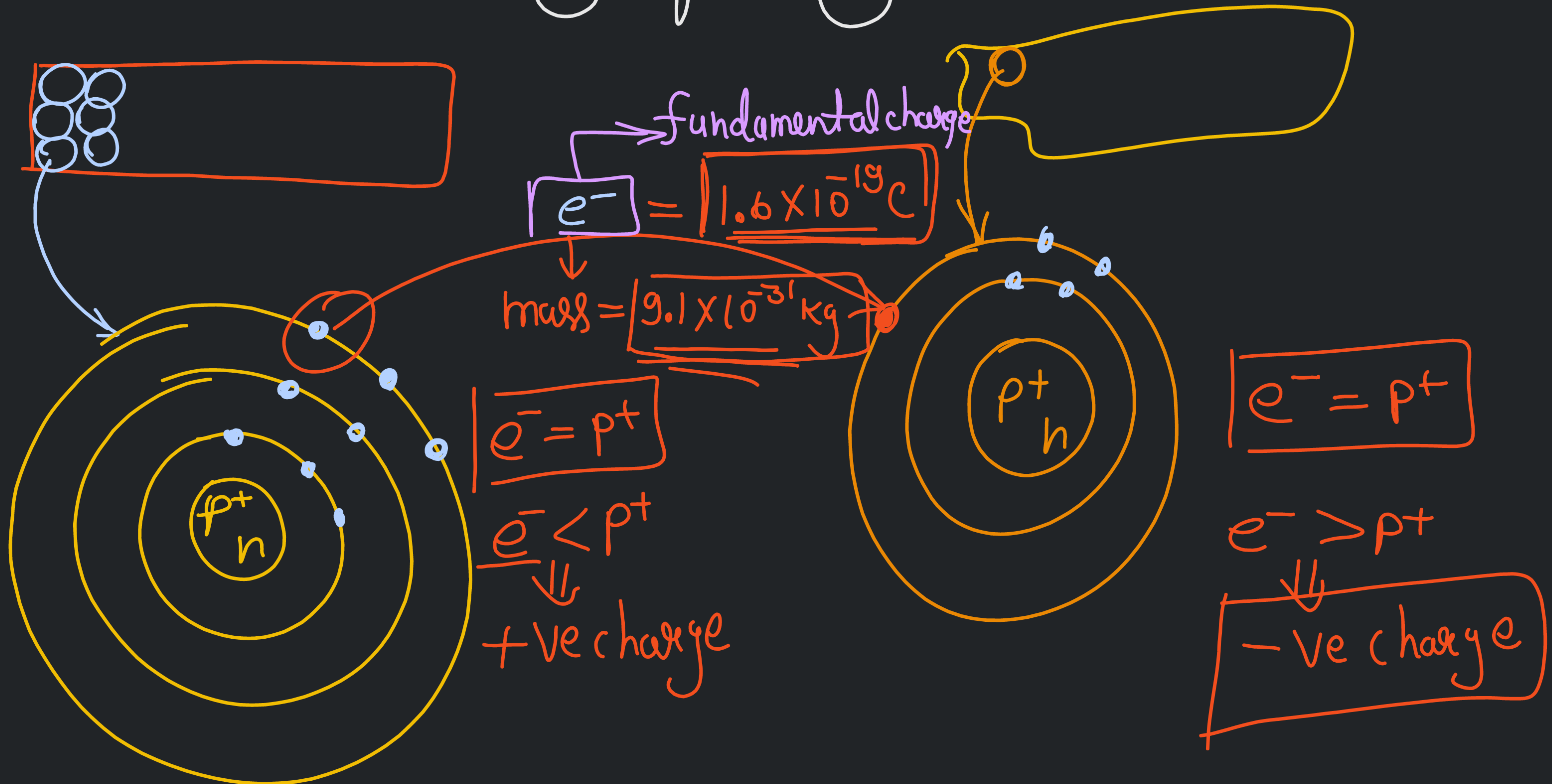
→ It is a scalar quantity.

(i) +ve charge

(ii) -ve charge

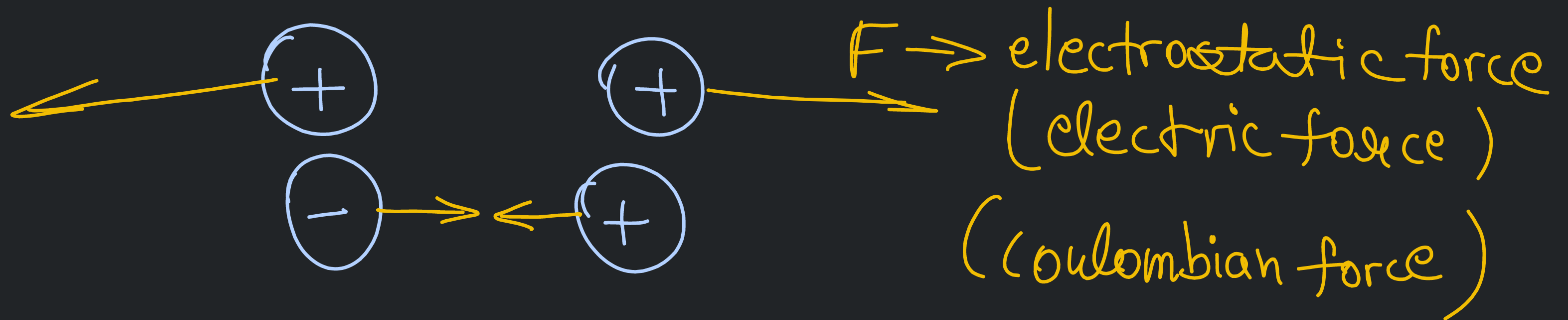


Electrical theory of charge :-



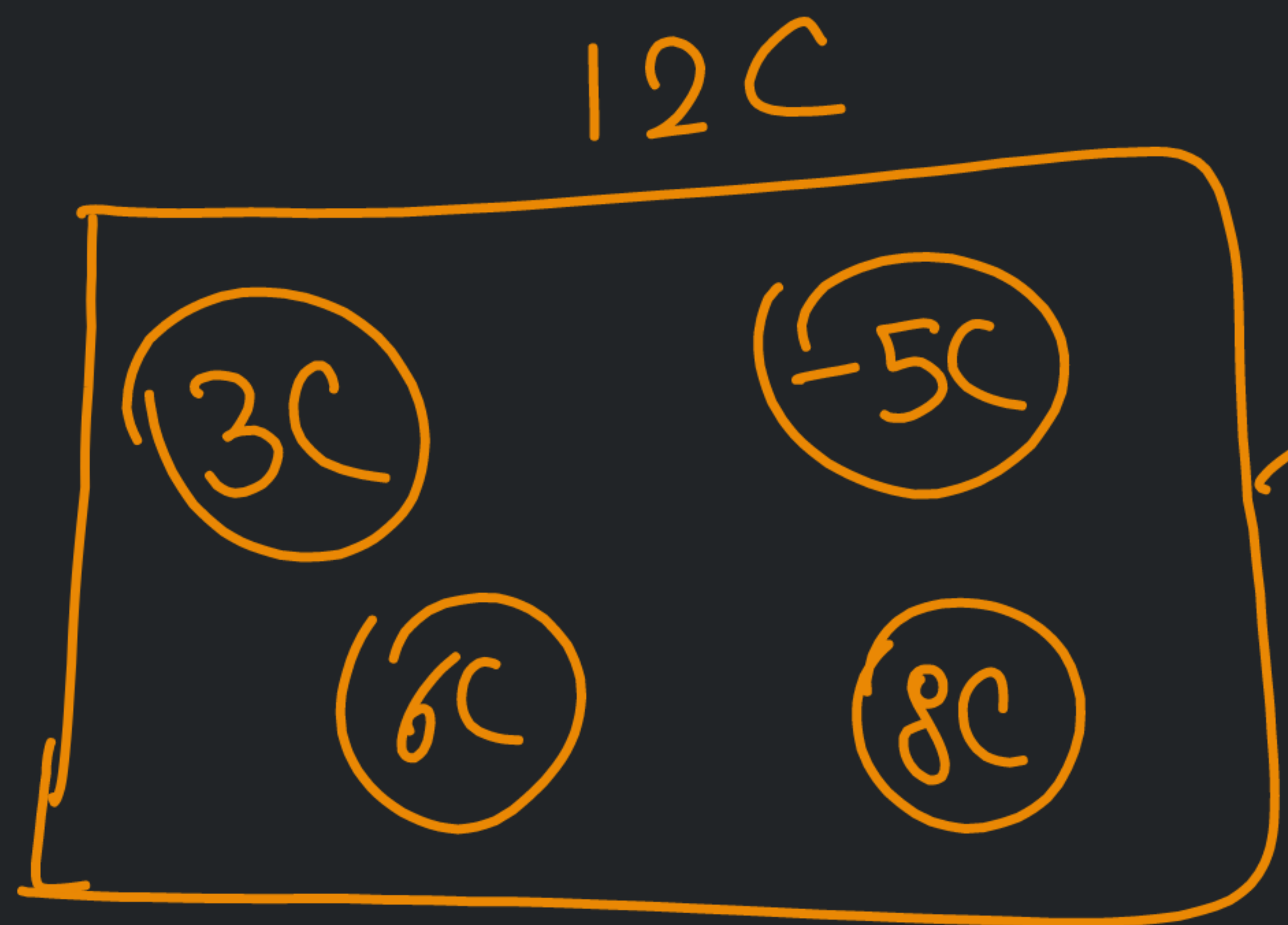
Properties of charge :-

- (i) Like charges repel each other and unlike charges attract each other



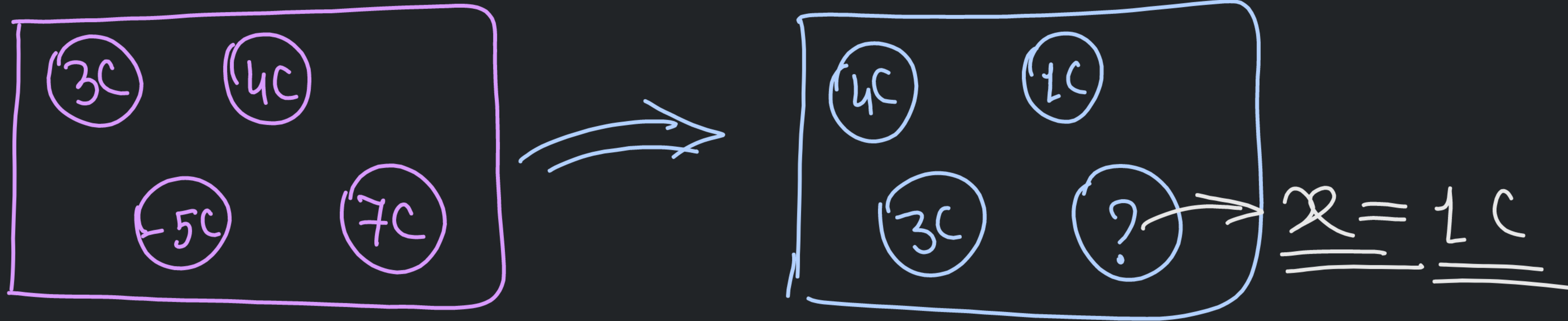
- ② Charge can be flow from one body to another body.
- ③ charges can be add by simple algebra.

Ex:-



$$\Rightarrow Q_{\text{net}} = \underline{3} - 5 + \underline{6} + \underline{8}$$
$$= \underline{\underline{12C}}$$

(iv) Conservation of charge:- net charge on an isolated system is always conserved. (fix)



$$3 + \cancel{4} - 5 + 7 = \cancel{4} + 1 + 3 + x$$

$$5 = 4 + x$$

$$x = 5 - 4 = \underline{1C}$$

⑤ Quantisation of charge :- Net amount of charge on a body is integral multiple of charge on one electron.

Ex :-

$1e, 2e, 3e, \dots ne$ ✓✓

$1.5e, \frac{3}{7}e, \pi e, \dots$ ✗

$Q = \pm ne$		Charge on one e^- $= 1.6 \times 10^{-19} \text{ C}$
Amount of Charge	no. of e^-	

Q. How many electrons in one coulomb charge :-

Solve :-

$$Q = 1 \text{ Coulomb}$$

$$n = ?$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

then

$$Q = ne$$

$$1 = n \times 1.6 \times 10^{-19} \text{ C}$$

$$n = \frac{10}{1.6 \times 10^{-19}}$$

$$n = \frac{10^5}{1.6} \times 10^{19}$$

$$8 \overline{) 50}$$

$$n = \frac{50}{1.6} \times 10^{18}$$

$$n = 6.25 \times 10^{18}$$

Imp obj

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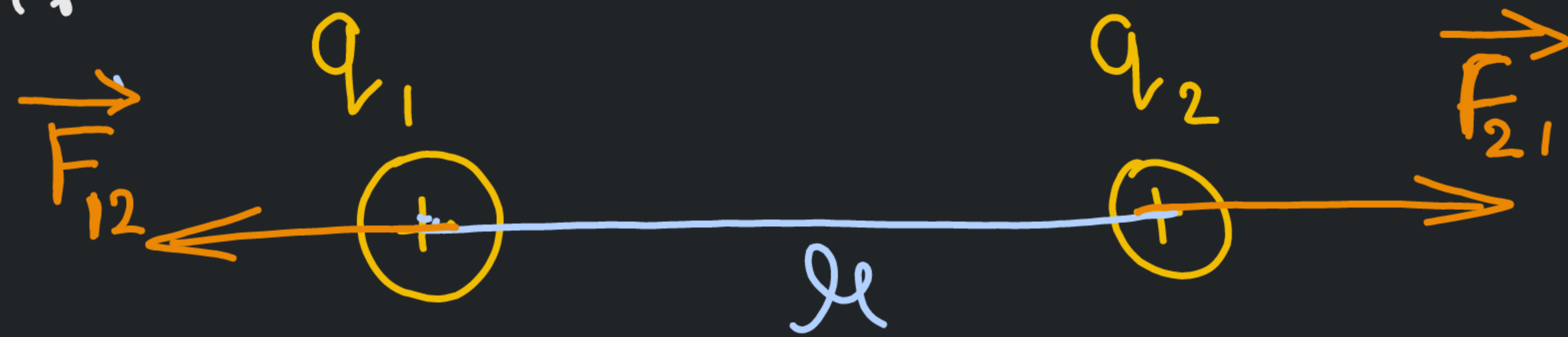


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Coulomb's law:- According to this law "attraction or repulsion for b/w two point charges is directly proportional product of their magnitude and inversely proportional to square of distance b/w them.



$$|\vec{F}_{12}| = |\vec{F}_{21}| = \underline{\underline{F}}$$

$$\left. \begin{aligned} F &\propto q_1 \cdot q_2 \\ F &\propto \frac{1}{r^2} \end{aligned} \right\}$$

$$F \propto \frac{q_1 q_2}{r^2}$$

$$F = k \frac{q_1 q_2}{r^2}$$

$k \rightarrow$ constant

$$k = \frac{9 \times 10^9}{c^2} \text{ Nxm}^2$$

$$\therefore k = \frac{1}{4\pi\epsilon_0}$$

$\epsilon_0 \rightarrow$ permittivity of air/Vacuum

$$\epsilon_0 = 8.854 \times 10^{-12} \frac{c^2}{\text{Nxm}^2}$$

~~$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$~~

Vector form of Coulomb's law:-

$$F = k \frac{q_1 q_2}{r^2}$$

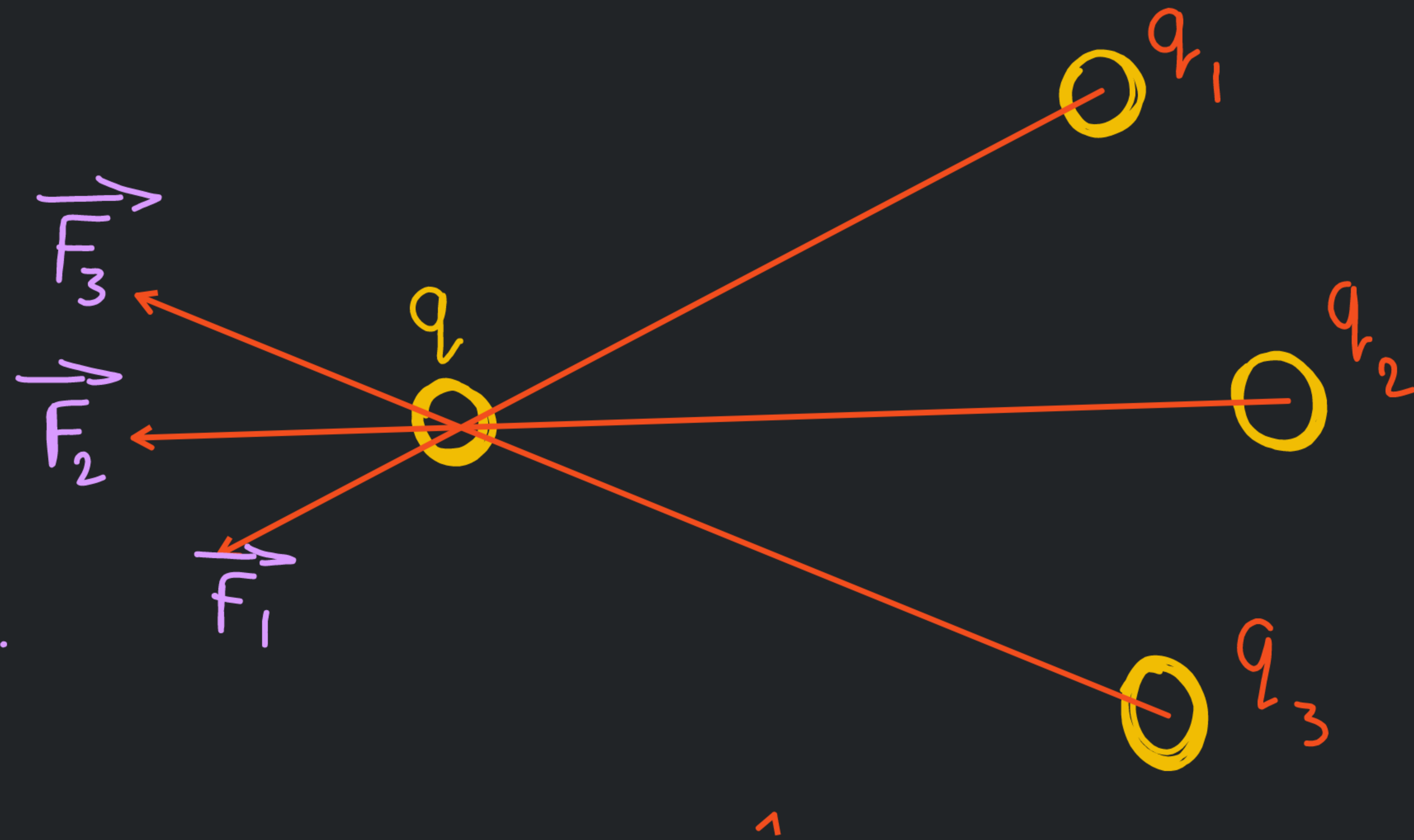
$$\vec{F} = k \frac{q_1 q_2}{|r|^2} \hat{r}$$

$$\therefore \hat{r} = \frac{\vec{r}}{|r|}$$

$$\vec{F} = k \frac{q_1 q_2}{|r|^2} \times \frac{\vec{r}}{|r|}$$

$$\vec{F} = k \frac{q_1 q_2}{|r|^3} \vec{r}$$

Principle of superposition:- net force on a charge by other charges is equal to vector sum of all individual forces.



$$\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3$$

Electrostatic force

(i) Attraction/Repulsion

(ii)
$$F = k \frac{q_1 q_2}{r^2}$$

$\downarrow$
medium

depends on
medium

(iii) It is stronger than gravitation

gravitational force

(i) attraction

(ii)
$$F = G \frac{m_1 m_2}{r^2}$$

$\downarrow$
Universal

not depends medium.

(iii) It is a weak force

$$F_e \approx 10^{42} F_g$$

Similarities:-

Electrostatic force

(i)

Inverse square law:

$$F \propto \frac{1}{r^2}$$

(ii)

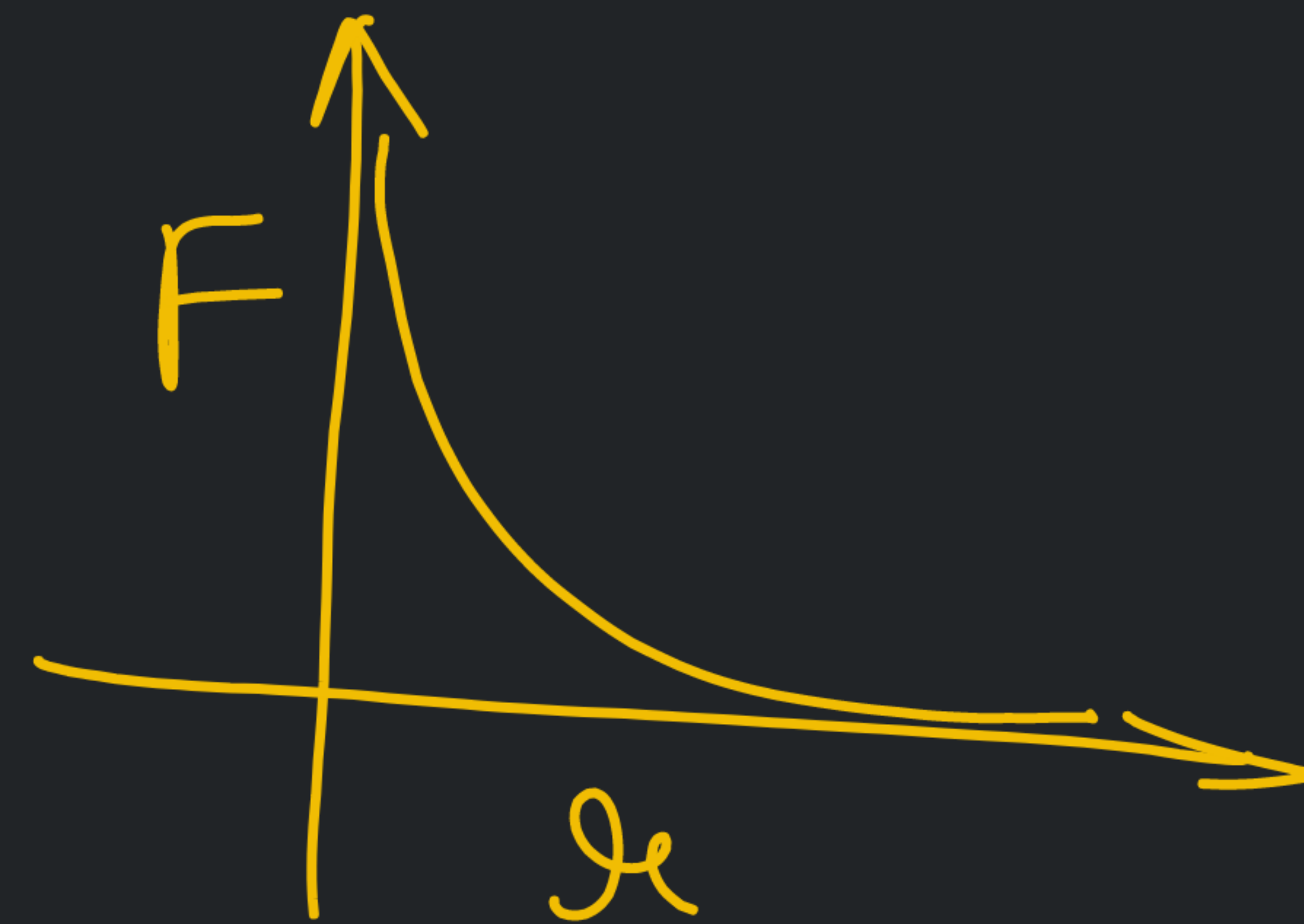
Central force



gravitational force

(i)

$$F \propto \frac{1}{r^2}$$

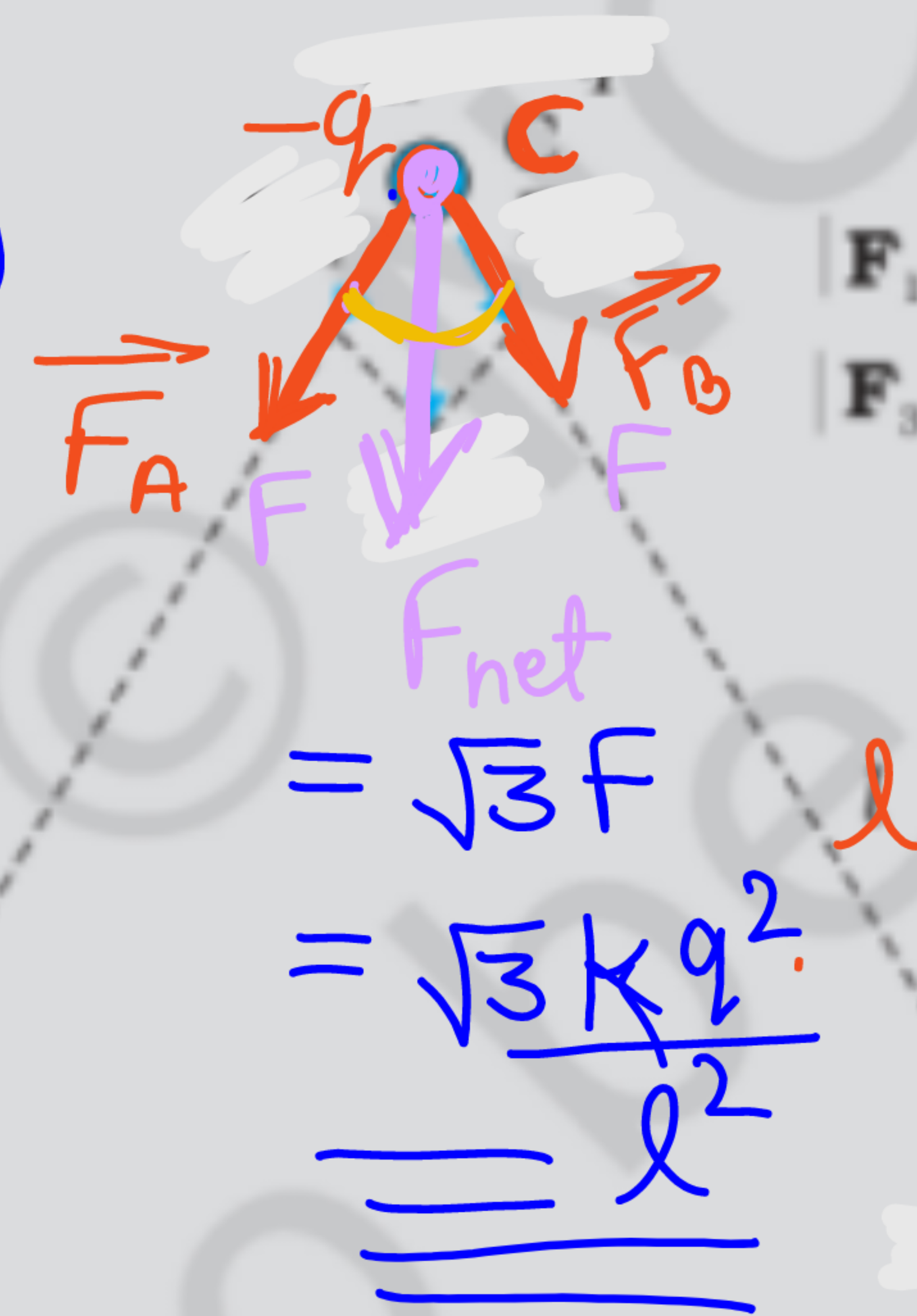
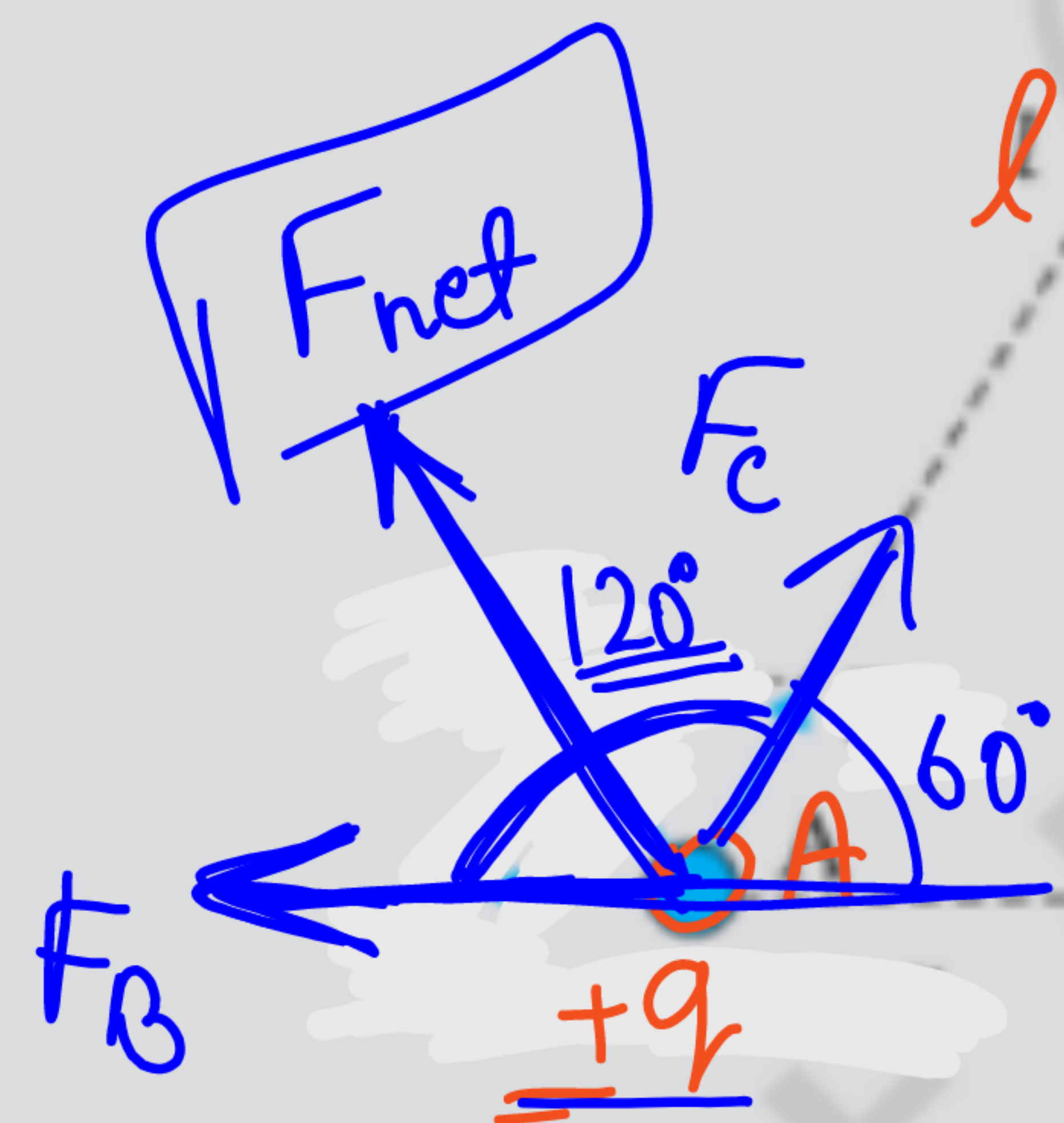


(ii)

central force

Example 1.6 Consider the charges q , q , and $-q$ placed at the vertices of an equilateral triangle, as shown in Fig. 1.7. What is the force on each charge?

$$\cos 120^\circ = -\frac{1}{2}$$



Force on C

$$F_A = k \frac{q \cdot q}{l^2}$$

$$F_A = \left(\frac{k q^2}{l^2} \right)$$

$$F_B = \left(\frac{k q^2}{l^2} \right) \rightarrow \underline{F}$$

$$R^2 = A^2 + B^2 + 2AB \cos \theta$$

$$F_{\text{net}}^2 = F^2 + F^2 + 2F \cdot F \cos 60^\circ$$

$$= 2F^2 + 2F^2 \times \frac{1}{2}$$

$$F_{\text{net}} = \sqrt{3F^2}$$

$$\boxed{F_{\text{net}} = \sqrt{3} F} \text{ Ans}$$

1.1 What is the force between two small charged spheres having charges of $2 \times 10^{-7} \text{ C}$ and $3 \times 10^{-7} \text{ C}$ placed 30 cm apart in air?

Solve :-

$$q_1 = 2 \times 10^{-7} \text{ C}$$

$$q_2 = 3 \times 10^{-7} \text{ C}$$

$$r = 30 \text{ cm} = 30 \times 10^{-2} \text{ m.}$$

then

$$F = k \frac{q_1 q_2}{r^2}$$

$$F = \frac{9 \times 10^9 \times 2 \times 10^{-7} \times 3 \times 10^{-7}}{30 \times 10^{-2} \times 30 \times 10^{-2}} \times 10^{-5}$$

$$F = 6 \times 10^{-3} \text{ Newton}$$

1.2 The electrostatic force on a small sphere of charge $0.4 \mu\text{C}$ due to another small sphere of charge $-0.8 \mu\text{C}$ in air is 0.2 N . (a) What is the distance between the two spheres? (b) What is the force on the second sphere due to the first?

Solve: (a)

$$q_1 = 0.4 \times 10^{-6} \text{ C}$$

$$q_2 = 0.8 \times 10^{-6} \text{ C}$$

$$F = 0.2 \text{ N}$$

$$r = ?$$

$$F = k \frac{q_1 q_2}{r^2}$$

$$0.2 = \frac{9 \times 10^9 \times 0.4 \times 10^{-6} \times 0.8 \times 10^{-6}}{r^2 \times 10}$$

$$1 = \frac{9 \times 16 \times 10^{-4}}{r^2}$$

$$r^2 = 9 \times 16 \times 10^{-4}$$

$$r = \sqrt{9 \times 16 \times 10^{-4}}$$

$$r = 3 \times 4 \times 10^{-2}$$

$$r = 12 \times 10^{-2} \text{ m}$$

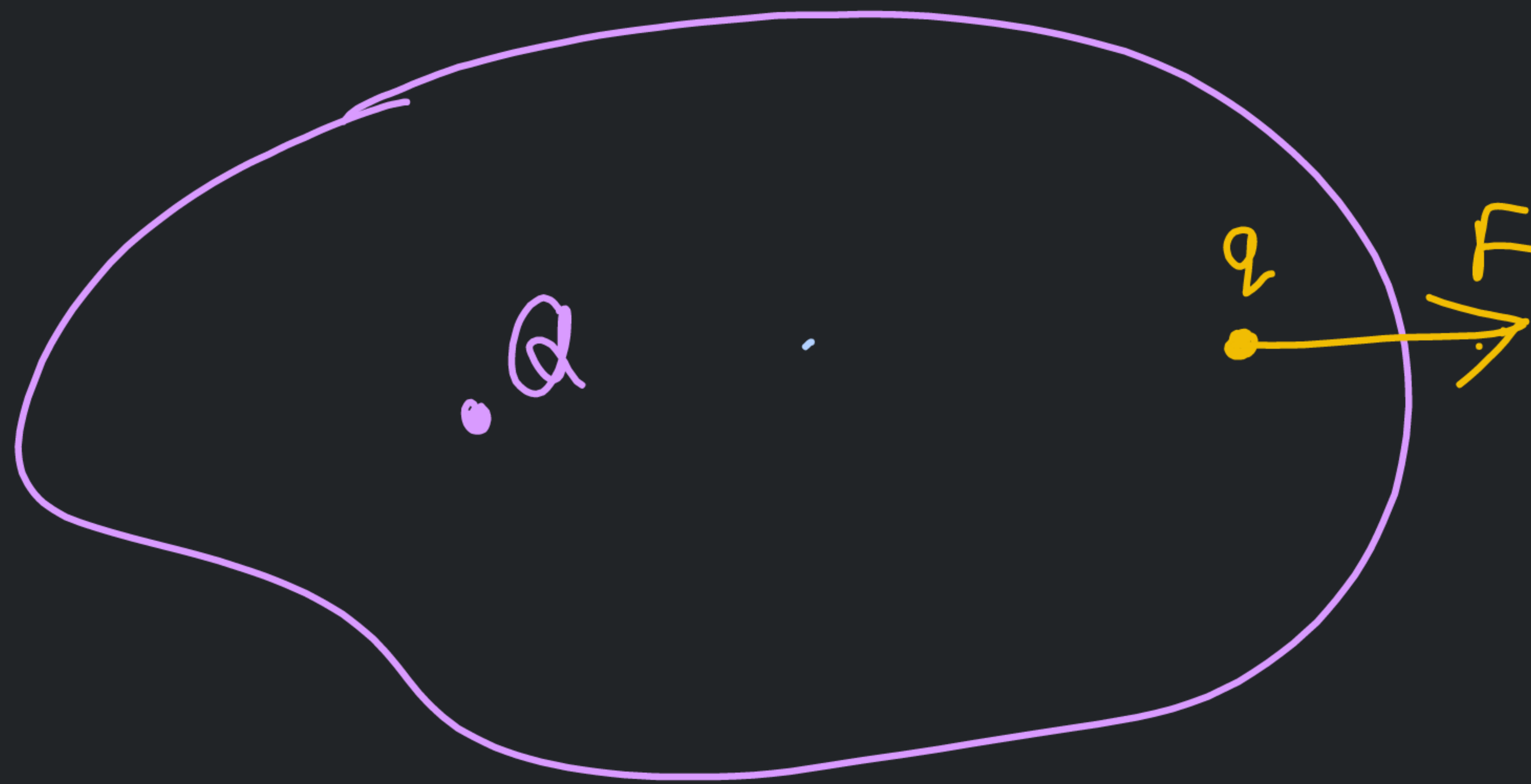
$$r = 12 \text{ cm}$$

$$q_1 = 0.4 \mu\text{C}$$

$$q_2 = -0.8 \mu\text{C}$$

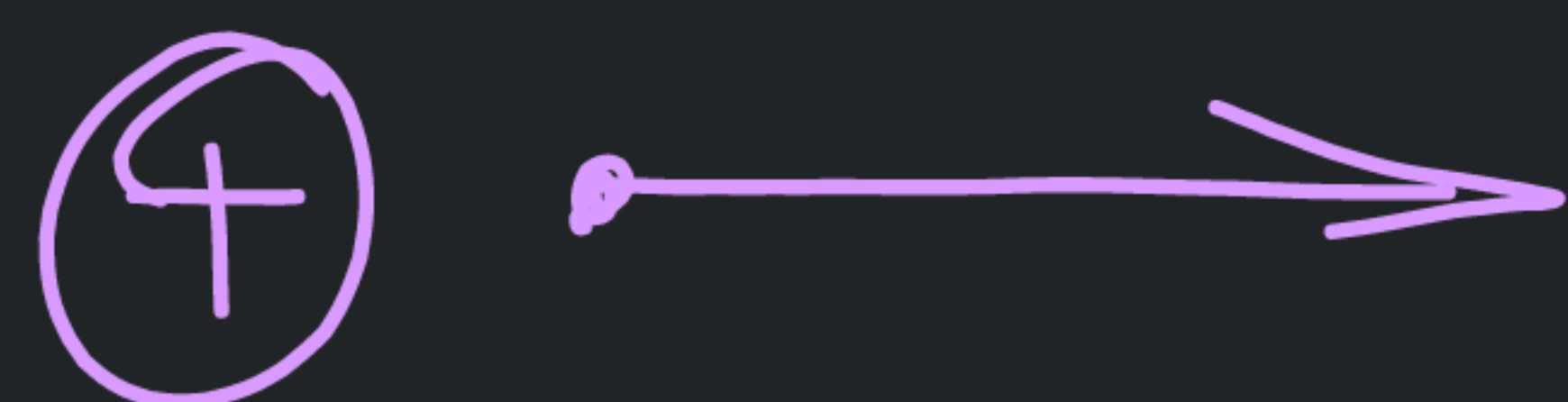


Concept of electric field:- Area around any point charge at which its influence can be experienced by other charges.



Intensity of electric field:- Force experienced by a unit +ve charge

inside a electric field is called intensity of electric field



$$E = \frac{F}{q_0}$$

Unit:- $\frac{\text{Newton}}{\text{Coulomb}}$ or $\frac{\text{Volt}}{\text{metre}}$

Dimensions:- $[MLT^{-3}A^{-1}] \Rightarrow 11-31$

It is a vector quantity $\left\{ \begin{array}{l} q_0 \rightarrow \text{Test charge} \\ \rightarrow +ve \\ \rightarrow \frac{F}{q_0} \end{array} \right.$

along the $\vec{F}$

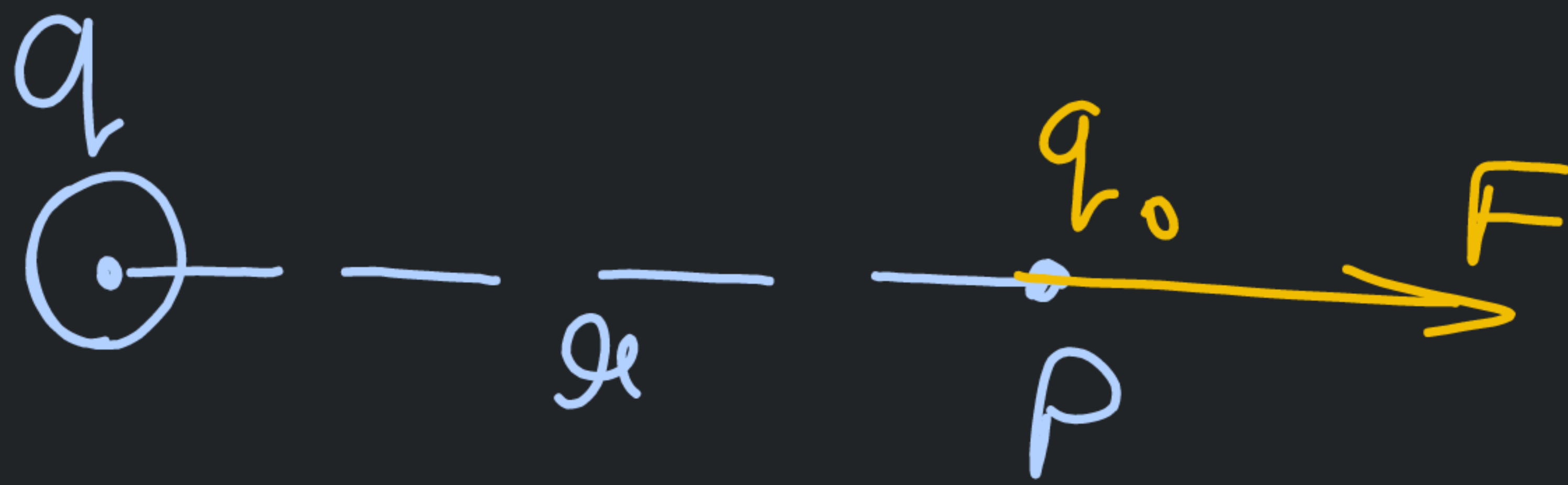
$\frac{F}{q_0}$

Force on a charge inside a field:—

$$E = \frac{F}{q_0}$$

$$\boxed{F = q_0 E} \rightarrow \underline{\underline{\text{objective}}}$$

Intensity of electric field due to point charge:-



$$F = \frac{1}{4\pi\epsilon_0} \frac{q q_0}{r^2} \quad \text{--- ①}$$

but

$$E = \left(\frac{F}{q_0} \right)$$

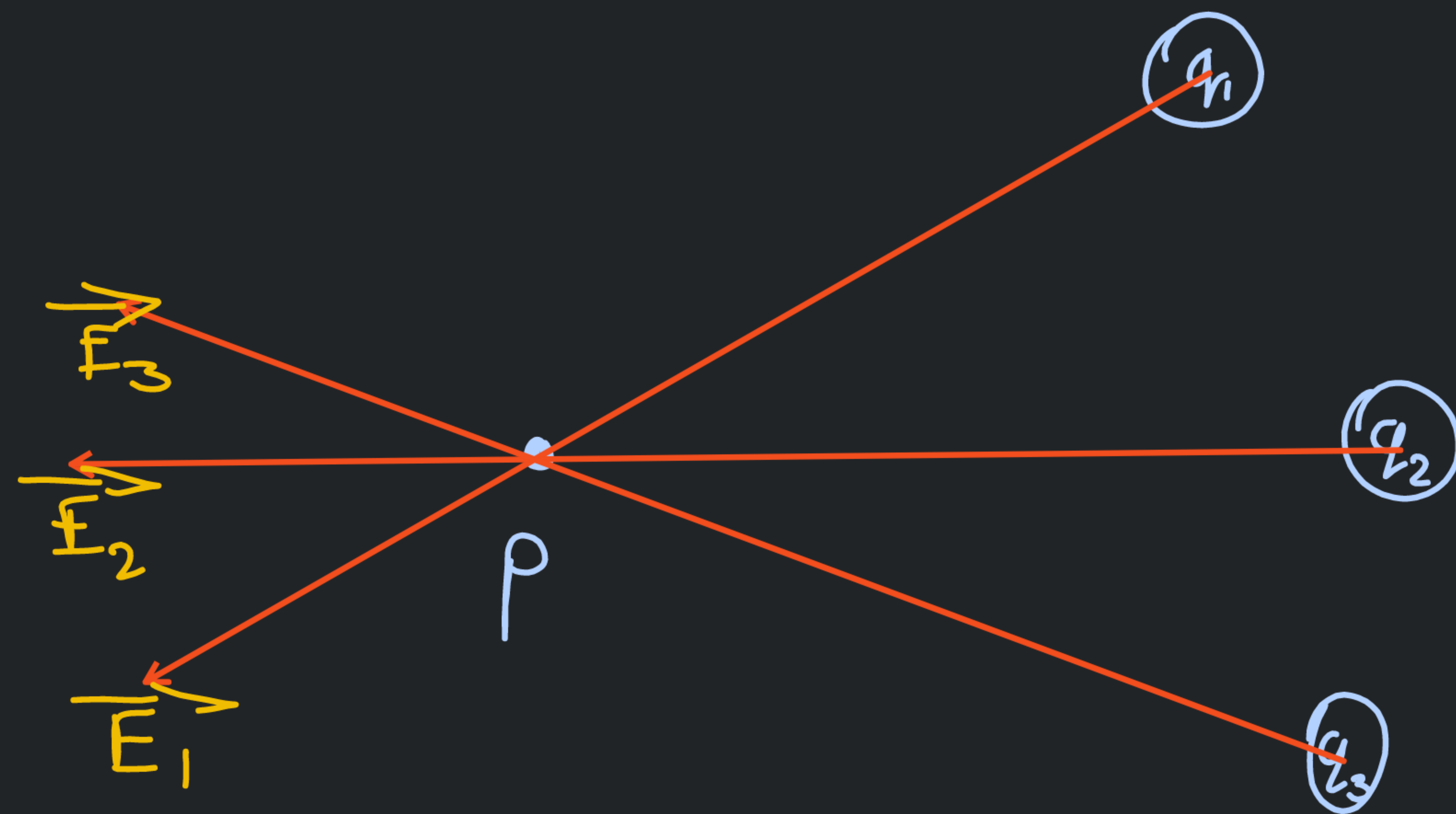
then by eqⁿ ①

$$E = \frac{\frac{1}{4\pi\epsilon_0} \frac{q q_0}{r^2}}{q_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

N/C

Principle of superposition:-



$$\therefore E_{\text{net}} = ?$$

$$\vec{E}_{\text{net}} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3$$

Electric dipole :- It is a system of charge in which two charges of same magnitude but different nature is placed very close to each other.



Electric dipole moment :- It is the product of magnitude of one of the charge to the separation

$p = \text{one of the charge} \times \text{distance b/w the charges.}$

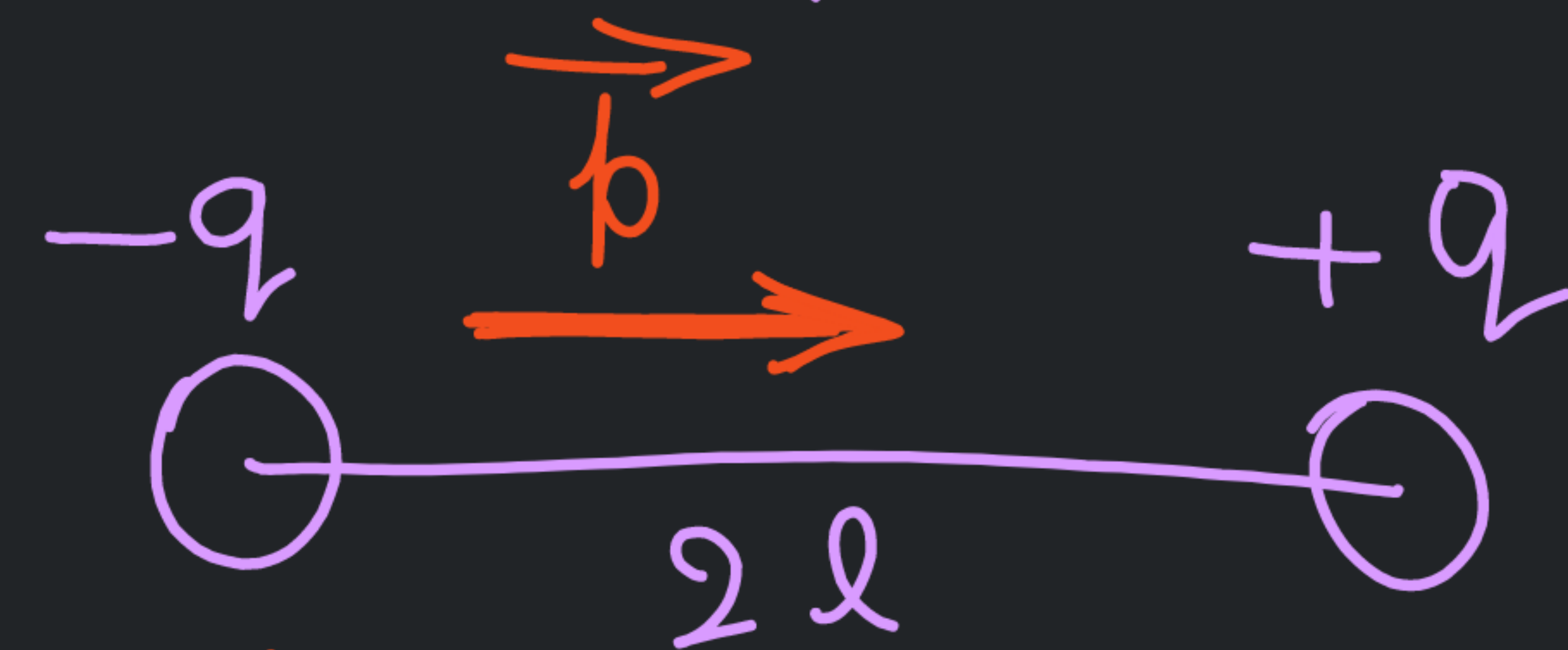
$$p = q \times 2l$$

Unit: Coulomb $\times$ metre

Dimensional formula:- $[LTA]$

It is a vector quantity.

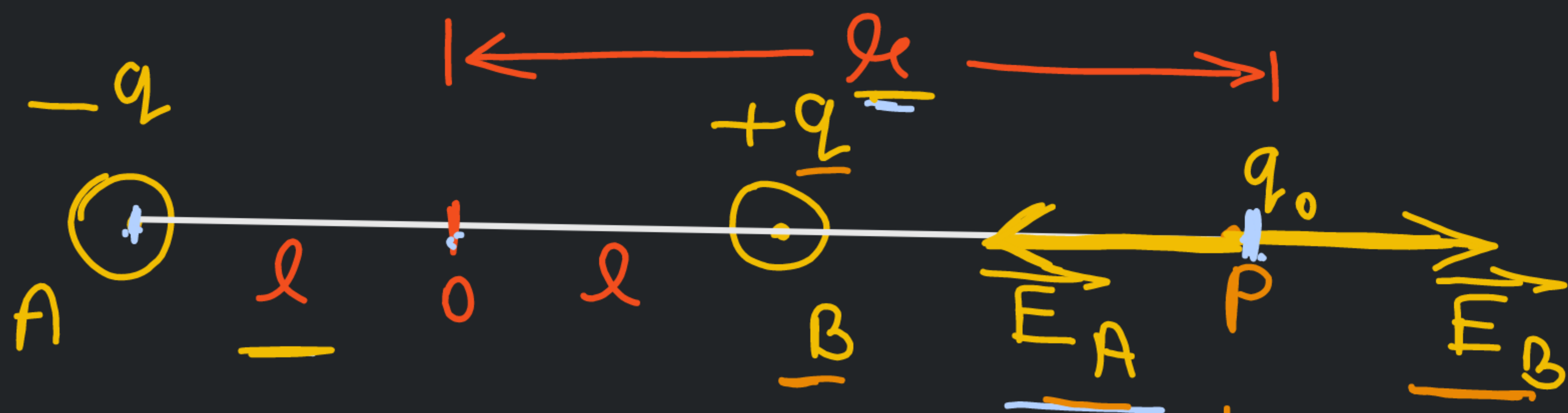
And its direction along to the



from $-ve$ charge to $+ve$ charge

Imp

Intensity of electric field due to dipole in axial position:-



Electric field due to $-q$ charge:-

$$E_A = \frac{1}{4\pi\epsilon_0} \frac{q}{AP^2}$$

$$E_A = \frac{1}{4\pi\epsilon_0} \frac{q}{(x+l)^2} \quad \text{--- (1)}$$

Electric field due to $+q$ charge

$$E_B = \frac{1}{4\pi\epsilon_0} \frac{q}{BP^2}$$

$$E_B = \frac{1}{4\pi\epsilon_0} \frac{q}{(x-l)^2} \quad \text{--- (2)}$$

then net field:-

$$E_{\text{net}} = E_B - E_A$$

Put the values from eqⁿ (1) and (2)

$$E_{\text{net}} = \frac{1}{4\pi\epsilon_0} \frac{q}{(x-l)^2} - \frac{1}{4\pi\epsilon_0} \frac{q}{(x+l)^2}$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{1}{(x-l)^2} - \frac{1}{(x+l)^2} \right]$$

$$E_{\text{net}} = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{(x-l)^2} - \frac{1}{(x+l)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{(x+l)^2 - (x-l)^2}{(x-l)^2 (x+l)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{x^2 + l^2 + 2xl - (x^2 + l^2 - 2xl)}{(x^2 - l^2)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{\cancel{x^2} + \cancel{l^2} + 2xl - \cancel{x^2} - \cancel{l^2} + 2xl}{(x^2 - l^2)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \times \frac{4xl}{(x^2 - l^2)^2}$$

$$= \frac{(q \times 2l) \times 2x}{4\pi\epsilon_0 (x^2 - l^2)^2}$$

$$[\because p = q \times 2l]$$

$$E_{\text{net}} = \frac{1}{4\pi\epsilon_0} \frac{2xp}{(x^2 - l^2)^2}$$

Special case :-

If $l \ll x$ then
neglect the value of
 l

$$E_{\text{net}} = \frac{1}{4\pi\epsilon_0} \frac{2xp}{(x^2)^2}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{2xp}{x^4}$$

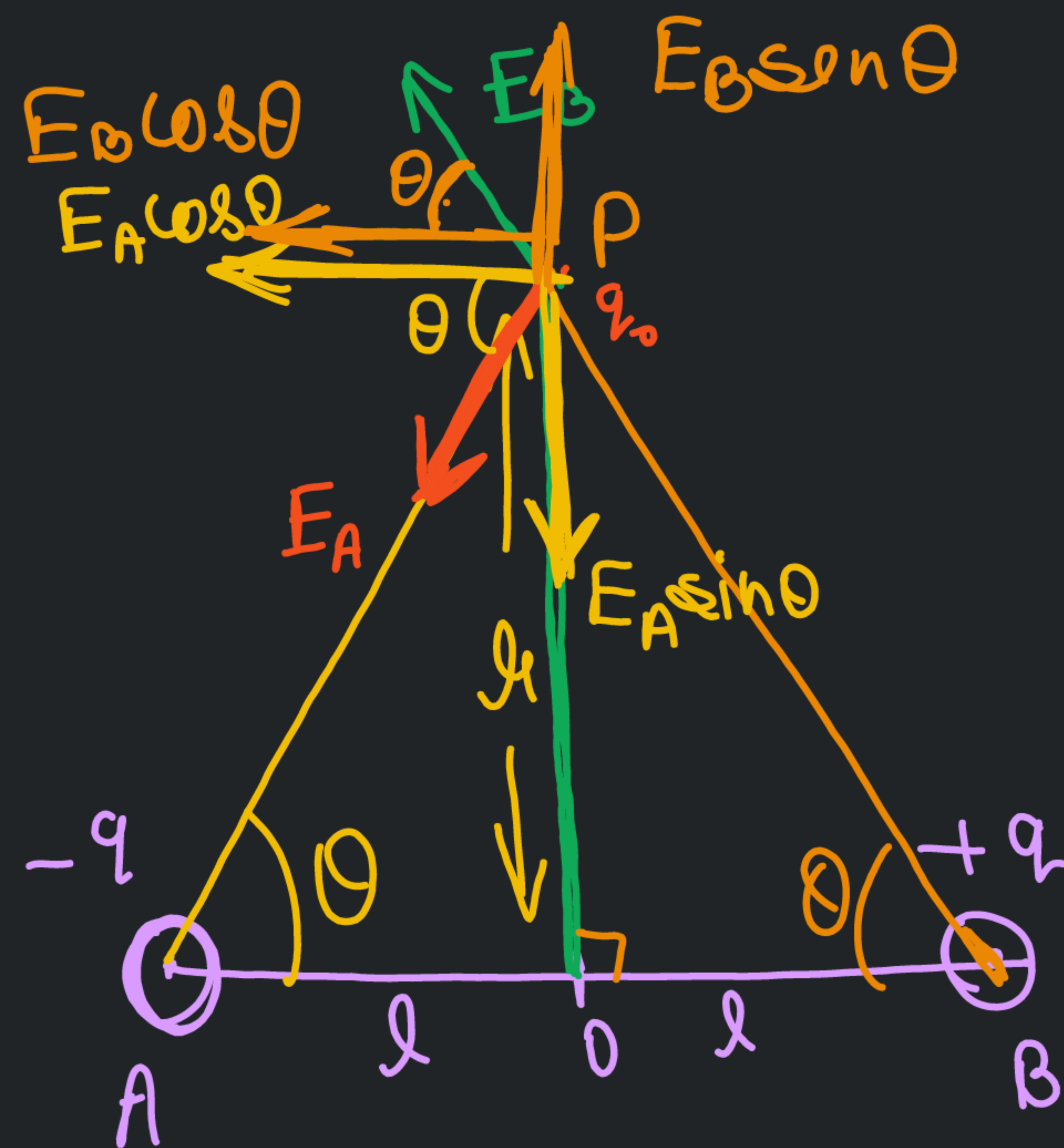
$$E_{\text{net}} = \frac{1}{4\pi\epsilon_0} \frac{2p}{x^3}$$

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Intensity of electric field due to dipole in equatorial position (co-axial) :-



Electric field due to $-q$ charge

$$E_A = \frac{1}{4\pi\epsilon_0} \frac{q}{AP^2}$$

In $\triangle AOP$ by Pythagoras

$$AP^2 = l^2 + r^2$$

$$AP = \sqrt{l^2 + r^2}$$

$$E_A = \frac{1}{4\pi\epsilon_0} \frac{q}{(l^2 + r^2)} \quad \text{--- (1)}$$

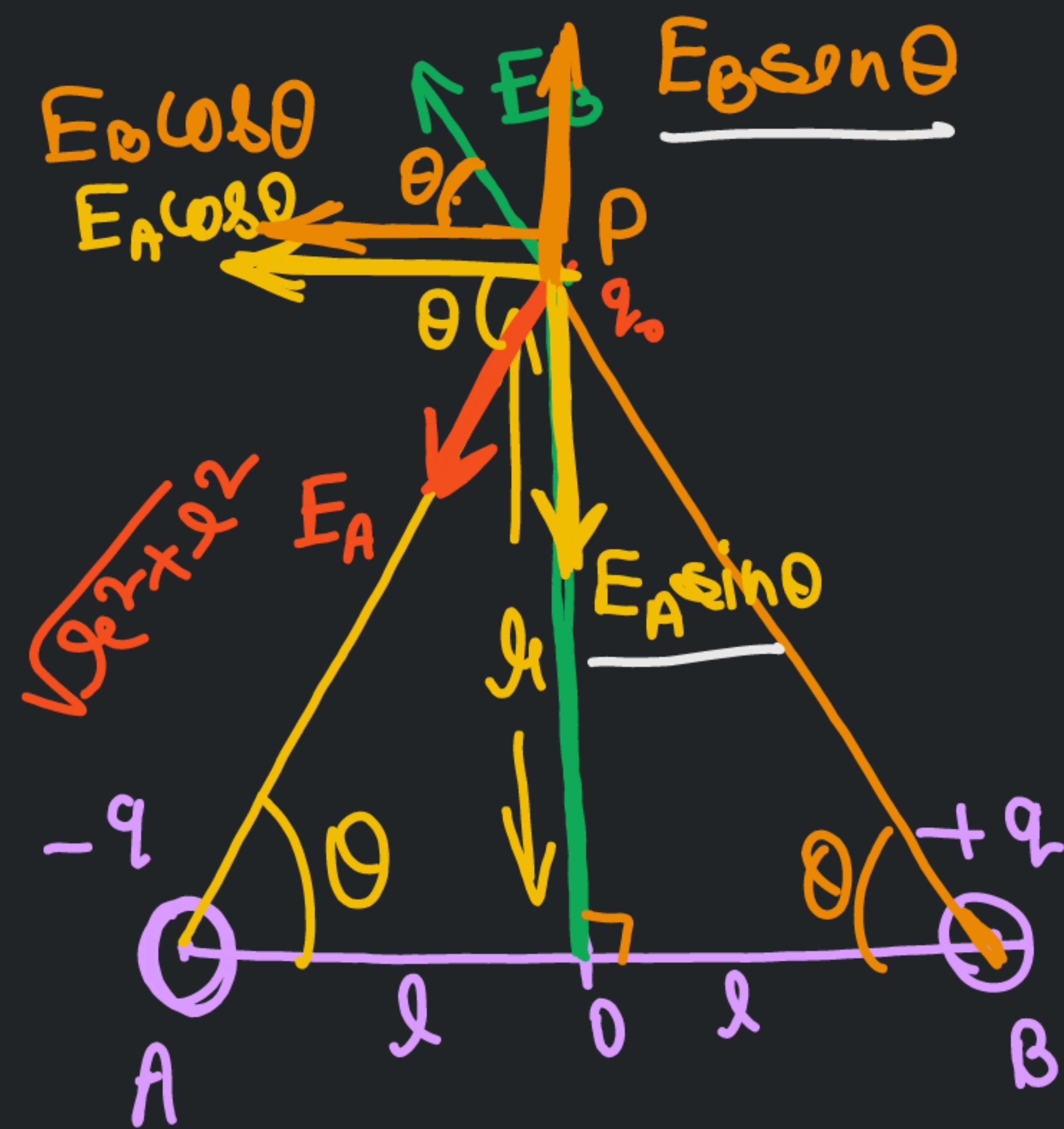
Electric field due to $+q$ charge :-

$$E_B = \frac{1}{4\pi\epsilon_0} \frac{q}{BP^2}$$

$$\because AP^2 = BP^2 = l^2 + r^2$$

$$E_B = \frac{1}{4\pi\epsilon_0} \frac{q}{(l^2 + r^2)} \quad \text{--- (2)}$$

$$\underline{E_B = E_A = E}$$



$$E_{net} = E_A \cos \theta + E_B \cos \theta + E_A \cos \theta - E_B \sin \theta$$

$$= \underline{E \cos \theta} + \underline{E \cos \theta} + \underline{E \cos \theta} - \underline{E \sin \theta}$$

$$E_{net} = \underline{2E \cos \theta} \quad \text{--- (3)}$$

$$\left[\begin{array}{l} \because \text{In } \triangle AOP \\ \cos \theta = \frac{l}{\sqrt{x^2 + l^2}} \end{array} \right]$$

by eqⁿ (3) :-

$$E_{net} = 2 \times \frac{1}{4\pi\epsilon_0} \frac{q}{\underline{x^2 + l^2}} \times \underline{\frac{l}{\sqrt{x^2 + l^2}}}$$

$$E_{net} = \frac{1}{4\pi\epsilon_0} \frac{q \times 2l}{(x^2 + l^2)^{3/2}}$$

$$\left[\because p = q \times 2l \right]$$

$$E_{net} = \frac{1}{4\pi\epsilon_0} \frac{p}{(x^2 + l^2)^{3/2}}$$

Special case :-
If $l \ll x$ then
neglect the value of l

$$E_{net} = \frac{1}{4\pi\epsilon_0} \frac{p}{(x^2)^{3/2}}$$

$$E_{net} = \frac{1}{4\pi\epsilon_0} \frac{p}{x^3}$$

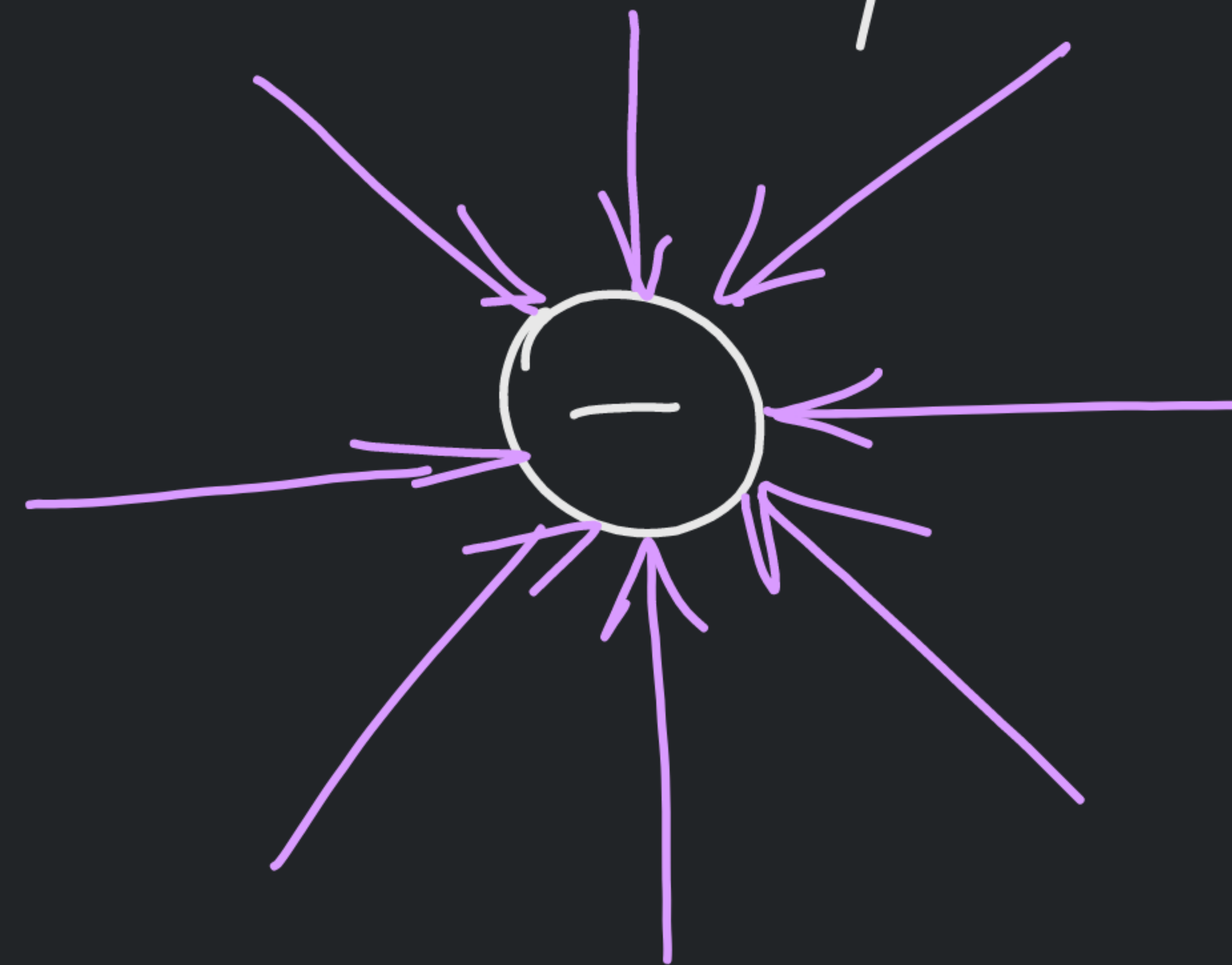
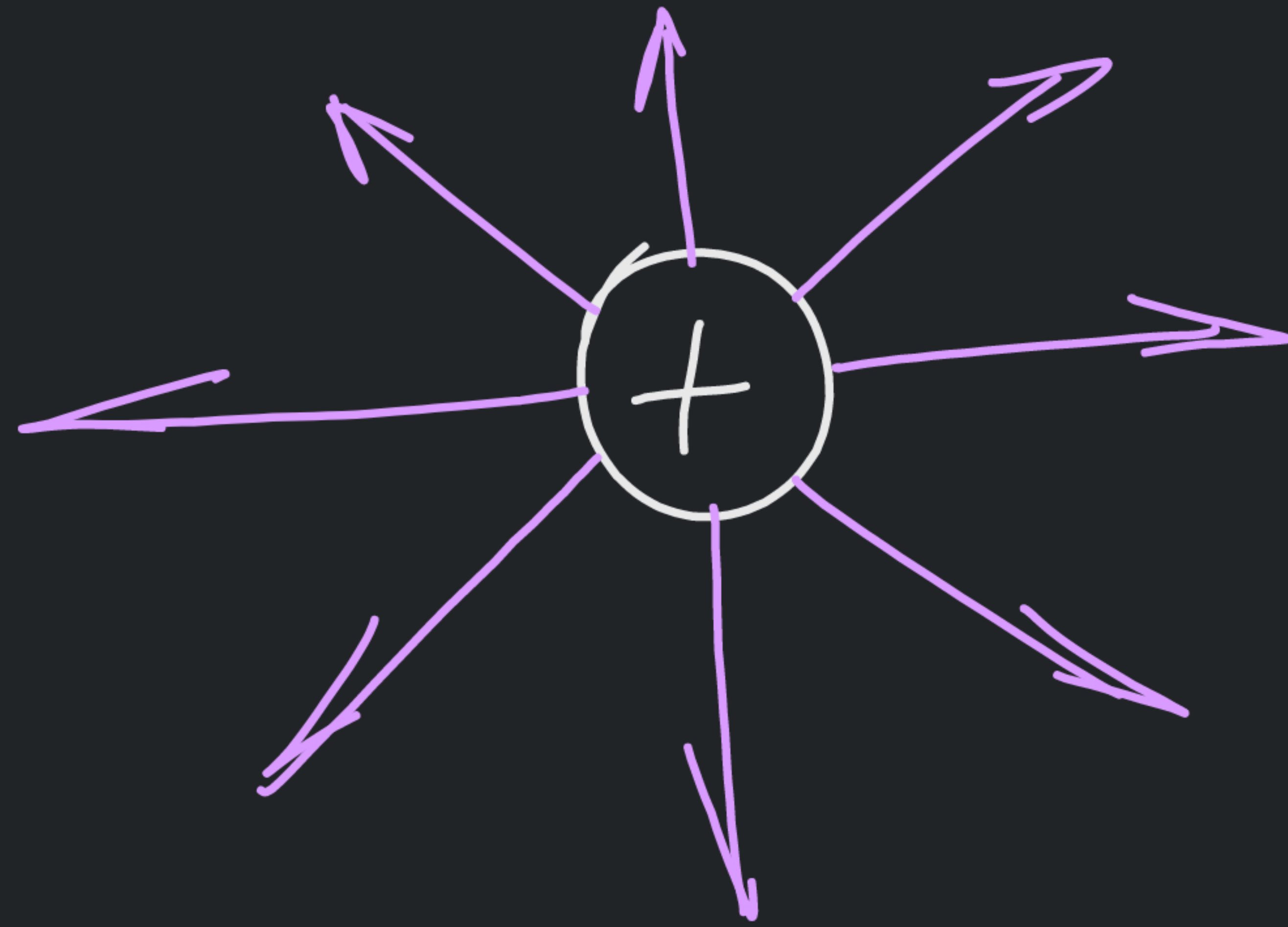
N/C

Electric Field lines: They are the imaginary
(Electric Line of force) curved lines form in
a electric field at which
a unit positive charge can be
travel.



Properties of field lines:-

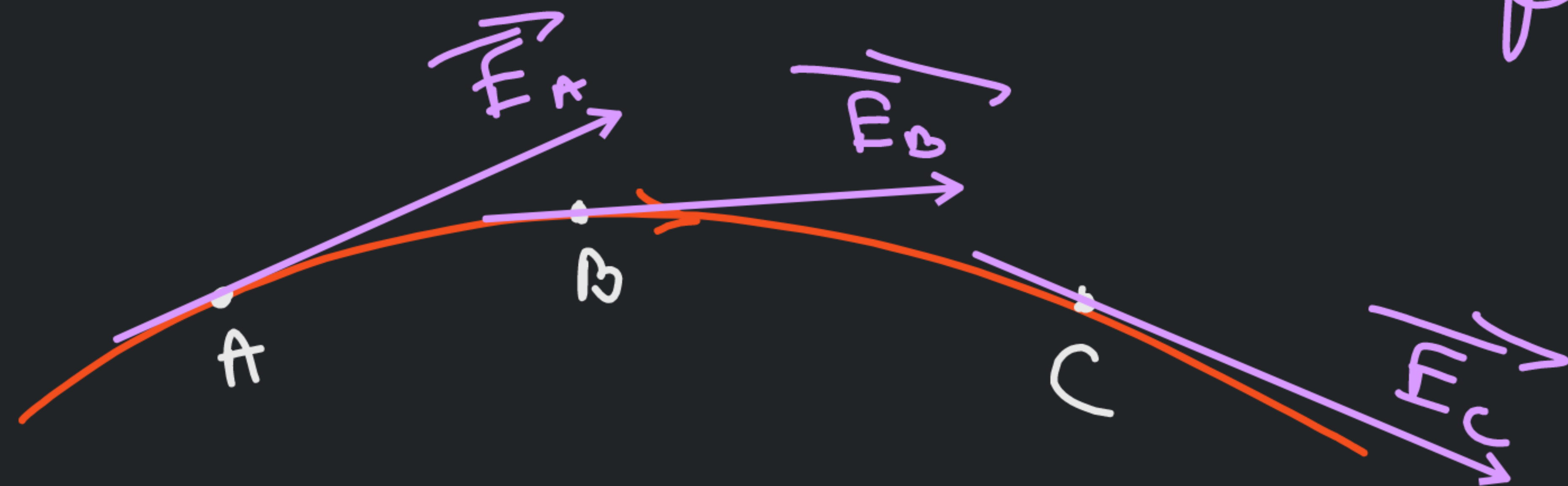
(i) They are generated from +ve charge and terminated at -ve charge.



② They do not form closed curve.

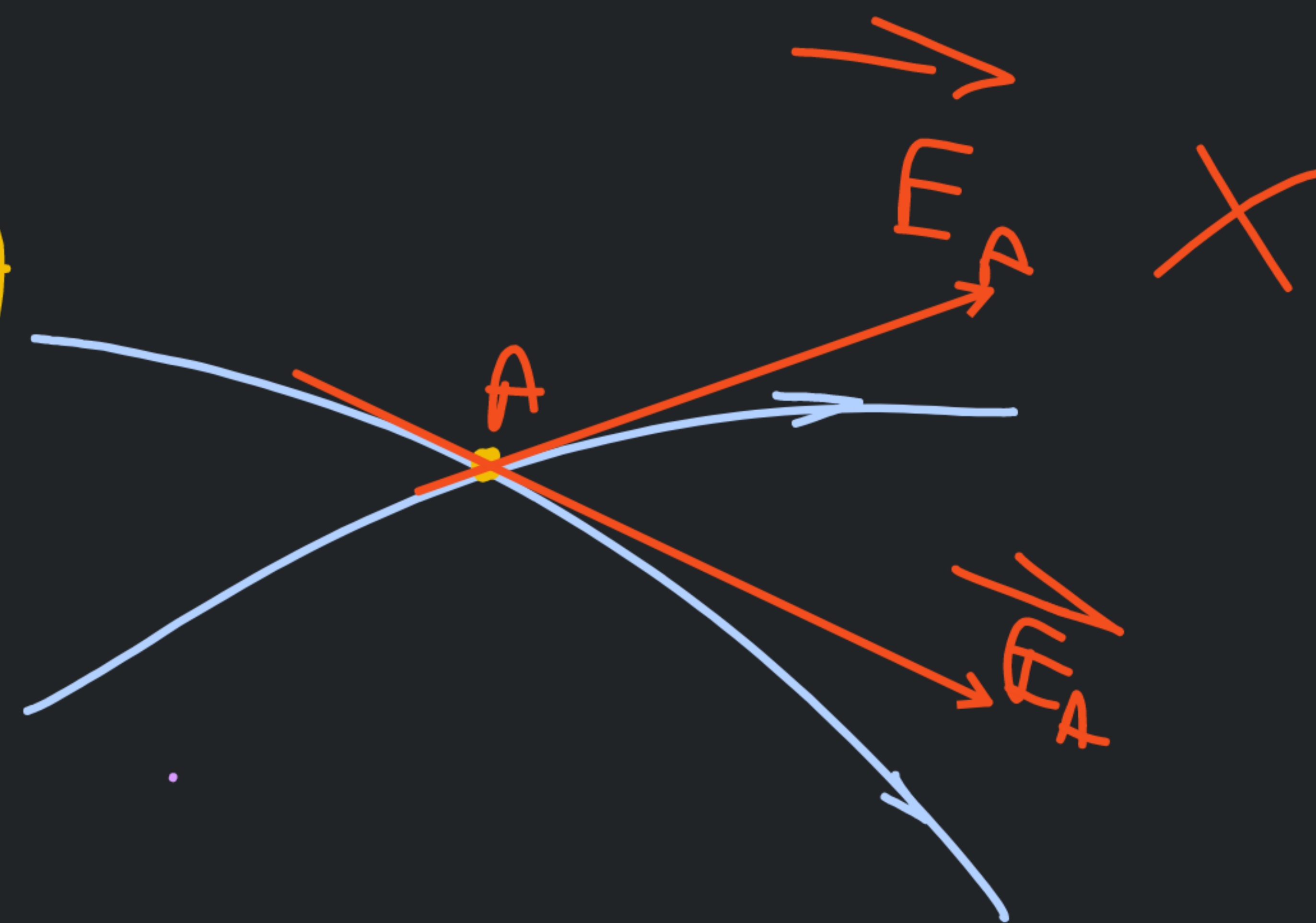


- (iii) If we draw a tangent on a point at field lines gives the direction of net field at that point.

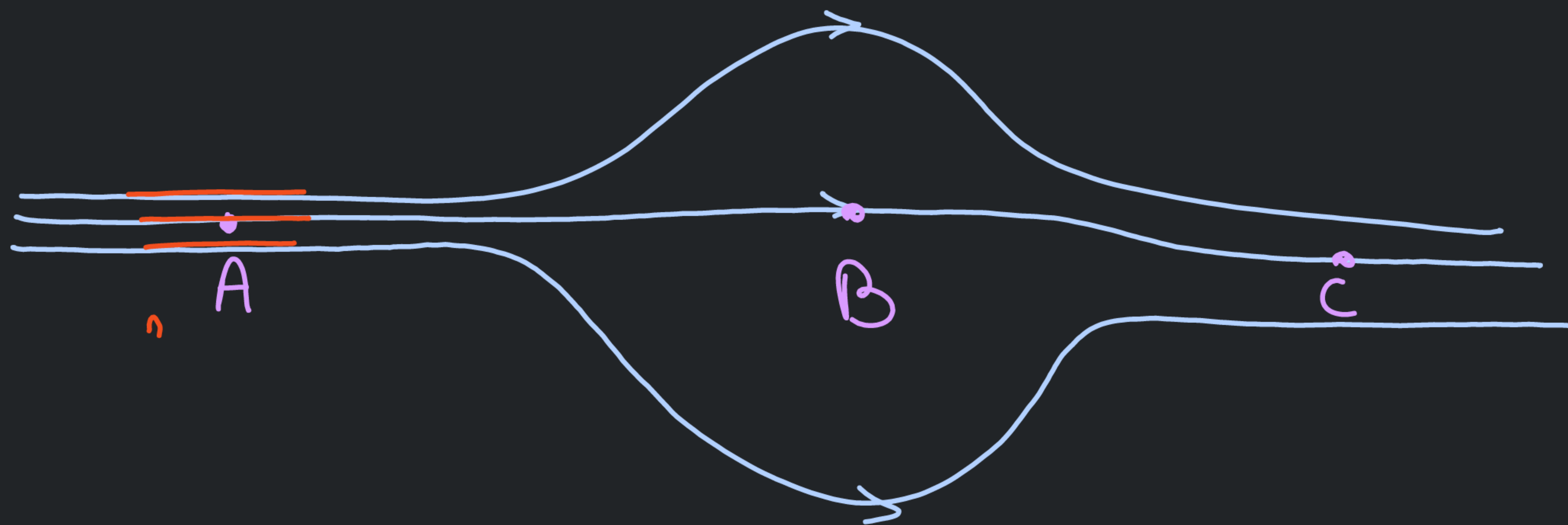


- (iv) Two electric field lines never intersect each other.

Reason:— If they do so then we get two direction of field at the point of intersection which is not possible.

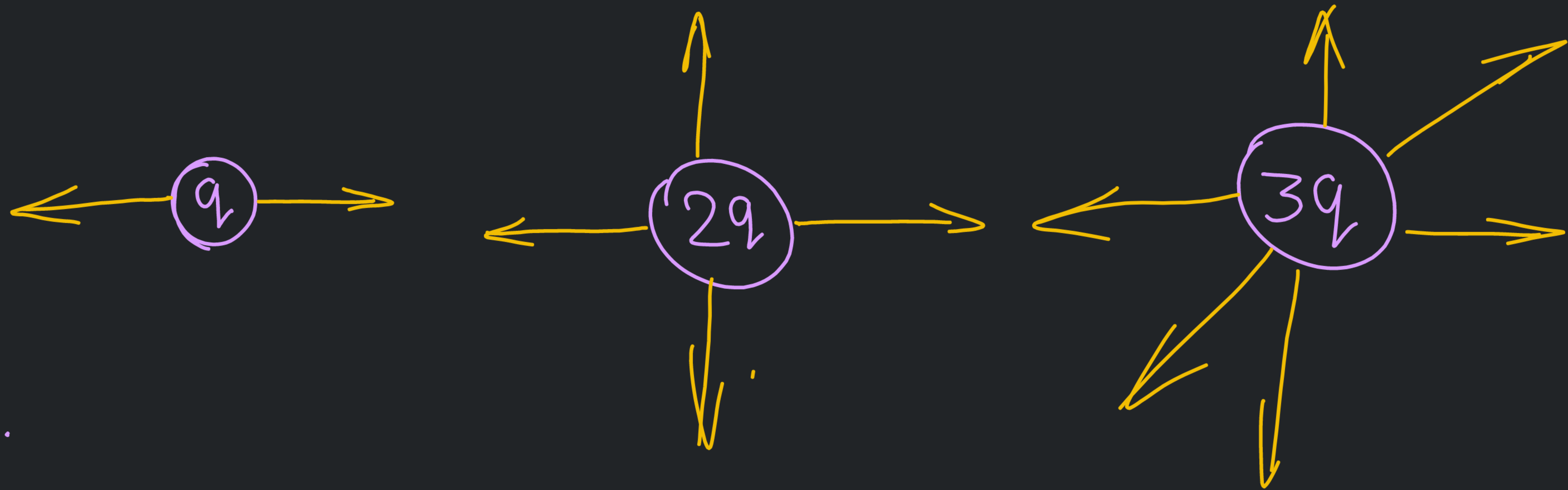


⑤ Relative closeness of field lines is proportional to magnitude of field.

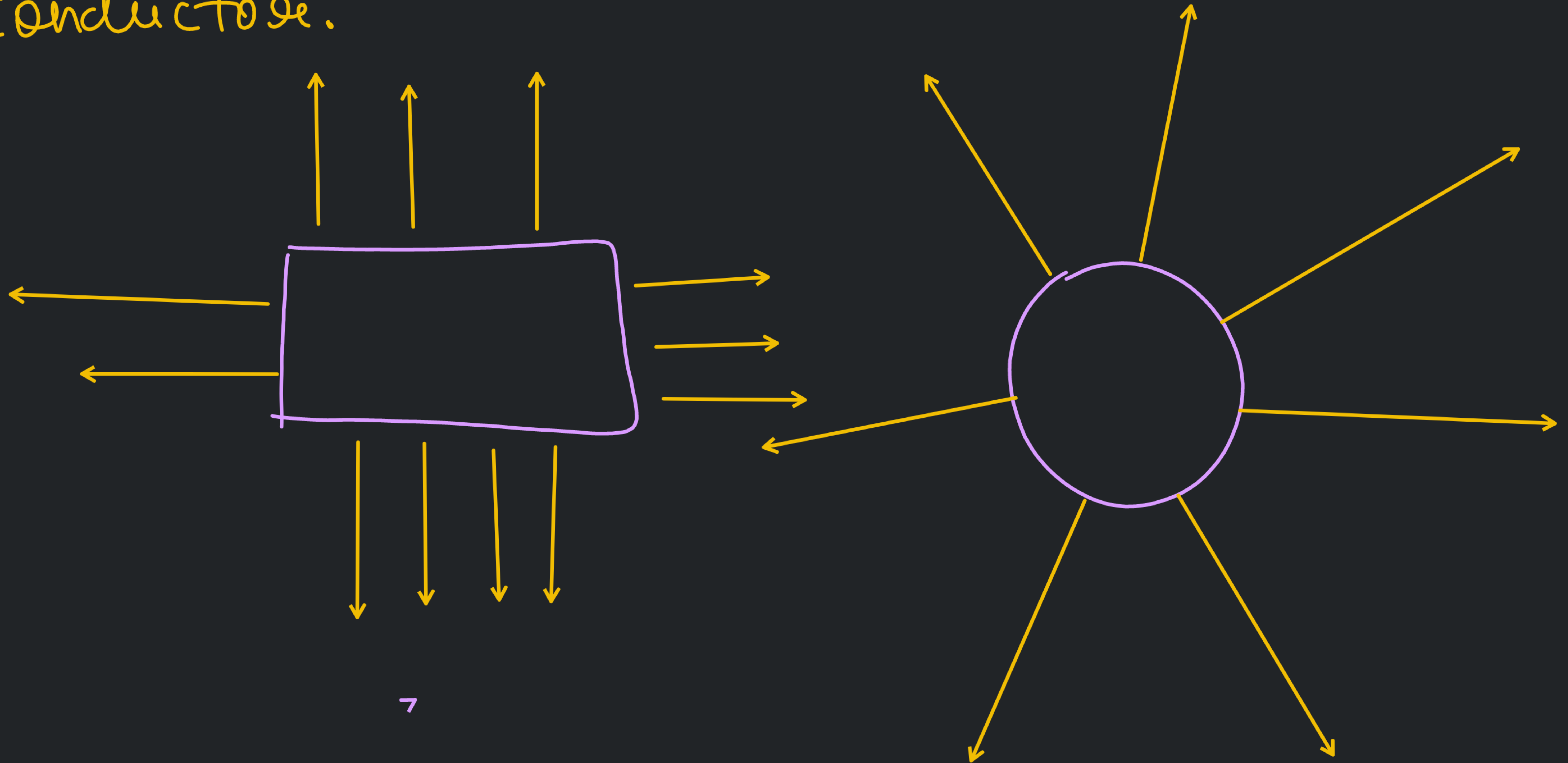


$$E_A > E_C > E_B$$

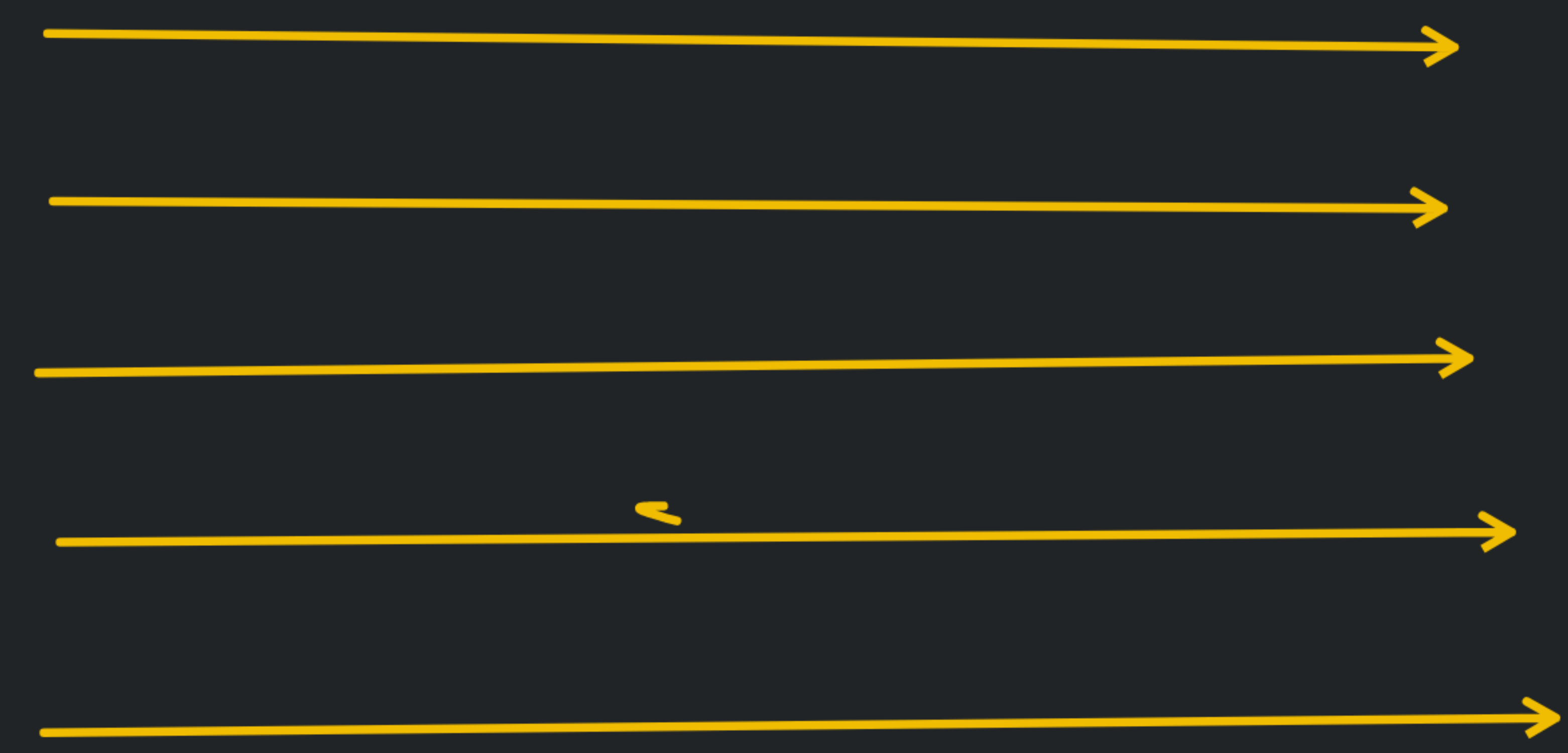
⑥ magnitude of electric field is directly proportional to no. of field lines:- (Subjective)



⑦ Field lines always perpendicular to the surface of conductors.



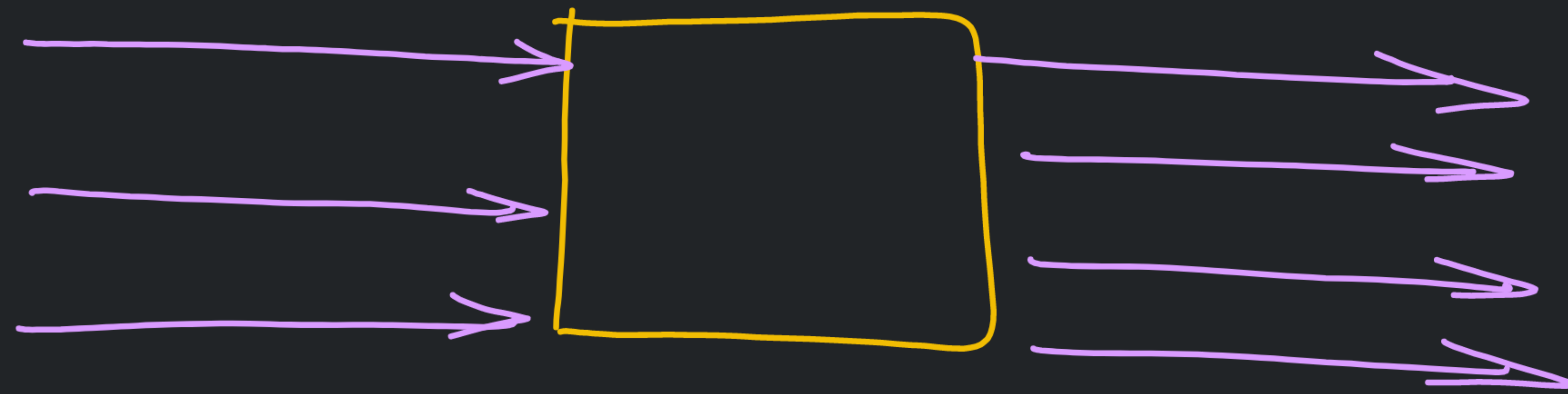
⑧ Equidistance, parallel and straight field lines form uniform electric field.



⑨ Electric field lines are always symmetric about line joining of two charges.



⑩ Field lines are absent inside the conductor.



Electric flux:- no. of electric field lines passing through any surface normally is called electric flux associated with that surface.

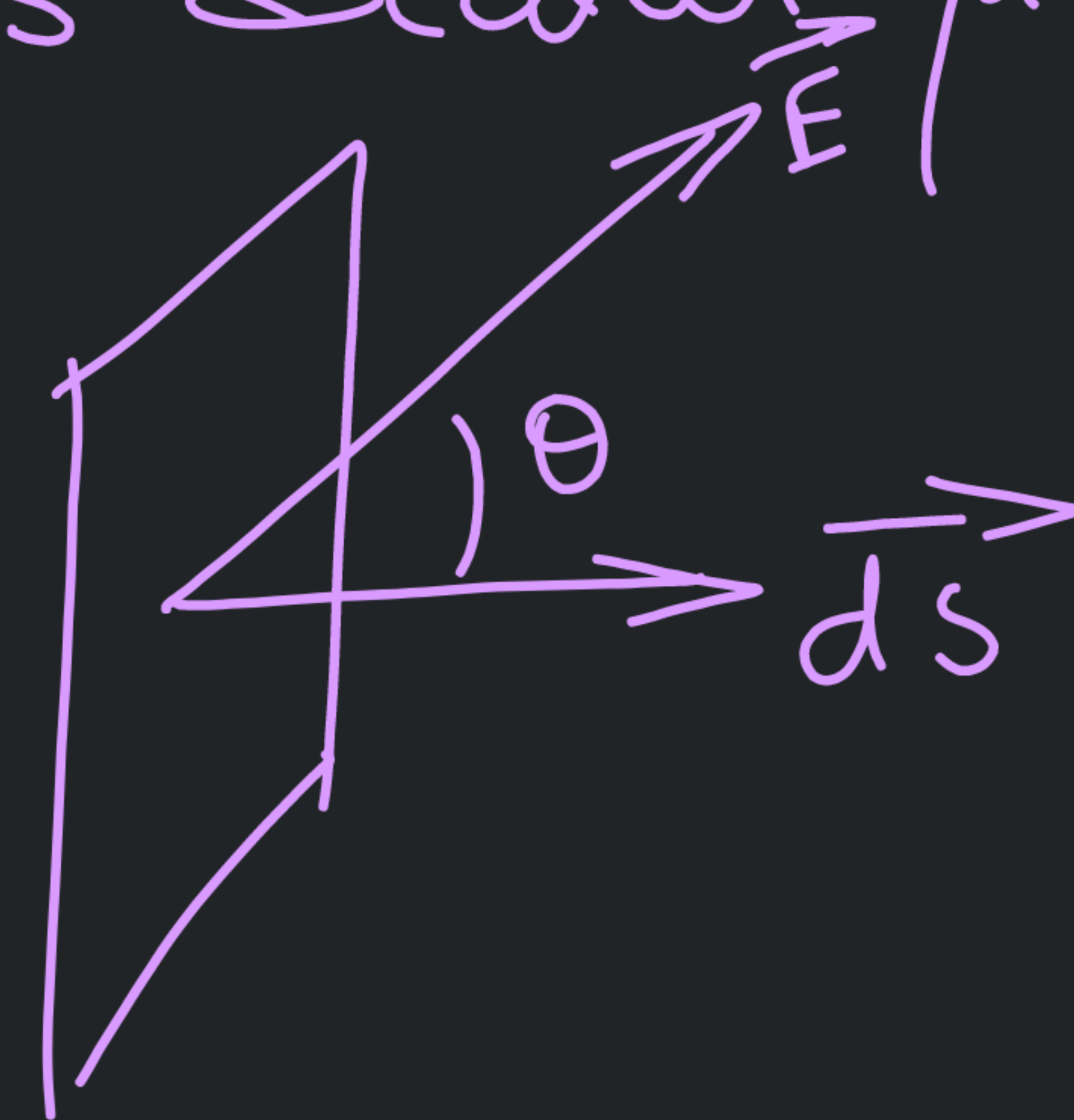
$$\phi = \vec{E} \cdot d\vec{s}$$

$$\phi_E = E ds \cos \theta$$

Unit: $\left(\frac{\text{Newton} \cdot \text{m}^2}{\text{Coulomb}} \right)$

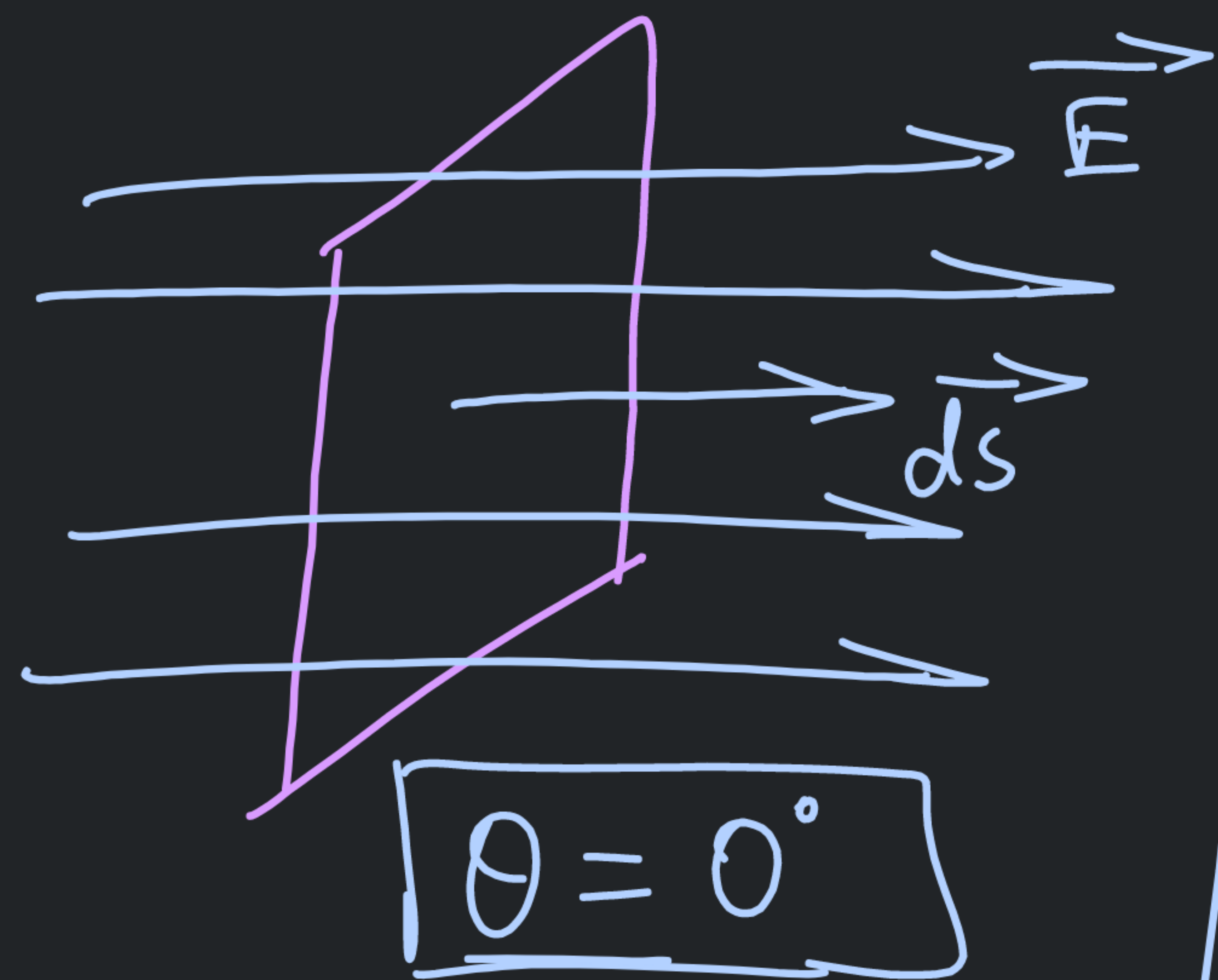
Dimensional formula:- 12-31
 $[M L^2 T^{-3} A^{-1}]$

It is scalar quantity



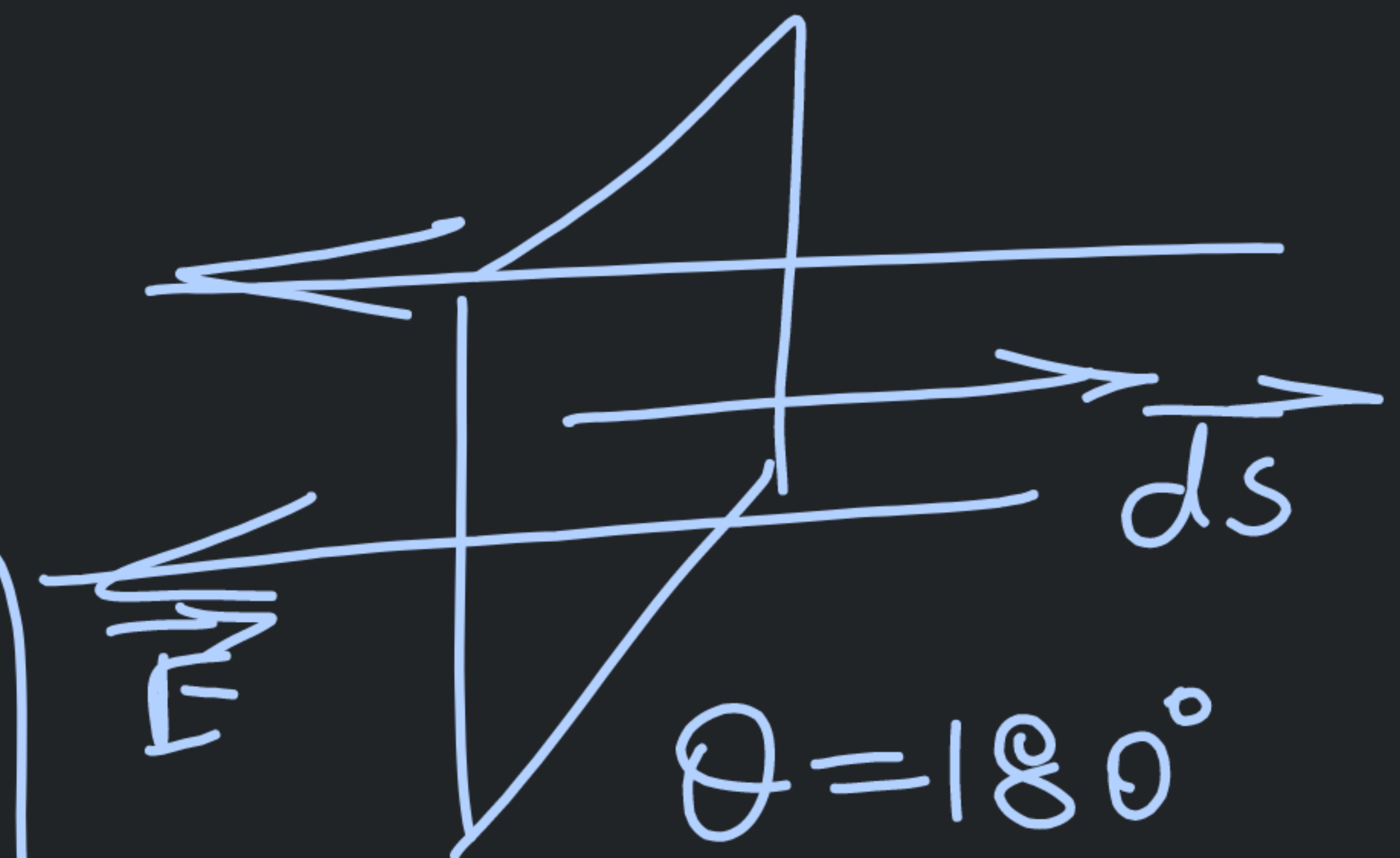
Special case:-

(i) Max. flux:-



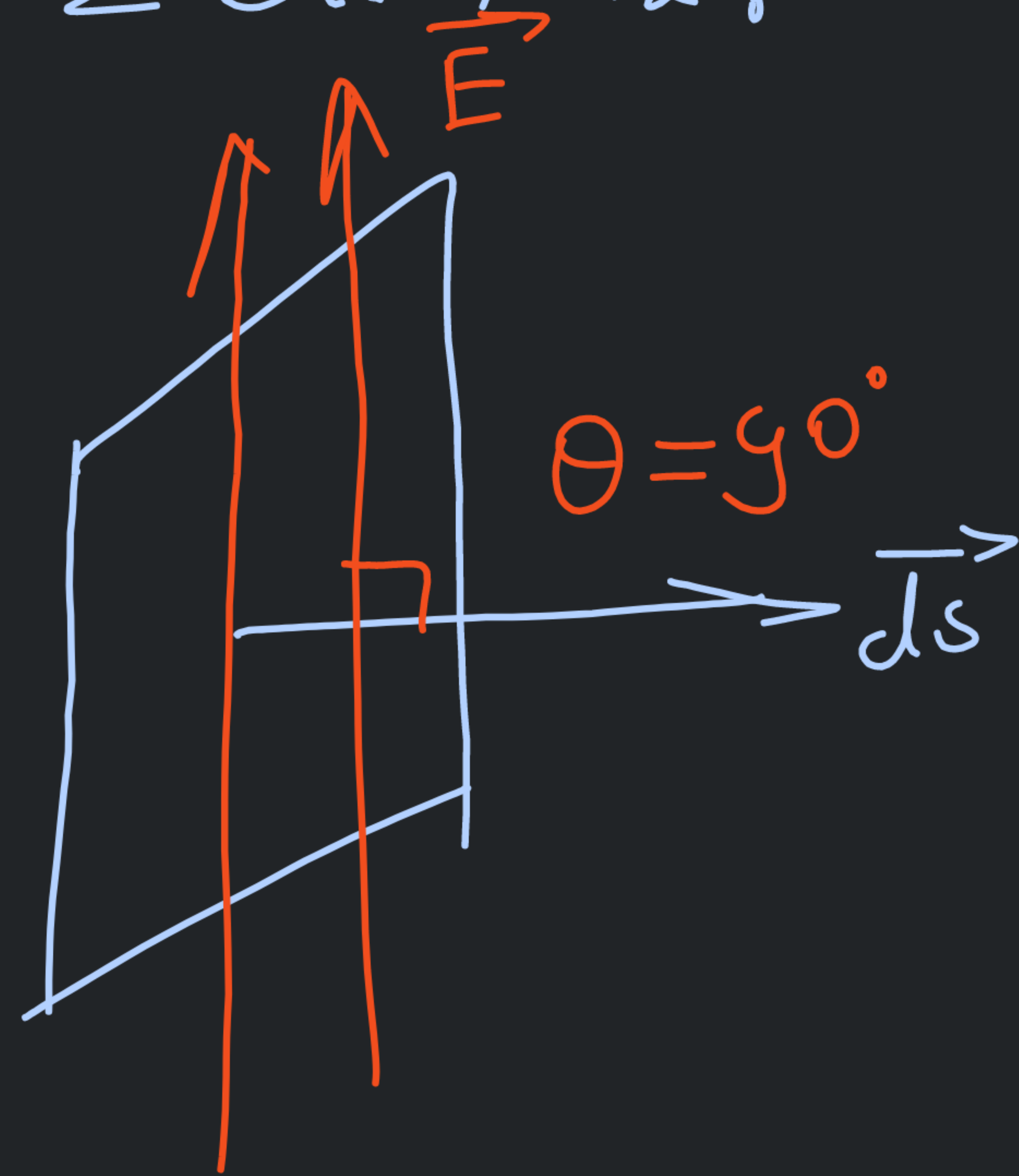
$$\begin{aligned}\phi &= Eds \cos 0 \\ &= Eds \cos 0^\circ \\ \phi &= Eds \text{ (max.)} \\ &\quad \text{(+ve flux)}\end{aligned}$$

(ii) -ve flux:-



$$\begin{aligned}\phi &= Eds \cos 180^\circ \\ \phi &= -Eds\end{aligned}$$

(iii) Zero flux:-



$$\phi = E ds \cos 90^\circ$$

$$\phi = 0$$

Gauss' law:- According to this law " net electric flux associated with closed surface is equal to $\frac{1}{\epsilon_0}$ times of net charge present inside the closed surface."

Closed surface $\rightarrow$ 3d
 $\swarrow$ sphere, cylinder, cube
 $\searrow$ Gaussian surface

$$\phi_{\text{closed surface}} = \frac{1}{\epsilon_0} \times q_{\text{net}}$$

$$\phi = \frac{q}{\epsilon_0}$$



Proof:-

Let a charge q present at centre of sphere with radius ' R '.

Let a point P on the surface of sphere then electric field at point:-

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{R^2} \quad \text{--- (1)}$$

Consider a small surface $d\vec{S}$ around point P then flux associated with $d\vec{S}$:-

$$d\phi = E dS \cos\theta$$

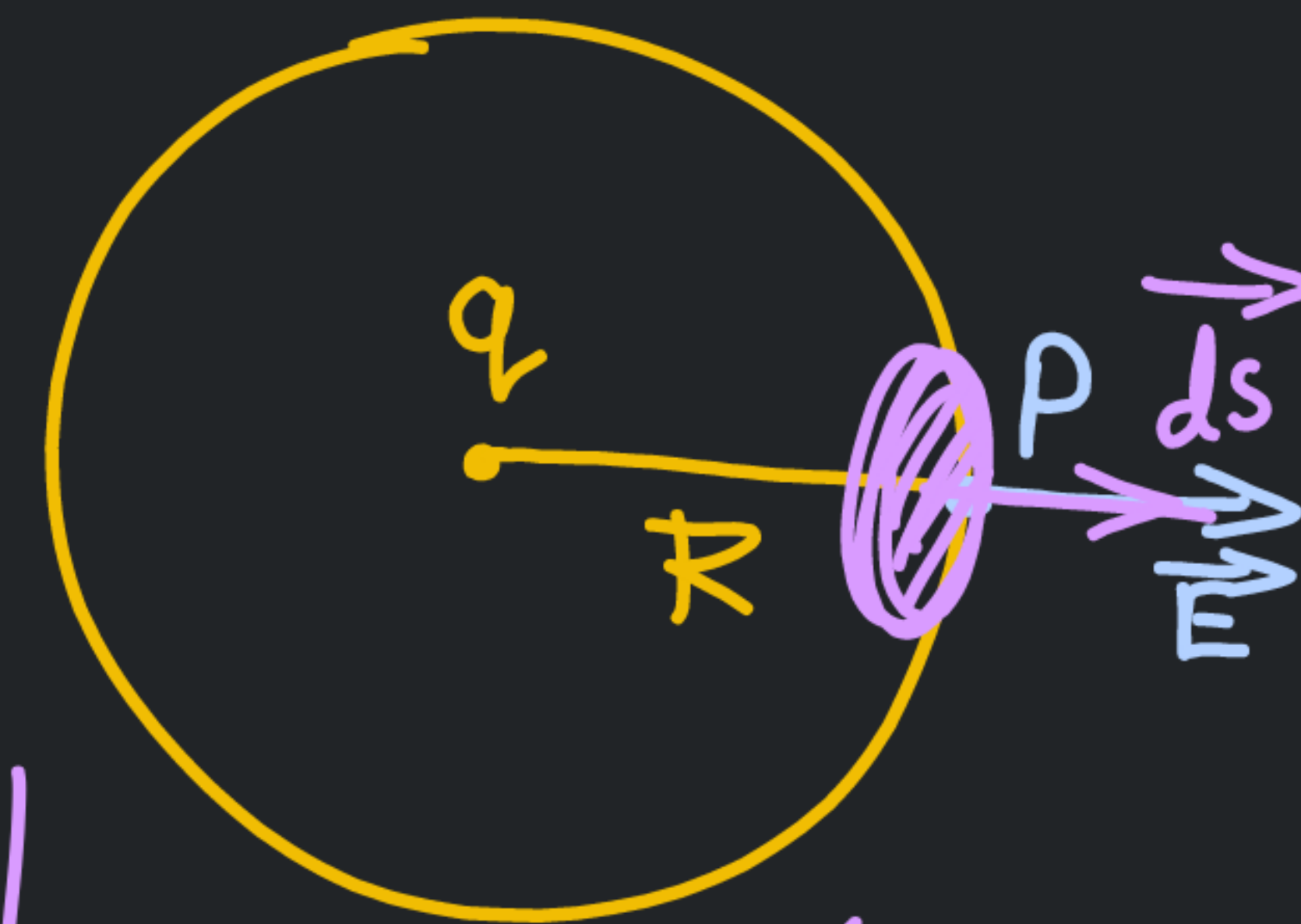
$$[\because \theta = 0^\circ \Rightarrow \cos 0^\circ = 1]$$

$$d\phi = E dS$$

Put the value of E from eqⁿ (1)

$$d\phi = \frac{1}{4\pi\epsilon_0} \frac{q}{R^2} dS$$

taking integral in both side of eqⁿ:-



$$\int d\phi = \int \frac{1}{4\pi\epsilon_0} \frac{q}{R^2} dS$$

$$\phi = \frac{q}{4\pi\epsilon_0 R^2} \int dS$$

$$[\because \int dS = 4\pi R^2]$$

$$\phi = \frac{q}{4\pi\epsilon_0 R^2} \times 4\pi R^2$$

$$\boxed{\phi = \frac{q}{\epsilon_0}}$$

Hence proved

Applications of Gauss' law:-

Continuous charge distribution:-

(i) Linear charge density:- charge per unit length

$$\lambda = \frac{Q}{l} \text{ C/m.}$$

(2) Surface charge density:- Charge per unit area.

$$\sigma = \frac{Q}{A} \text{ C/m}^2$$

③ Volume charge density:- charge per unit volume

$$\rho = \frac{Q}{\text{Volume}} \quad \text{C/m}^3$$

Intensity of electric field due to uniform charged infinite rod:-

flux associated with S_1 surface:-

$$d\phi_1 = E ds_1 \cos \theta$$

$$[\because \theta = 90^\circ \Rightarrow \cos 90^\circ = 0]$$

$$d\phi_1 = 0$$

$$\boxed{\phi_1 = 0}$$

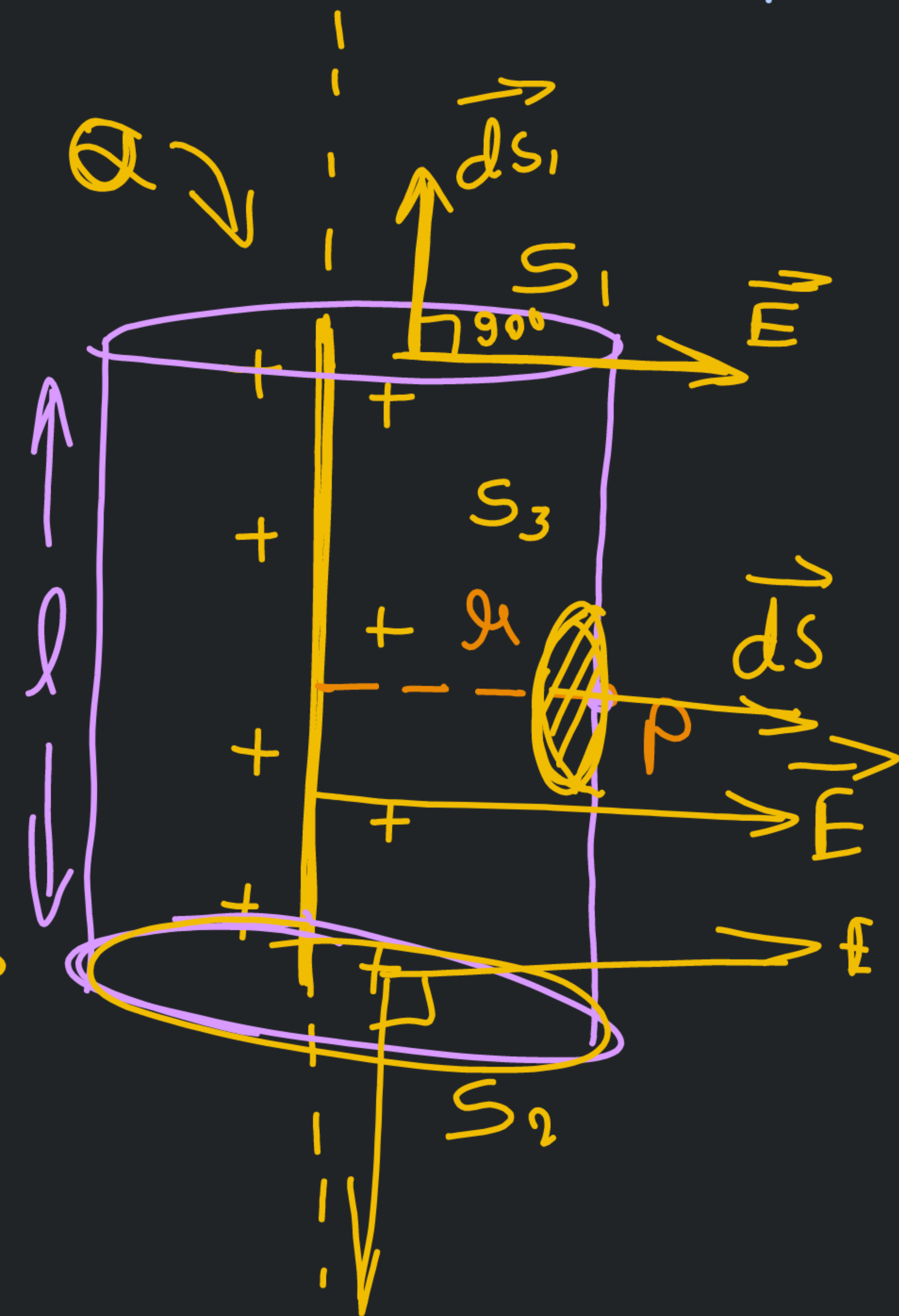
then flux associated with S_2 --

$$\boxed{\phi_2 = 0}$$

flux associated with S_3 Surface

$$d\phi_3 = E ds_3 \cos \theta$$

$$[\because \theta = 0^\circ \Rightarrow \cos 0^\circ = 1]$$



$$d\phi_3 = E ds_3$$

$$\int d\phi_3 = \int E ds_3$$

$$\phi_3 = E \int ds_3$$

$$\left[\because \int ds_3 = 2\pi r l \right]$$

$$\phi_3 = E \cdot 2\pi r l$$

net flux:-

$$\phi = \phi_1 + \phi_2 + \phi_3$$

$$\phi = 0 + 0 + E \cdot 2\pi r l$$

$$\phi = E \cdot 2\pi r l \text{ --- (1)}$$

but Gauss' law:-

$$\phi = \frac{Q}{\epsilon_0} \text{ --- (2)}$$

by eqⁿ (1) and (2)

$$E \cdot 2\pi r l = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{2\pi r l \epsilon_0}$$

$$E = \frac{1}{2\pi \epsilon_0} \left(\frac{Q}{l/r} \right)$$

$$\therefore \lambda = \frac{Q}{l}$$

$$E = \frac{1}{2\pi \epsilon_0} \frac{\lambda}{r} \text{ N/C}$$

Intensity of electric field due to uniform charged Sheet :-

flux associated with S_1

$$d\phi_1 = E ds_1 \cos \theta$$

$$[\because \theta = 0^\circ \Rightarrow \cos 0^\circ = 1]$$

$$d\phi_1 = E ds_1$$

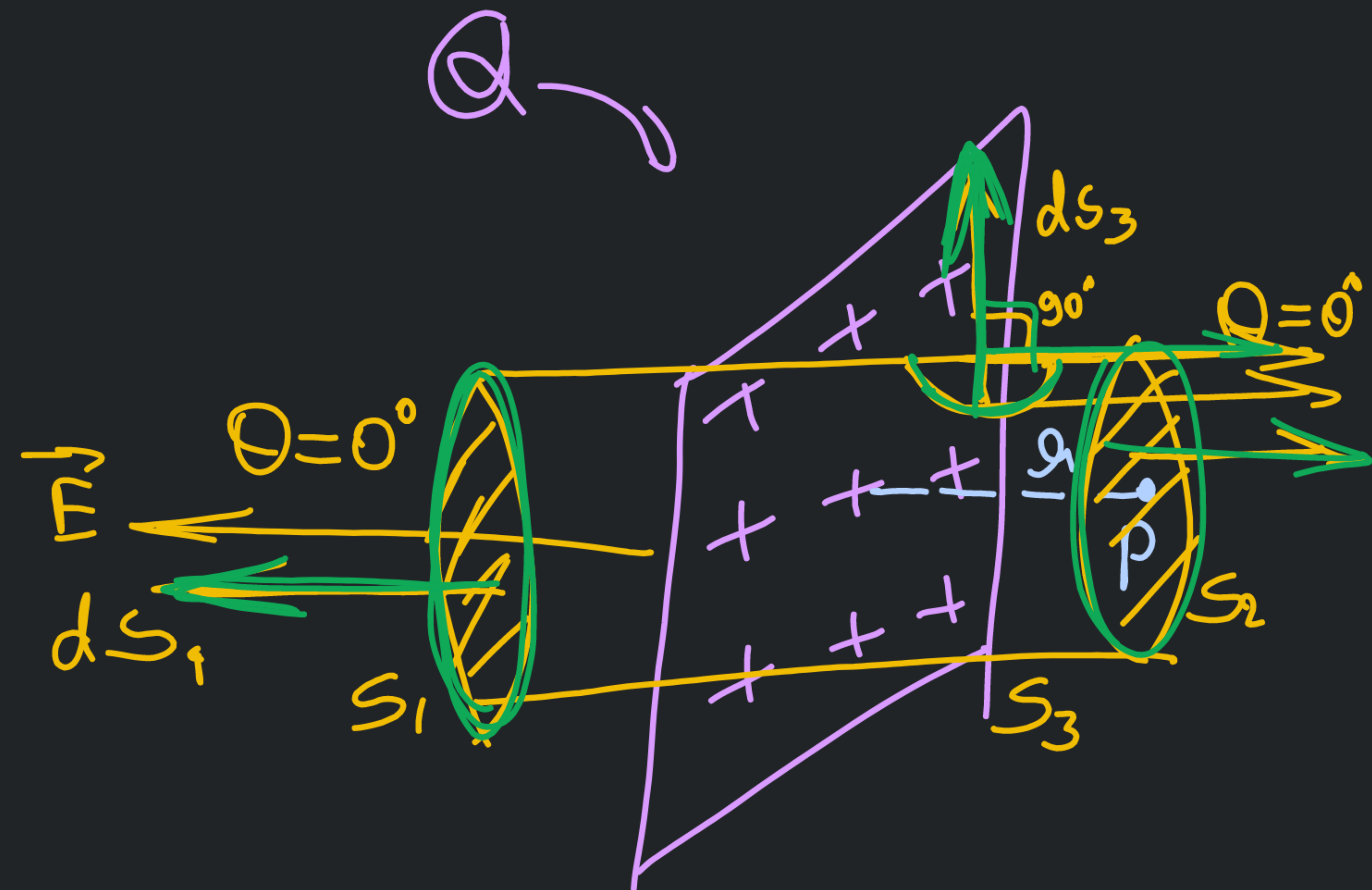
$$\int d\phi_1 = \int E ds_1$$

$$\phi_1 = E \int ds_1$$

$$\phi_1 = \underline{EA}$$

Similarly:-
 $\phi_2 = EA$

and $\phi_3 = 0$ $[\because \theta = 90^\circ]$



then net flux:-

$$\phi = \phi_1 + \phi_2 + \phi_3$$

$$\phi = EA + EA + 0$$

$$\phi = 2EA \text{ --- (1)}$$

but Gauss' flux:-

$$\phi = \frac{Q}{\epsilon_0} \text{ --- (2)}$$

by eqⁿ (1) and (2)

$$2EA = \frac{Q}{\epsilon_0}$$

$$E = \frac{(Q)}{2(A)\epsilon_0}$$

$$\left[\therefore \sigma = \frac{Q}{A} \right]$$

$$E = \frac{\sigma}{2\epsilon_0}$$

Intensity of electric field due to uniform charge hollow sphere (Shell)

① Outside the sphere:-

flux associated with $\vec{ds}$

$$d\phi = E ds \cos \theta$$

$$[\because \theta = 0^\circ \Rightarrow \cos 0^\circ = 1]$$

$$d\phi = E ds$$

$$\int d\phi = \int E ds$$

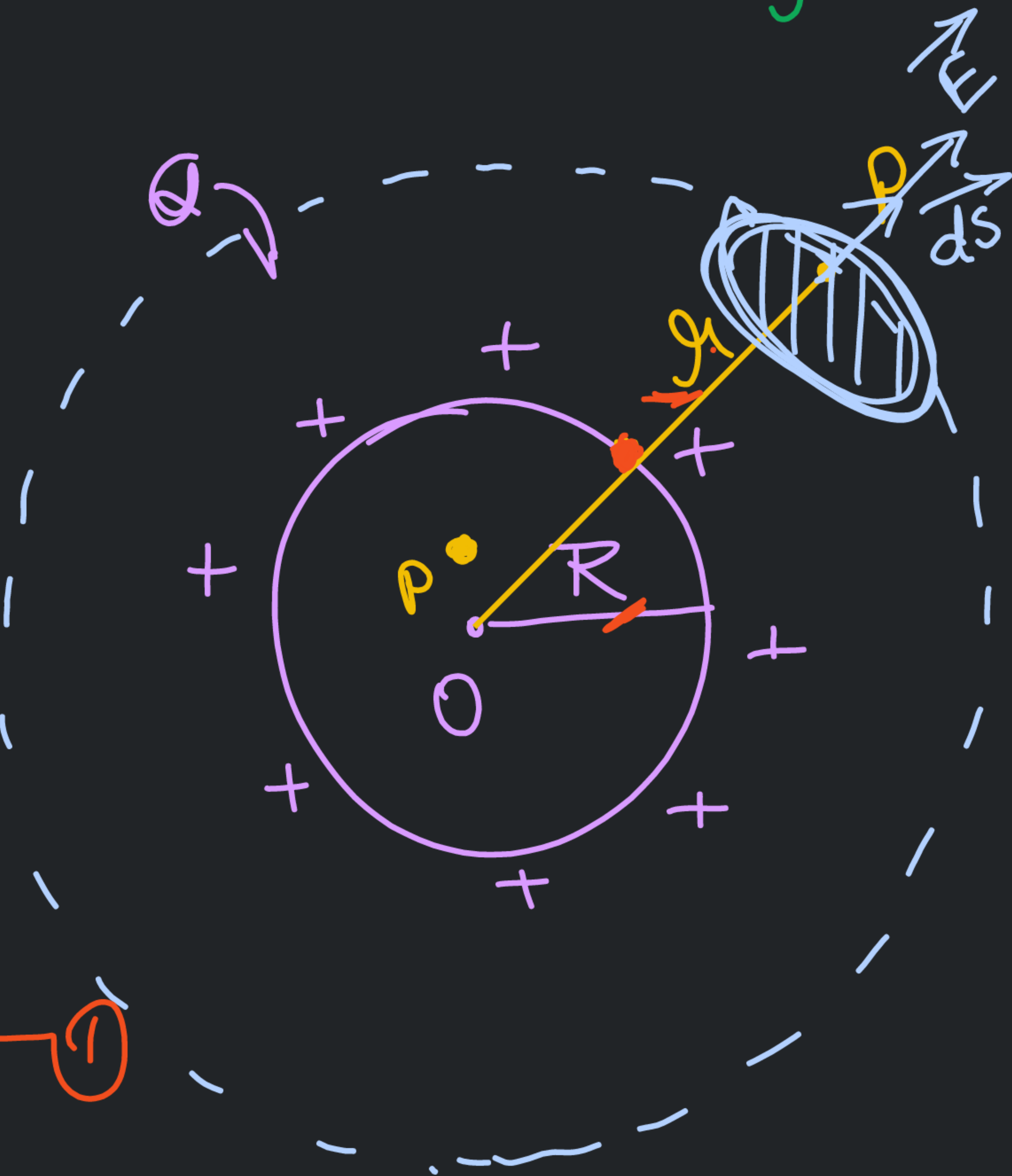
$$\phi = E \int ds$$

$$[\because \int ds = 4\pi R^2]$$

$$\phi = \frac{E \cdot 4\pi R^2}{1} \quad \text{--- ①}$$

but Gauss' law:-

$$\phi = \frac{Q}{\epsilon_0} \quad \text{--- ②}$$



by eqⁿ ① and ②

$$E \cdot 4\pi r^2 = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{4\pi r^2 \epsilon_0}$$

$$E = \frac{1}{4\pi \epsilon_0} \frac{Q}{r^2} \quad \text{N/C}$$

② On the sphere ($r = \underline{R}$)

$$E = \frac{1}{4\pi \epsilon_0} \frac{Q}{R^2}$$

N/C
Constant

③ Inside the sphere:-

$$q_{\text{inside}} = 0$$

hence

$$E = 0$$



Coulomb's law with the help of Gauss' law:—

Let a charge q present at the centre of sphere of radius R then

Consider a point P and a small area ds around P on the surface of sphere. then flux associated with $\vec{ds}$:-

$$d\phi = E ds \cos \theta$$

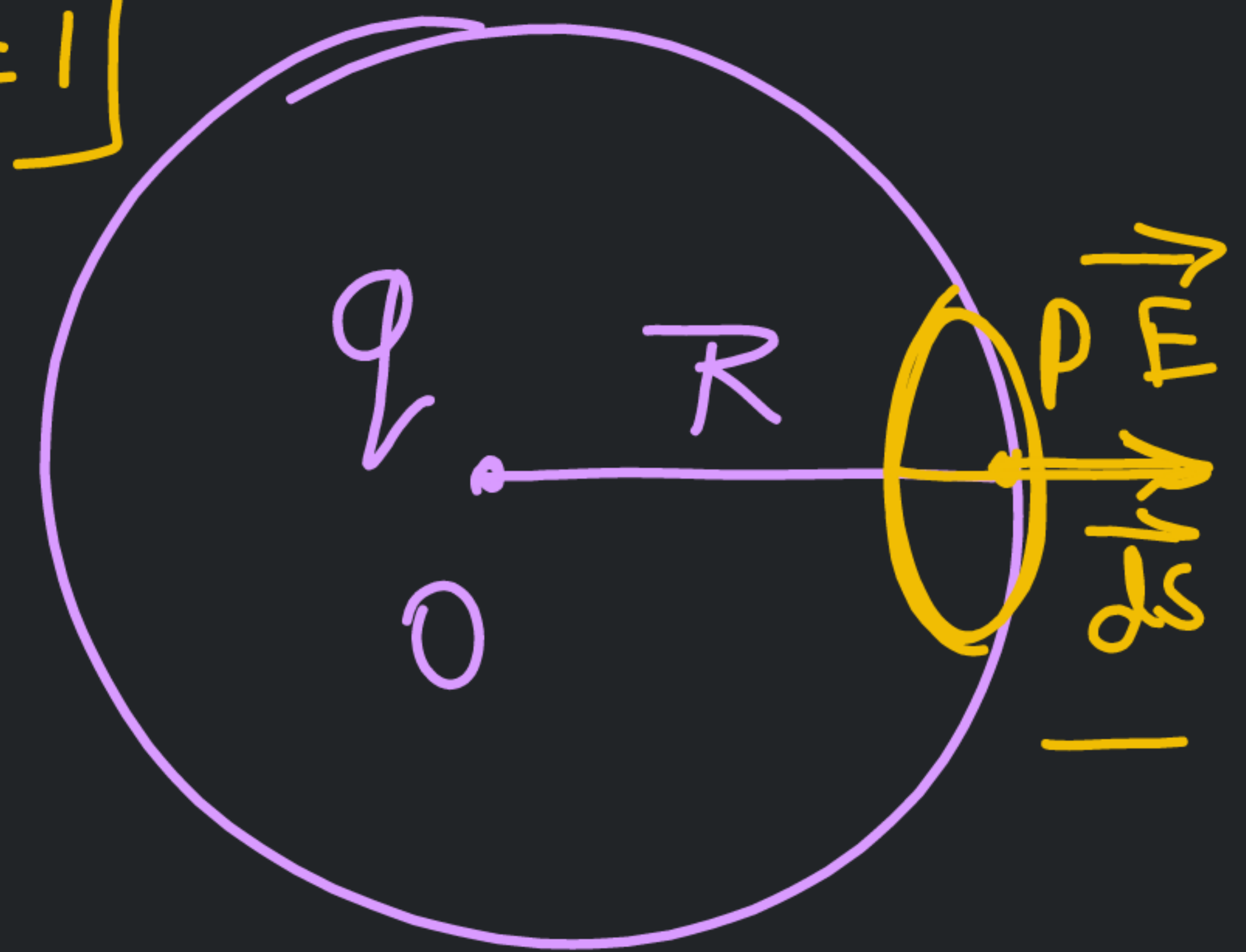
$$[\because \theta = 0^\circ \Rightarrow \cos 0^\circ = 1]$$

$$d\phi = E ds$$

$$\int d\phi = \int E ds$$

$$\phi = E \int ds$$

$$[\because \int ds = 4\pi R^2]$$



$$\phi = E \cdot 4\pi R^2 \text{ --- (1)}$$

but Gauss' law:-

$$\phi = \frac{q}{\epsilon_0} \text{ --- (2)}$$

by eqⁿ (1) and (2)

$$E \cdot 4\pi R^2 = \frac{q}{\epsilon_0}$$

$$E = \frac{q}{4\pi R^2 \epsilon_0}$$

$$E = \frac{1}{4\pi \epsilon_0} \frac{q}{R^2} \text{ --- (3)}$$

but force on charge inside field:-

$$F = q_0 E$$

then

$$F = q_0 \left(\frac{1}{4\pi \epsilon_0} \frac{q}{R^2} \right)$$

$$F = \frac{1}{4\pi \epsilon_0} \frac{q q_0}{R^2} \text{ --- } \underline{\underline{N}}$$

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